- Find the quotient obtained in dividing
 - **a** $(x^3 + 2x^2 x 2)$ by (x + 1)
 - $c (20 + x + 3x^2 + x^3)$ by (x + 4)
 - e $(6x^3 19x^2 73x + 90)$ by (x 5)
 - $g(x^3-2x+21)$ by (x+3)

- **b** $(x^3 + 2x^2 9x + 2)$ by (x 2)
- **d** $(2x^3 x^2 4x + 3)$ by (x 1)
- $\mathbf{f} = (-x^3 + 5x^2 + 10x 8)$ by (x + 2)
- **h** $(3x^3 + 16x^2 + 72)$ by (x+6)
- 2 Find the quotient and remainder obtained in dividing
 - **a** $(x^3 + 8x^2 + 17x + 16)$ by (x + 5)
- **b** $(x^3 15x^2 + 61x 48)$ by (x 7)
- c $(3x^3 + 4x^2 + 7)$ by (2 + x)

- **d** $(-x^3 5x^2 + 15x 50)$ by (x + 8)
- e $(4x^3 + 2x^2 16x + 3)$ by (x 3)
- \mathbf{f} $(1-22x^2-6x^3)$ by (x+2)
- Use the factor theorem to determine whether or not 3

 - **a** (x-1) is a factor of $(x^3 + 2x^2 2x 1)$ **b** (x+2) is a factor of $(x^3 5x^2 9x + 2)$ **c** (x-3) is a factor of $(x^3 x^2 14x + 27)$ **d** (x+6) is a factor of $(2x^3 + 13x^2 + 2x 24)$

- e (2x+1) is a factor of $(2x^3-5x^2+7x-14)$ f (3x-2) is a factor of $(2-17x+25x^2-6x^3)$
- $f(x) \equiv x^3 2x^2 11x + 12$. 4
 - a Show that (x 1) is a factor of f(x).
 - **b** Hence, express f(x) as the product of three linear factors.
- $g(x) \equiv 2x^3 + x^2 13x + 6$. 5
 - Show that (x + 3) is a factor of g(x) and solve the equation g(x) = 0.
- $f(x) \equiv 6x^3 7x^2 71x + 12$. 6
 - Given that f(4) = 0, find all solutions to the equation f(x) = 0.
- $g(x) \equiv x^3 + 7x^2 + 7x 6$ 7
 - Given that x = -2 is a solution to the equation g(x) = 0,
 - a express g(x) as the product of a linear factor and a quadratic factor,
 - **b** find, to 2 decimal places, the other two solutions to the equation g(x) = 0.
- $f(x) \equiv x^3 + 2x^2 11x 12$ 8
 - **a** Evaluate f(1), f(2), f(-1) and f(-2).
 - **b** Hence, state a linear factor of f(x) and fully factorise f(x).
- By first finding a linear factor, fully factorise 9
 - **a** $x^3 2x^2 5x + 6$
- **b** $x^3 + x^2 5x 2$
- c 20 + 11x 8x² + x³

- **d** $3x^3 4x^2 35x + 12$
- **e** $x^3 + 8$

- \mathbf{f} 12 + 29x + 8x² 4x³
- Solve each equation, giving your answers in exact form. 10

 - **a** $x^3 x^2 10x 8 = 0$ **b** $x^3 + 2x^2 9x 18 = 0$
- $\mathbf{c} \quad 4x^3 12x^2 + 9x = 2$

- **d** $x^3 5x^2 + 3x + 1 = 0$
- e $x^2(x+4) = 3(3x+2)$ f $x^3 14x + 15 = 0$



11
$$f(x) = 2x^3 - x^2 - 15x + c.$$

Given that (x-2) is a factor of f(x),

- a find the value of the constant c,
- **b** fully factorise f(x).

12
$$g(x) \equiv x^3 + px^2 - 13x + q$$
.

Given that (x + 1) and (x - 3) are factors of g(x),

- a show that p = 3 and find the value of q,
- **b** solve the equation g(x) = 0.
- Use the remainder theorem to find the remainder obtained in dividing 13

a
$$(x^3 + 4x^2 - x + 6)$$
 by $(x - 2)$

b
$$(x^3 - 2x^2 + 7x + 1)$$
 by $(x + 1)$

c
$$(2x^3 + x^2 - 9x + 17)$$
 by $(x + 5)$

c
$$(2x^3 + x^2 - 9x + 17)$$
 by $(x + 5)$ **d** $(8x^3 + 4x^2 - 6x - 3)$ by $(2x - 1)$ **e** $(2x^3 - 3x^2 - 20x - 7)$ by $(2x + 1)$ **f** $(3x^3 - 6x^2 + 2x - 7)$ by $(3x - 2)$

e
$$(2x^3 - 3x^2 - 20x - 7)$$
 by $(2x + 1)$

$$\mathbf{f}$$
 $(3x^3 - 6x^2 + 2x - 7)$ by $(3x - 2)$

- Given that when $(x^3 4x^2 + 5x + c)$ is divided by (x 2) the remainder is 5, find the value of the 14 constant c.
- Given that when $(2x^3 9x^2 + kx + 5)$ is divided by (2x 1) the remainder is -2, find the value of 15 the constant k.
- Given that when $(2x^3 + ax^2 + 13)$ is divided by (x + 3) the remainder is 22, 16
 - a find the value of the constant a.
 - **b** find the remainder when $(2x^3 + ax^2 + 13)$ is divided by (x 4).

17
$$f(x) = px^3 + qx^2 + qx + 3.$$

Given that (x + 1) is a factor of f(x),

a find the value of the constant p.

Given also that when f(x) is divided by (x - 2) the remainder is 15,

b find the value of the constant q.

18
$$p(x) \equiv x^3 + ax^2 + 9x + b.$$

Given that (x-3) is a factor of p(x),

a find a linear relationship between the constants a and b.

Given also that when p(x) is divided by (x + 2) the remainder is -30,

b find the values of the constants a and b.

19
$$f(x) = 4x^3 - 6x^2 + mx + n.$$

Given that when f(x) is divided by (x + 1) the remainder is 3 and that when f(x) is divided by (2x - 1) the remainder is 15, find the values of the constants m and n.

20
$$g(x) \equiv x^3 + cx + 3.$$

Given that when g(x) is divided by (x - 4) the remainder is 39,

- a find the value of the constant c,
- **b** find the quotient and remainder when g(x) is divided by (x + 2).



1

$$f(x) \equiv x^3 - 5x^2 + ax + b$$
.

Given that (x + 2) and (x - 3) are factors of f(x),

- a show that a = -2 and find the value of b.
- **b** Hence, express f(x) as the product of three linear factors.

2

$$f(x) \equiv 8x^3 - x^2 + 7.$$

The remainder when f(x) is divided by (x - k) is eight times the remainder when f(x) is divided by (2x - k).

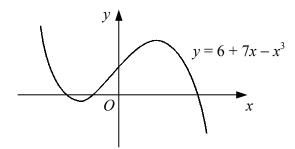
Find the two possible values of the constant k.

3

$$f(x) \equiv 3x^3 - x^2 - 12x + 4.$$

- a Show that (x-2) is a factor of f(x).
- **b** Solve the equation f(x) = 0.

4



The diagram shows the curve with the equation $y = 6 + 7x - x^3$.

Find the coordinates of the points where the curve crosses the x-axis.

5

$$f(x) = 3x^3 + px^2 + 8x + q.$$

When f(x) is divided by (x + 1) there is a remainder of -4.

When f(x) is divided by (x - 2) there is a remainder of 80.

- **a** Find the values of the constants p and q.
- **b** Show that (x + 2) is a factor of f(x).
- **c** Solve the equation f(x) = 0.

6

Solve the equation

$$x^3 - 4x^2 - 7x + 10 = 0.$$

b Hence, solve the equation

$$y^6 - 4y^4 - 7y^2 + 10 = 0.$$

7

$$f(n) \equiv n^3 + 7n^2 + 14n + 3.$$

- **a** Find the remainder when f(n) is divided by (n + 1).
- **b** Express f(n) in the form

$$f(n) \equiv (n+1)(n+a)(n+b) + c$$
,

where a, b and c are integers.

c Hence, show that f(n) is odd for all positive integer values of n.

