

Solomon Practice Paper

Pure Mathematics 5D

Time allowed: 90 minutes

Centre: www.CasperYC.club

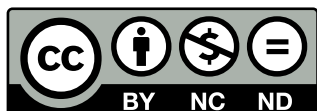
Name:

Teacher:

Question	Points	Score
1	5	
2	5	
3	11	
4	12	
5	13	
6	13	
7	16	
Total:	75	

How I can achieve better:

-
-
-



Last updated: July 14, 2025



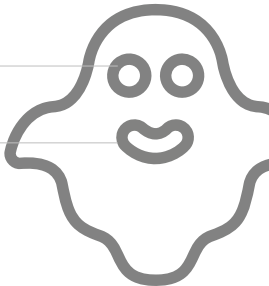
1.

$$y = \frac{\operatorname{cosech}(x)}{x^2 + 1}.$$

(a) Find $\frac{dy}{dx}$. [4]

(b) Find the value of $\frac{dy}{dx}$ when $x = 0.5$, giving your answer to 2 decimal places. [1]

Total: 5



2. A curve has intrinsic coordinates (s, ψ) and radius of curvature ρ .

[5]

Given that $\rho = 2(s + a)$, where a is constant, show that the intrinsic equation of the curve can be written in the form

$$s = Ae^{2\psi} - a,$$

where A is constant.



3. (a) Prove that [5]

$$\sinh(3x) \equiv 4 \sinh^3(x) + 3 \sinh(x).$$

(b) Hence, or otherwise, solve the equation [6]

$$\sinh(3x) = 7 \sinh^2(x),$$

giving your answers in terms of natural logarithms where appropriate.

Total: 11

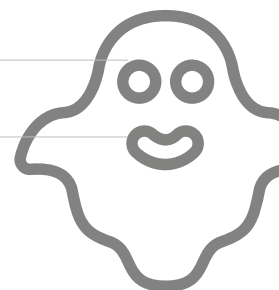


4. (a) Find $\int \frac{1}{\sqrt{9-4x^2}} dx$. [3]
- (b) Find $\int \frac{1-2x}{\sqrt{9-4x^2}} dx$. [3]
- (c) Hence, or otherwise, solve the differential equation [6]

$$\sqrt{9-4x^2} \frac{dy}{dx} = y(1-2x),$$

given that $y = 1$ when $x = 0$.

Total: 12



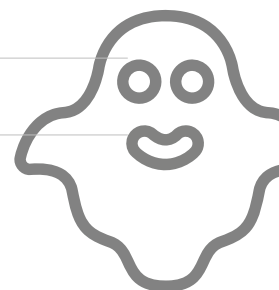
(a) Show that an equation of the tangent to C at the point $P(ap^2, 2ap)$, $p \neq 0$, is

$$yp = x + ap^2.$$

(b) $pq = -1$, [5]

(c) the tangent to C at P and the tangent to C at Q meet on the directrix of C . [4]

Total: 13



$$I_n = \int_0^{\frac{\pi}{4}} \sec^n(x) \, dx, \quad n \geq 0.$$

[7]

(b) Hence find the exact value of I_3 , giving your answer in terms of natural logarithms.

[6]

Total: 13



[9]

The parametric equations of the curve C are

[4]

[3]

Total: 16

