

Solomon Practice Paper

Pure Mathematics 5A

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	5	
2	8	
3	9	
4	10	
5	10	
6	10	
7	11	
8	12	
Total:	75	

How I can achieve better:

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Last updated: July 14, 2025

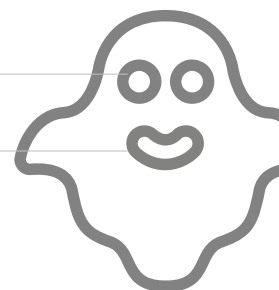


1. A curve has the equation

[5]

$$y = x + 2x^2 + 5x^3.$$

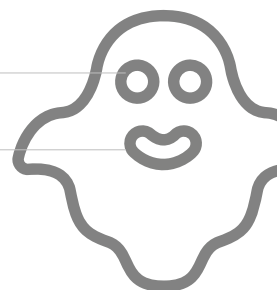
Show that the radius of curvature of the curve at the origin is $\frac{1}{\sqrt{2}}$.



2. Show that

[8]

$$\int_0^{\ln(2)} x \operatorname{sech}^2(x) \, dx = \frac{3}{5} \ln(2) - \ln\left(\frac{5}{4}\right).$$



[3]

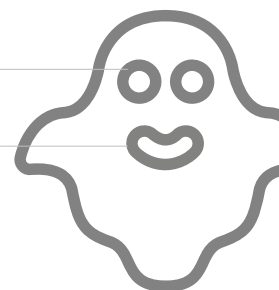
$$\frac{d}{dx} \arcsin(2x) = \frac{2}{\sqrt{1-4x^2}}.$$

$$f(x) = 2x \arcsin(2x) + \sqrt{1 - 4x^2},$$

[6]

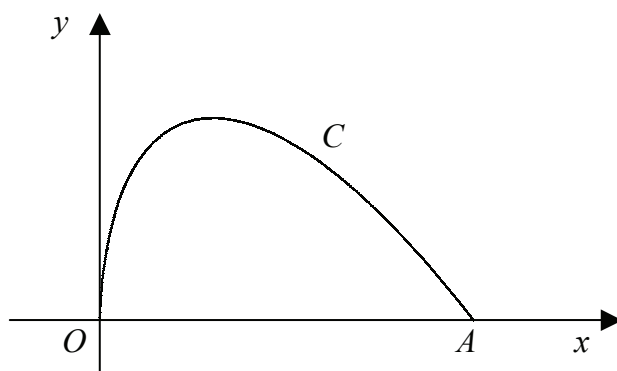
$$f''(x) [f(x) - xf'(x)] = 4.$$

Total: 9



4. The parametric coordinates of the curve C shown above are

$$x = t^2, \quad \text{and} \quad y = t - \frac{1}{3}t^3, \quad 0 \leq t \leq a.$$



The curve C meets the x -axis at the point A where $t = a$.

(a) Find the value of a .

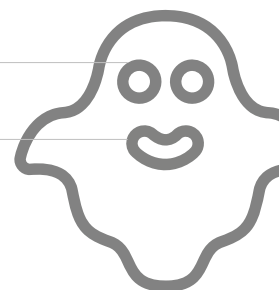
[2]

The curve C is rotated through 2π about Ox .

(b) Find the surface area of the solid generated.

[8]

Total: 10

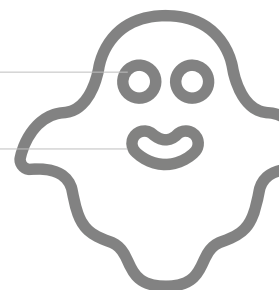


- $$\cosh(2x) = 2 \cosh^2(x) - 1.$$

- $$2 \cosh(2x) = 13 \cosh(x) - 12,$$

giving your answers in terms of natural logarithms.

Total: 10



6.

$$x^2 - 10x + 41 \equiv (x + a)^2 + b.$$

(a) Find the values of the constants a and b .

[2]

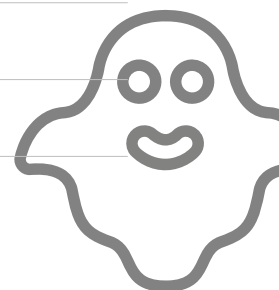
(b) Show that

[8]

$$\int_5^9 \frac{x}{\sqrt{x^2 - 10x + 41}} dx = p(\sqrt{2} - 1) + q \ln(r),$$

stating your values of p, q and r .

Total: 10



7.

$$I_n = \int_0^{\frac{\pi}{2}} x^n \cos(x) \, dx \quad n \geq 0.$$

(a) Prove that

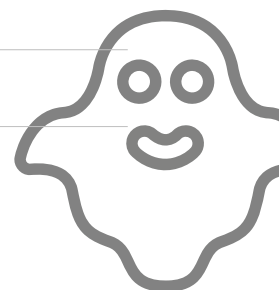
[5]

$$I_n = \left(\frac{\pi}{2}\right) - n(n-1)I_{n-2}, \quad n \geq 2.$$

(b) Hence find the value of I_4 , giving your answer in terms of π .

[6]

Total: 11



(a) Show that an equation of the tangent to C at the point $P\left(cp, \frac{c}{p}\right)$ is [4]

The tangent to C at P meets the x -axis at the point X .

(b) Show that $q = 2p$. [3]

(c) Find, in Cartesian form, an equation of the locus of M as p varies. [5]

Total: 12

