

Solomon Practice Paper

Pure Mathematics 4G

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	7	
2	7	
3	9	
4	11	
5	12	
6	12	
7	17	
Total:	75	

How I can achieve better:

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Last updated: July 14, 2025



1. Find the set of values of x for which

$$\frac{x^2 - 12}{x} \geq 1.$$

[7]

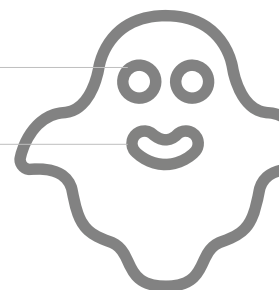


2. Show that the sum of the first n terms of the series

[7]

$$5^2 + 9^2 + 13^3 + 17^2 + \dots$$

is given by $\frac{1}{3}n(16n^2 + 36n + 23)$.



3.

$f(x) \equiv x^3 - 5x^2 + 2.$

- (a) Show that the equation $f(x) = 0$ has a root α in the interval $[0, 1]$. [2]
- (b) Use the Newton-Raphson method with initial value $x = 0.5$ to find a value for α which is correct to 2 decimal places. [5]
- (c) Give a reason why the Newton-Raphson method fails if an initial value of $x = 0$ is used in part (b). [2]

Total: 9



4. The complex number z is given by

$$z = \frac{1 + \mathbf{i}\sqrt{3}}{1 - \mathbf{i}\sqrt{3}}.$$

(a) Show that z can be expressed in the form $\lambda(1 - \mathbf{i}\sqrt{3})$ where λ is a rational number which you should find. [4]

(b) Find the modulus and argument of z . [3]

(c) Hence, or otherwise, find the modulus and argument of [4]

$$\left(\frac{1 + \mathbf{i}\sqrt{3}}{1 - \mathbf{i}\sqrt{3}} \right)^4.$$

Total: 11



5. (a) Find the values of p and q such that $y = p \sin(x) + q \cos(x)$ is a particular integral of the differential equation [7]

$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + 5y = \sin(x).$$

- (b) Find the general solution of this differential equation. [5]

Total: 12



[3]

where c is an arbitrary constant.

[5]

Given that $y = 0$ when $x = \frac{\pi}{4}$,

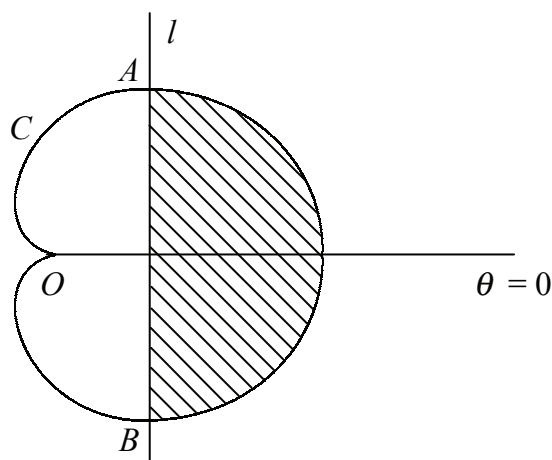
[4]

Total: 12



7. Figure shows the curve C with polar equation

$$r = 2(1 + \cos(\theta)), \quad -\pi < \theta \leq \pi,$$



and the line l with polar equation

$$r \cos(\theta) = \frac{3}{2},$$

referred to the pole O and initial line $\theta = 0$.

(a) Find the polar coordinates of the points A and B , where l intersects C . [6]

(b) Show that the area of triangle OAB is $\frac{9\sqrt{3}}{4}$. [3]

(c) Hence find the area of the shaded region bounded by C and l . [8]

Total: 17

