

# Solomon Practice Paper

## Pure Mathematics 4E

Time allowed: 90 minutes

Centre: [www.CasperYC.club](http://www.CasperYC.club)

Name:

Teacher:

Question	Points	Score
1	7	
2	7	
3	9	
4	10	
5	12	
6	13	
7	17	
Total:	75	

How I can achieve better:

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Last updated: July 14, 2025



1. The complex number  $w$  is given by  $w = \frac{10 + 5\mathbf{i}}{2 - \mathbf{i}}$ .

(a) Express  $w$  in the form  $a + \mathbf{i}b$  where  $a$  and  $b$  are real.

[3]

(b) Using your answer to part (a) find the complex number  $z$  such that

[4]

$$z + 2z^* = w.$$

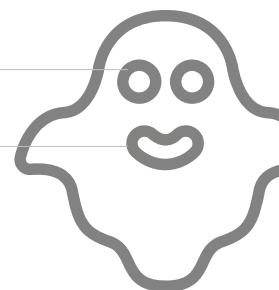
Total: 7



2. Show that

[7]

$$\sum_{r=0}^n (r+1)(r+2) = \frac{1}{3}(n+1)(n+2)(n+3).$$

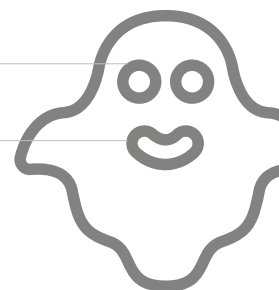


3. Find the equation of the curve which passes through the origin and for which

[9]

$$\frac{dy}{dx} = x + y,$$

giving your answer in the form  $y = f(x)$ .



4. The curve  $C$  has the polar equation

$$r = a(1 + \sin(\theta)), \quad 0 \leq \theta \leq \frac{\pi}{2}.$$

- (a) Sketch the curve  $C$ . [2]
- (b) Find the polar coordinates of the point on the curve where the tangent to the curve is perpendicular to the initial line  $\theta = 0$ . [8]

Total: 10



- $$y = \frac{ax - 1}{x + b},$$

(b) Sketch the curve [3]

$$y = \frac{ax - 1}{x + b},$$

(c) Hence, or otherwise, find the set of values of  $x$  for which

$$\left| \frac{3x - 1}{x + 2} \right| < 2.$$

Total: 12



6. (a) Show that the equation  $e^x - 4\sin(x) = 0$  has a root,  $\alpha$ , in the interval  $[0, 1]$  and a root,  $\beta$ , in the interval  $[1, 1.5]$ . [3]
- (b) Using the Newton-Raphson method with an initial value of  $x = 0.5$ , find  $\alpha$  correct to 2 decimal places. [5]
- (c) Use linear interpolation once between the values  $x = 1$  and  $x = 1.5$  to find an approximate value for  $\beta$ , giving your answer correct to 1 decimal place. [3]
- (d) Determine whether or not your answer to part (c) gives the value of  $\beta$  correct to 1 decimal place. [2]

Total: 13

