

Solomon Practice Paper

Pure Mathematics 4B

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	6	
2	8	
3	9	
4	9	
5	10	
6	15	
7	18	
Total:	75	

How I can achieve better:

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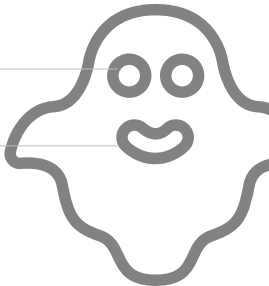
Last updated: July 14, 2025



1. Find the set of values of x for which

[6]

$$|2x^2 - 5x| < x.$$



2. (a) Sketch the curve C with the polar equation [3]

$$r^2 = a^2 \sin^2(2\theta), \quad 0 \leq \theta < 2\pi.$$

- (b) Find the exact area of the region enclosed by one loop of the curve C . [5]

Total: 8



3. (a) Show that

[6]

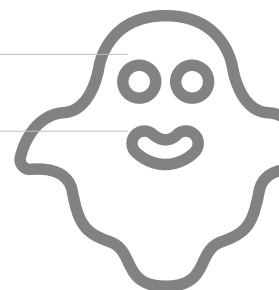
$$\sum_{r=1}^n (r^2 + 1)(r - 1) = \frac{1}{12}n(n - 1)(3n^2 + 5n + 8).$$

(b) Hence evaluate

[3]

$$\sum_{r=5}^{25} (r^2 + 1)(r - 1).$$

Total: 9



4. (a) Find the general solution of the differential equation

[6]

$$\frac{dy}{dx} - y \cot(x) = \sin(2x).$$

- (b) Given also that $y = 2$ when $x = \frac{\pi}{6}$, find the exact value of y when $x = \frac{2\pi}{3}$.

[3]

Total: 9

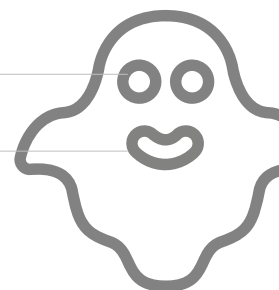


5.

$$f(x) \equiv x^3 - \ln(4 - x^2), \quad x \in \mathbb{R}, \quad -2 < x < 2.$$

- (a) Show that one root, α , of the equation $f(x) = 0$ lies in the interval $1.0 < \alpha < 1.1$. [2]
- (b) Starting with $x = 1.0$, show that using the Newton-Raphson method twice gives an approximation to α that is correct to 6 decimal places. [8]

Total: 10



6. The complex numbers z_1, z_2 and z_3 are given by

$$z_1 = 7 - \mathbf{i}, \quad z_2 = 1 + \mathbf{i}\sqrt{3}, \quad z_3 = a + \mathbf{i}b,$$

where a and b are rational constants.

Given that the modulus of $z_1 z_3$ is 50,

(a) find the modulus of z_3 . [3]

Given also that the argument of $\frac{z_2}{z_3}$ is $\frac{7\pi}{12}$,

(b) find the argument of z_3 . [3]

(c) Find the values of a and b . [2]

(d) Show that $\frac{z_1}{z_3} = \frac{1}{5}(4 + 3\mathbf{i})$. [3]

(e) Represent z_1, z_3 and $\frac{z_1}{z_3}$ on the same Argand diagram. [2]

(f) By considering the modulus and argument of z_1 and z_3 , explain why [2]

$$\frac{z_3}{z_1} = \left(\frac{z_1}{z_3} \right)^*.$$

Total: 15



- $$\frac{d^2y}{dx^2} = e^{-2t} \left(\frac{d^2y}{dt^2} - \frac{dy}{dt} \right).$$

- $$x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} - 3y = 6x^2$$

$$\frac{d^2y}{dt^2} - 2\frac{dy}{dt} - 3y = 6e^{2t}.$$

- $$x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} - 3y = 6x^2.$$

