

# Solomon Practice Paper

## Pure Mathematics 4A

Time allowed: 90 minutes

Centre: [www.CasperYC.club](http://www.CasperYC.club)

Name:

Teacher:

Question	Points	Score
1	6	
2	6	
3	6	
4	7	
5	9	
6	12	
7	14	
8	15	
Total:	75	

How I can achieve better:

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Last updated: July 14, 2025



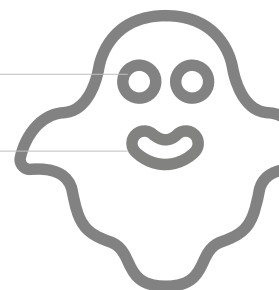
1.

$$f(z) \equiv z^3 - 5z^2 + 17z - 13.$$

(a) Show that  $(z - 1)$  is a factor of  $f(z)$ . [1]

(b) Hence find all the roots of the equation  $f(z) = 0$ , giving your answers in the form  $a + \mathbf{i}b$  [5]  
where  $a$  and  $b$  are integers.

Total: 6

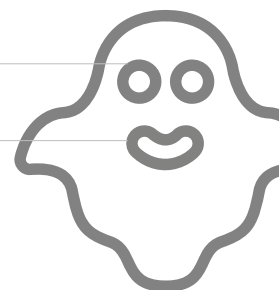


2. Find the general solution of the differential equation

[6]

$$x \frac{dy}{dx} + 3y = \frac{e^x}{x^2},$$

giving your answer in the form  $y = f(x)$ .



3. (a) Express  $\frac{1}{r(r+1)}$  in partial fractions.

[2]

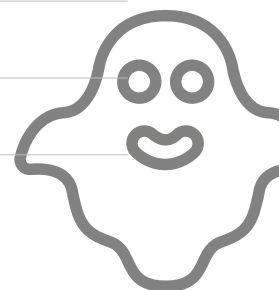
(b) Hence, or otherwise, find

[4]

$$\sum_{r=3}^{35} \frac{1}{r(r+1)},$$

giving your answer as a fraction in its lowest terms.

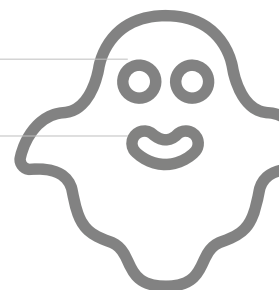
Total: 6



4. Find the set of values of  $x$  for which

[7]

$$\frac{(x+3)^2}{x+1} < 2.$$



5. (a) Sketch the curve with polar equation [3]

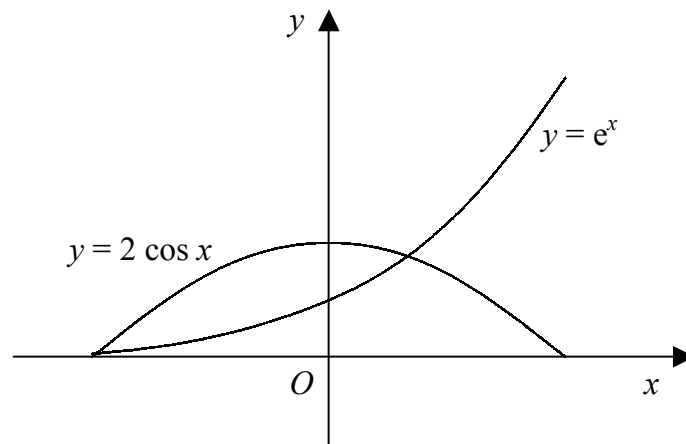
$$r = a \cos(3\theta), \quad a > 0, \quad \text{for } 0 \leq \theta \leq \pi.$$

(b) Show that the total area enclosed by the curve  $r = a \cos(3\theta)$  is  $\frac{\pi a^2}{4}$ . [6]

Total: 9



6. Figure shows the curves  $y = 2 \cos(x)$  and  $y = e^x$  in the interval  $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$ .



Given that  $f(x) \equiv e^x - 2 \cos(x)$ ,

- write down the number of solutions of the equation  $f(x) = 0$  in the interval  $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$ . [1]
- Show that the equation  $f(x) = 0$  has a solution,  $\alpha$ , in the interval  $[0, 1]$ . [2]
- Using 0.5 as a first approximation to  $\alpha$ , use the Newton-Raphson process once to find an improved estimate for  $\alpha$ , giving your answer correct to 2 decimal places. [4]
- Show that the estimate of  $\alpha$  obtained in part (c) is accurate to 2 decimal places. [2]

There is another root,  $\beta$ , of the equation  $f(x) = 0$  in the interval  $[-2, -1]$ .

- Use linear interpolation once on this interval to estimate the value of  $\beta$ , giving your answer correct to 2 decimal places. [3]

Total: 12



$$z = \frac{A}{1-i} \quad \text{and} \quad w = \frac{B}{2+i},$$

Given that  $z + w = 6$ ,

[6]

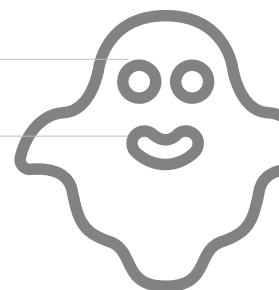
(b) Show  $P$  and  $Q$  on the same Argand diagram.

[5]

(c) Find the distance  $PQ$  in the form  $a\sqrt{5}$ .

[3]

Total: 14





[6]

satisfies the differential equation

(b) Hence find the solution of this differential equation for which  $x = 1$  and  $\frac{dx}{dt} = 12$  at  $t = 0$ . [9]

Total: 15

