

# Solomon Practice Paper

## Pure Mathematics 3L

Time allowed: 90 minutes

Centre: [www.CasperYC.club](http://www.CasperYC.club)

Name:

Teacher:

Question	Points	Score
1	5	
2	6	
3	7	
4	8	
5	9	
6	12	
7	13	
8	15	
Total:	75	

How I can achieve better:

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Last updated: July 14, 2025



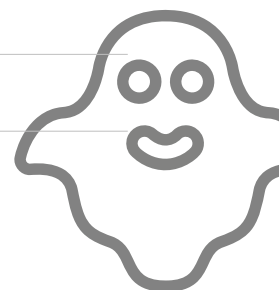
1. A circle has the equation

[5]

$$4x^2 + 4y^2 - 4x + 24y + 1 = 0.$$

Find

- the coordinates of the centre of the circle,
- the radius of the circle.

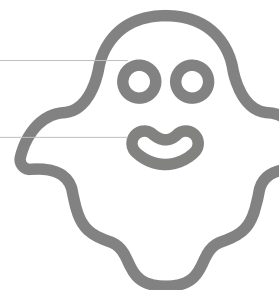


2. Find, in the form  $ax + by + c = 0$ , the equation of the normal to the curve

[6]

$$y = (x + 3)^2 e^{-x}$$

at the point with coordinates  $(0, 9)$ .



3.

$$f(x) \equiv x^3 + (a + 3)x^2 - a^3.$$

Given that when  $f(x)$  is divided by  $(x + 2)$  the remainder is 4,

(a) find the three possible values of  $a$ .

[4]

Given also that  $a > 0$ ,

(b) find the remainder when  $f(x)$  is divided by  $(2x + 3)$ .

[3]

Total: 7



4. Relative to a fixed origin,  $O$ , the points  $A, B$  and  $C$  have position vectors  $(5\mathbf{i} + \mathbf{j} - 11\mathbf{k})$ ,  $(-3\mathbf{i} + 5\mathbf{j} - 3\mathbf{k})$  and  $(11\mathbf{i} + \mathbf{j} + 4\mathbf{k})$  respectively.

(a) Find an equation of the line that passes through  $A$  and  $B$  in the form  $\mathbf{r} = \mathbf{a} + \lambda\mathbf{b}$ . [3]

The point  $M$  is the midpoint of  $AB$ .

(b) Show that  $\overrightarrow{CM}$  is perpendicular to  $\overrightarrow{AB}$ . [5]

Total: 8

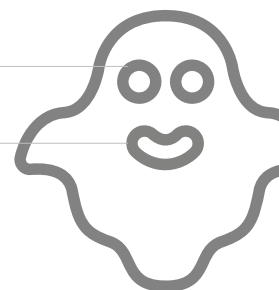


5.

$$f(x) \equiv (1 + 8x)^{\frac{1}{2}}, |x| < \frac{1}{8}.$$

- (a) Express  $f(x)$  as a series in ascending powers of  $x$  up to and including the term in  $x^3$ . [3]
- (b) Show that  $\sqrt{1.08} = \frac{3}{5}\sqrt{3}$ . [2]
- (c) Hence, use your series with a suitable value of  $x$  to estimate the value of  $\sqrt{3}$  correct to 6 significant figures. [4]

Total: 9



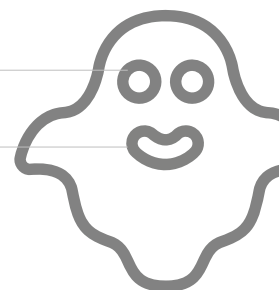
[3]

find the values of  $A$  and  $B$ .

[4]

[5]

Total: 12



7.

$$f: x \mapsto \cos(2x) + \sin(x), \quad 0 \leq x \leq 2\pi.$$

- (a) Find the values of  $x$  for which  $f(x) = 0$ . [4]
- (b) Find the values of  $x$  for which  $f'(x) = 0$ . [6]
- (c) Sketch the curve  $y = f(x)$ . [3]

Total: 13

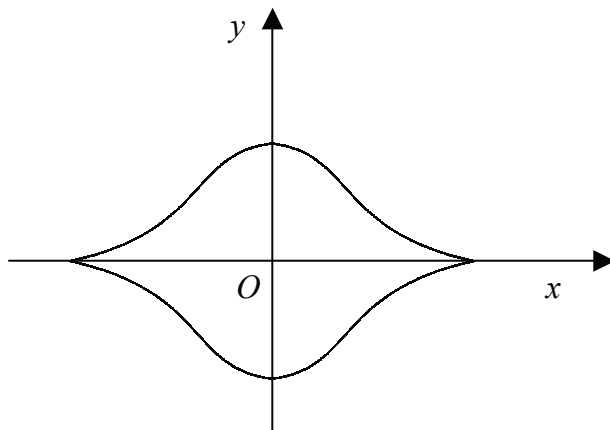




8. Figure shows the curve given by the parametric equations

$$x = 2 \cos(t), \quad \text{and} \quad y = \sin^3(t), \quad 0 \leq t \leq 2\pi.$$

where  $t$  is a parameter.



(a) Find the coordinates of the points  $A$  and  $B$  with parameters  $t = 0$  and  $t = \frac{\pi}{2}$  respectively. [2]

(b) Show that the area of the region enclosed by the curve is given by the integral [5]

$$\int_0^{\frac{\pi}{2}} 8 \sin^4(t) \, dt.$$

(c) Use the double angle identities to prove that [4]

$$\sin^4(A) = \frac{1}{8} (3 - 4 \cos(2A) + \cos(4A)).$$

(d) Find the area of the region enclosed by the curve, giving your answer in terms of  $\pi$ . [4]

Total: 15

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