

Solomon Practice Paper

Pure Mathematics 3G

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	5	
2	8	
3	8	
4	9	
5	10	
6	10	
7	12	
8	13	
Total:	75	

How I can achieve better:

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1. Given that

[5]

$$y = 2e^x(x - 1),$$

show that

$$\frac{dy}{dx} = \frac{xy}{x-1}.$$



2. (a) Find

[3]

$$\int \frac{x}{x^2 + 3} dx.$$

(b) Given that $y = 1$ when $x = 1$, solve the differential equation

[5]

$$(x^2 + 3) \frac{dy}{dx} = xy,$$

giving your answer in the form $y^2 = f(x)$.

Total: 8



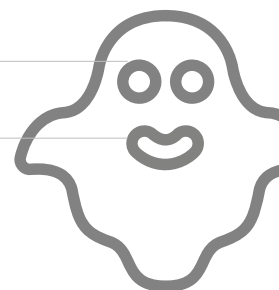
3.

[8]

$$f(x) \equiv x^3 - x^2 - 8x + 14.$$

When $f(x)$ is divided by $(x - a)$ the remainder is 2.

By forming and factorising a cubic equation, find all possible values of a .



$$\cos(2x) \tan(y) = 1.$$

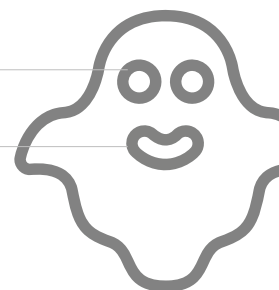
[4]

$$\frac{dy}{dx} = \tan(2x) \sin(2y).$$

(b) By evaluating $\frac{d^2y}{dx^2}$ at this stationary point, determine its nature.

[5]

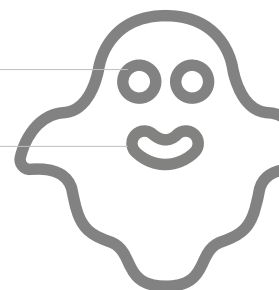
Total: 9



- $$\frac{1-3x}{(x^2+1)(x+1)} \equiv \frac{Ax+B}{x^2+1} + \frac{C}{x+1}.$$

- $$\frac{1-3x}{(x^2+1)(x+1)}$$

Total: 10



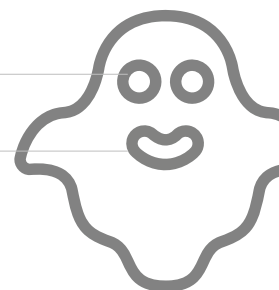
$$x^2 + y^2 + 2x - 8y + 15 = 0.$$

- P is the point with coordinates $(6, 3)$.

- T is a point on C such that the line PT is a tangent to C .

- (c) Find the length of the line PT in the form $k\sqrt{3}$. [3]

Total: 10



$$\begin{aligned} l &: \mathbf{r} = 12\mathbf{i} - 9\mathbf{j} + 8\mathbf{k} + \lambda(14\mathbf{i} - 5\mathbf{j} + 2\mathbf{k}), \\ m &: \mathbf{r} = 4\mathbf{i} + 8\mathbf{j} - 6\mathbf{k} + \mu(a\mathbf{i} + b\mathbf{j} - 4\mathbf{k}), \end{aligned}$$

Given that l and m are perpendicular,

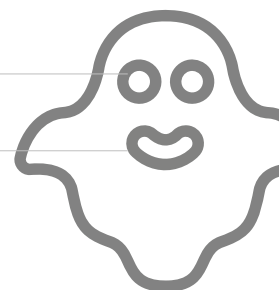
[2]

(b) show that $a = 2$ and find the value of b ,

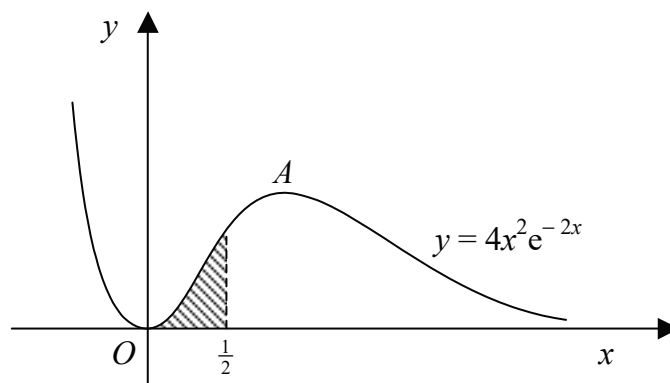
[5]

[5]

Total: 12



8. Figure shows the curve with equation $y = 4x^2e^{-2x}$.



The curve is stationary at the origin, O , and at the point A .

(a) Find the coordinates of point A .

[4]

The shaded region is bounded by the curve, the x -axis, and the line $x = \frac{1}{2}$.

(b) Show that the area of the shaded region is $\left(1 - \frac{5}{2}e^{-1}\right)$.

[9]

Total: 13

