

Solomon Practice Paper

Pure Mathematics 3D

Time allowed: 90 minutes

Centre: www.CasperYC.club

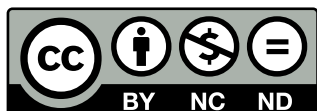
Name:

Teacher:

Question	Points	Score
1	5	
2	7	
3	8	
4	8	
5	10	
6	10	
7	13	
8	16	
Total:	77	

How I can achieve better:

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Last updated: July 14, 2025

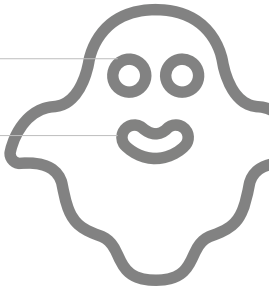


1. A curve is given by the parametric equations

$$x = 1 + t^2, \quad \text{and} \quad y = 2t^6.$$

- (a) Find an equation of the curve in Cartesian form. [2]
- (b) Sketch the curve, labelling the coordinates of any points where the curve meets the coordinate axes. [3]

Total: 5



2. The lines l_1 and l_2 are given by

$$\begin{aligned} l_1 &: \mathbf{r} = -38 + 8\mathbf{k} + \lambda(5\mathbf{i} - 7\mathbf{j} + 4\mathbf{k}) \\ l_2 &: \frac{x-5}{2} = \frac{y+9}{3} + \frac{z-3}{6}. \end{aligned},$$

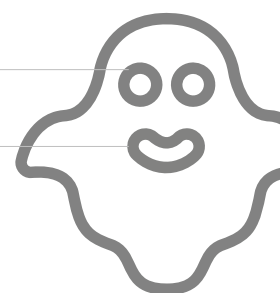
(a) Find an equation for l_2 in vector form.

[3]

(b) Find the size of the acute angle between lines l_1 and l_2 in degrees correct to 1 decimal place.

[4]

Total: 7



3. (a) Use integration by parts to find

[4]

$$\int 2x \ln(x) \, dx.$$

(b) Given that $y = 2e$ when $x = e$, solve the differential equation

[4]

$$\frac{dy}{dx} = \frac{2x \ln(x)}{y}.$$

Total: 8

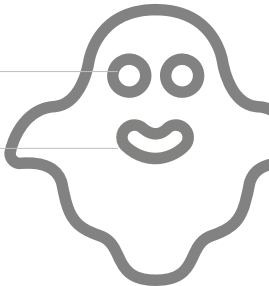


4. A curve has the equation

$$4 \cos(x) + \tan(y) = 0.$$

- (a) Show that $\frac{dy}{dx} = 4 \sin(x) \cos^2(y)$. [3]
- (b) Find the equation of the normal to the curve at the point with coordinates $(\frac{\pi}{2}, \frac{\pi}{6})$ in the form $ax + by + c = 0$. [5]

Total: 8



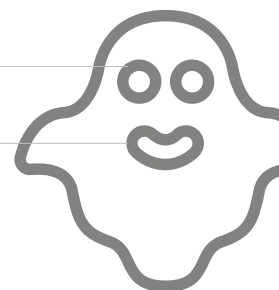
5. (a) Given that $|x| < 1$, express $(1+x)^{-1}$ as a series in ascending powers of x , as far as the term in x^3 . [3]

(b) [7]

$$f(x) \equiv \frac{4x+1}{(1-2x)(1+x)}.$$

By expressing $f(x)$ in partial fractions, find the series expansion of $f(x)$ in ascending powers of x as far as the term in x^3 and state the set of values of x for which your series is valid.

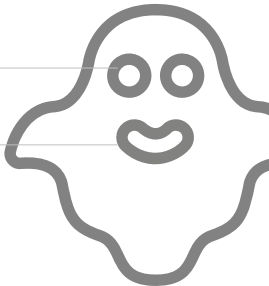
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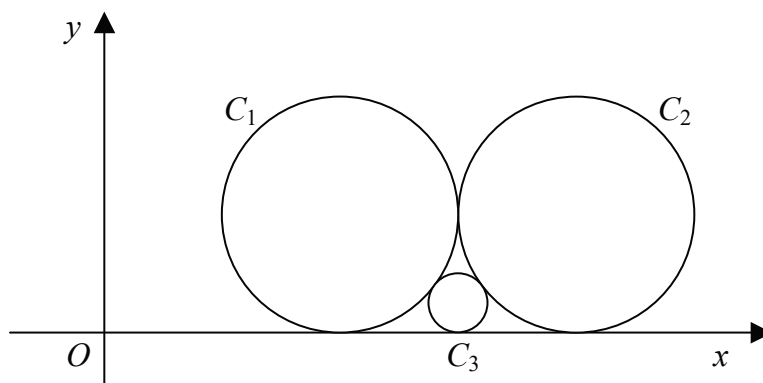
6. (a) Find $\int \tan^2(3x) \, dx$. [3]
- (b) Using the substitution $u = x^2 + 4$, or otherwise, evaluate [7]

$$\int_0^2 \frac{5x}{(x^2 + 4)^2} \, dx.$$

Total: 10



7. Figure shows three circles, C_1 , C_2 and C_3 which all touch the x -axis.



Circle C_1 has the equation $x^2 + y^2 - 12x - 8y + 36 = 0$.

(a) Find the coordinates of the centre of C_1 and write down its radius. [5]

Circle C_2 has the same radius as C_1 and is touching circle C_1 .

(b) Find an equation of circle C_2 . [3]

Circle C_3 is touching both circles C_1 and C_2 .

(c) Find an equation of circle C_3 . [5]

Total: 13



8. (a) A curve has the equation

[5]

$$y = \frac{x}{\sqrt{x-2}}, \quad x > 2.$$

Show that

$$\frac{dy}{dx} = \frac{x-4}{2(x-2)^{\frac{3}{2}}}$$

- (b) Find the coordinates of the stationary point on the curve.

[3]

- (c) Find and simplify an expression for $\frac{d^2y}{dx^2}$.

[5]

- (d) Hence, determine the nature of the stationary point on the curve.

[3]

Total: 16

