

Solomon Practice Paper

Pure Mathematics 3B

Time allowed: 90 minutes

Centre: www.CasperYC.club

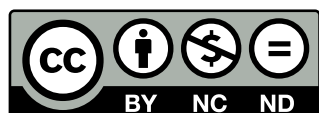
Name:

Teacher:

Question	Points	Score
1	5	
2	7	
3	9	
4	9	
5	10	
6	10	
7	12	
8	13	
Total:	75	

How I can achieve better:

-
-
-



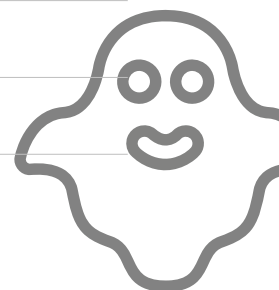
Last updated: July 14, 2025



[5]

$$\frac{3x^2 + 5x + 13}{(x^2 + 2)(x - 3)} \equiv \frac{Ax + B}{x^2 + 2} + \frac{C}{x - 3}$$

find the values of the constants A, B and C .



2. (a) Find $\int 6xe^{3x} \, dx$. [4]
- (b) Find the general solution of the differential equation [3]

$$\frac{dy}{dx} = 6xe^{3x+y}.$$

Total: 7



3. Air is pumped into a balloon such that its volume increases at the rate of 75 cm^3 per second. It is assumed that the balloon is spherical at all times.
- (a) Find, in terms of π , the rate at which the radius of the balloon is increasing when the radius is 5 cm. [4]
- (b) Given that the balloon was initially empty, show that one minute after the pumping begins the radius is increasing at the rate of $\frac{1}{12}\pi^{-\frac{1}{3}} \text{ cm}$ per second. [5]

Total: 9



4. (a) Given that $|x| < 1$, express $(1 + x)^{-\frac{1}{2}}$ as a series in ascending powers of x , as far as the term in x^3 . You should simplify the coefficients in your series. [4]

(b) Hence, express [5]

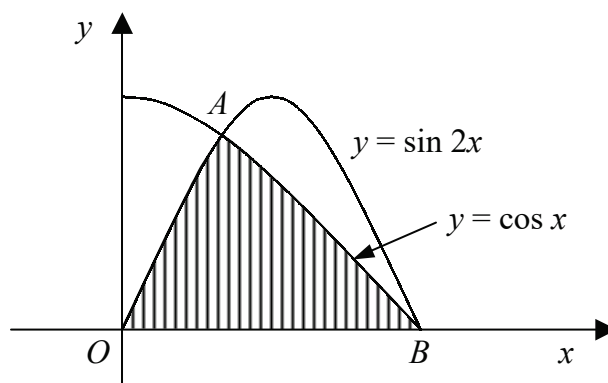
$$\frac{8x}{\sqrt{4-x}}$$

as a series in ascending powers of x , as far as the term in x^3 , and state the set of values of x for which your series is valid.

Total: 9



5. Figure shows part of the curves $y = \cos(x)$ and $y = \sin(2x)$ for $x > 0$.



The curves intersect at the points A and B .

- (a) Find the coordinates of A and B . [5]
- (b) Show that the area of the shaded region bounded by the two curves and the x -axis is $\frac{3}{4}$. [5]

Total: 10



6. (a) Write down in cartesian form the equation of a circle with centre $(-4, 3)$ and a radius of 5. [2]
- (b) Find, in the form $ax + by + c = 0$, the equation of the normal to the circle at the point $(-1, 7)$. [8]

Total: 10



7. The line l_1 passes through the points with position vectors $(6\mathbf{i} + \mathbf{j} + \mathbf{k})$ and $(12\mathbf{i} + \mathbf{j} - 11\mathbf{k})$ relative to a fixed origin, O .

(a) Find an equation of the line l_1 in vector form.

[3]

The line l_2 has the equation

$$\mathbf{r} = 4\mathbf{i} - 3\mathbf{j} + 7\mathbf{k} + \mu(2\mathbf{i} + 2\mathbf{j} - 5\mathbf{k}).$$

- (b) Show that the lines l_1 and l_2 intersect and find the position vector of their point of intersection, P .

[5]

The line l_3 is perpendicular to l_1 and intersects lines l_1 and l_2 at Q and R respectively.

- (c) Find in degrees, correct to 1 decimal place, the size of angle PRQ .

[4]

Total: 12



$$x = \frac{3}{t}, \quad \text{and} \quad y = 2t^2, \quad t \neq 0.$$

The point A on C has parameter $t = 1$.

$$4x + 3y - 18 = 0.$$

(c) Find the coordinates of B . [6]

Total: 13

