

Solomon Practice Paper

Pure Mathematics 2J

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	4	
2	8	
3	8	
4	10	
5	11	
6	11	
7	11	
8	12	
Total:	75	

How I can achieve better:

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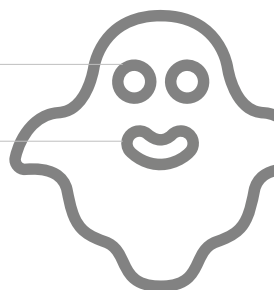


Last updated: July 14, 2025



1. Given that $y = 3e^x + 2\ln(x)$, find $\frac{d^2y}{dx^2}$.

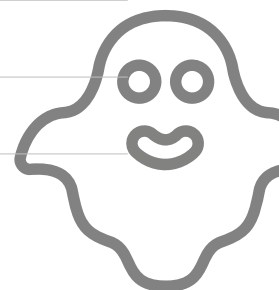
[4]



[4]

[4]

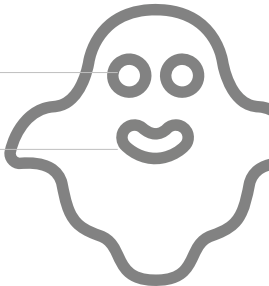
$$\ln(48) + \ln(108) = A \ln(2) + B \ln(3).$$



3. (a) Express $\left(x^{\frac{1}{2}} - 2x^{-\frac{3}{2}}\right)^2$ in the form $px + qx^{-1} + rx^{-3}$. [3]
- (b) Show that [5]

$$\int_2^4 \left(x^{\frac{1}{2}} - 2x^{-\frac{3}{2}}\right)^2 \, dx = \frac{51}{8} - 4 \ln(2).$$

Total: 8



4. (a) Find the values of θ in the interval $0 \leq \theta \leq 2\pi$, for which

[5]

$$2 \tan^2(\theta) + \sec^2(\theta) = 2,$$

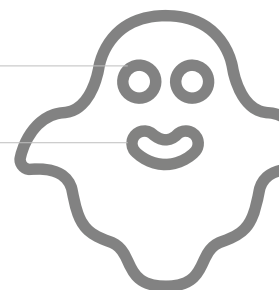
giving your answers in terms of π .

- (b) Find the values of x in the interval $0 \leq x \leq 180^\circ$, for which

[5]

$$\sin(3x) = \sin(2x).$$

Total: 10



5. Given that $a > 0$,

(a) sketch on the same set of coordinate axes the graphs of $y = \frac{1}{2}(x + a)$ and $y = |2x - a|$, [5]
labelling the coordinates of any points where each graph meets the coordinate axes,

(b) find, in terms of a , the coordinates of any points where the two graphs intersect. [6]

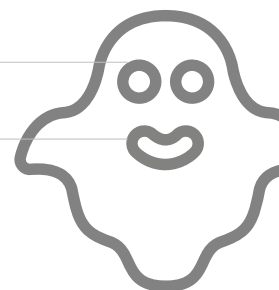
Total: 11



- Hence, find

- (c) the coefficient of z^6 in the expansion of $(2 + \sqrt{2}z)^5(2 - \sqrt{2}z)^5$. [4]

Total: 11



7.

$$f(x) \equiv x^4 - 5x + 3.$$

(a) Show that one root of the equation $f(x) = 0$ lies in the interval $(0.6, 0.7)$. [2]

(b) Using the iteration formula [3]

$$x_{n+1} = 0.2(x_n^4 + 3),$$

with a starting value of $x_1 = 0.65$, find this root correct to 3 significant figures.

(c) Show that the equation $f(x) = 0$ can be rewritten as [2]

$$x = \pm \sqrt{\frac{ax + b}{x^2}}$$

where a and b are integers to be found.

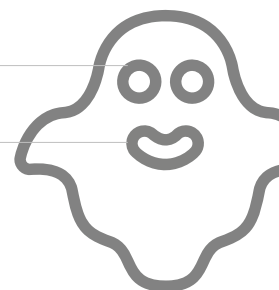
(d) Hence, use the iteration formula [2]

$$x_{n+1} = \pm \sqrt{\frac{a_n x + b}{x_n^2}},$$

together with your values of a and b and with $x_1 = 1.5$ to find x_2, x_3 and x_4 correct to 6 significant figures.

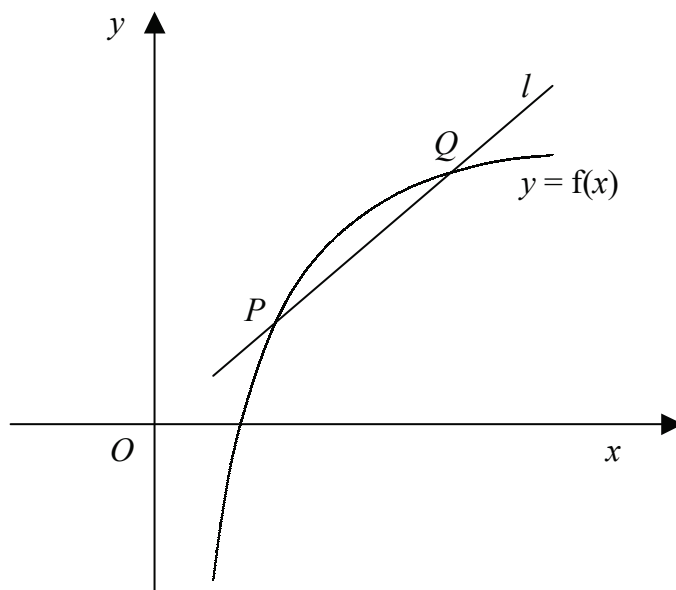
(e) Considering only your values of x_2, x_3 and x_4 , explain why it is reasonable to give a second root of the equation as 1.43 correct to 3 significant figures. [2]

Total: 11





8. Figure shows the straight line l and the curve $y = f(x)$.



The line and curve intersect at the points $P(1, \ln(2))$ and $Q(3, \ln(8))$.

- (a) Find in its simplest form the equation of the line l .

[4]

Given that $f(x) \equiv \ln(ax + b)$,

- (b) find the values of a and b ,

[5]

- (c) hence, find an expression for $f^{-1}(x)$.

[3]

Total: 12

