Solomon Practice Paper

Pure Mathematics 1D

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	5	
2	8	
3	8	
4	8	
5	8	
6	11	
7	13	
8	14	
Total:	75	

How I can achieve better:

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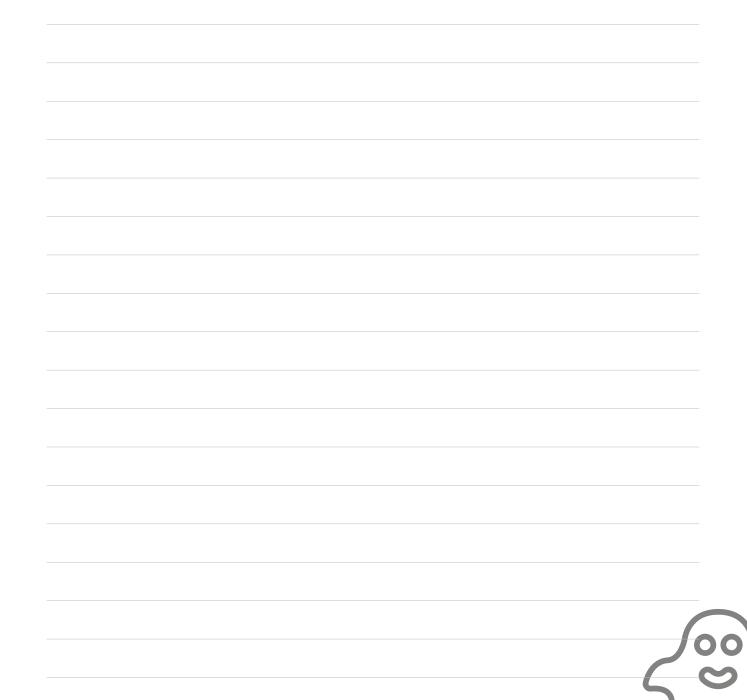
1. (a) State the condition for which the equation $ax^2 + bx + c = 0$ will have real roots. [1]

Given that $f(x) \equiv x^2 + 2px + 3x + p^2$,

(b) prove that the equation f(x) = 0 will have real roots only if $p \ge -\frac{3}{4}$.

[4]

Total: 5

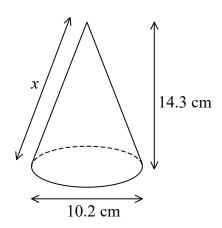


[3]

[5]

Total: 8

2. Figure shows a solid right-circular cone.



The height of the cone is 14.3 cm and the diameter of its base is 10.2 cm.

- (a) Calculate the slant height of the cone, x, in centimetres correct to 1 decimal place.
- (b) Show that the surface area of the cone is 325 cm², correct to 3 significant figures.



3.

$$f(x) \equiv 3x^3 - 7x^2 - 22x + 8.$$

- (a) Evaluate f(-2). [2]
- (b) Hence state one linear factor of f(x). [1]
- (c) Express f(x) as the product of three linear factors.

Total: 8

[5]



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4.	(a) Find		
		$\int 6x^2 - 20x + \frac{1}{\sqrt{x}} \mathrm{d}x.$	

[4]

[4]

(b) Hence, evaluate

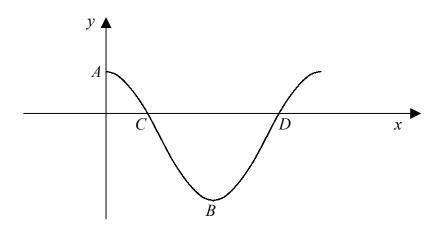
$$\int_{4}^{5} 6x^2 - 20x + \frac{1}{\sqrt{x}} \, \mathrm{d}x.$$

giving your answer in the form $a + b\sqrt{5}$.

Total: 8



5. Figure shows the curve with equation $y = 4\cos(x) - 1$, for x in the interval $0 \le x \le 2\pi$.



- (a) State the coordinates of the point A, where the curve crosses the y-axis, and the point B, the first minimum on the curve for x > 0.
- (b) Find the coordinates of the points C and D, where the curve crosses the x-axis in the interval $0 \le x \le 2\pi$.



Total: 8

6. The first term of a geometric series is $8\sqrt{3}$ and the second term is 12.	
(a) Show that the common ratio of the series is $\frac{\sqrt{3}}{2}$.	[
(b) Find the sixth term of the series.	[
(c) Show that the sum to infinity of the series can be written as $16(2\sqrt{3}+3)$.	[
	Total:

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7.

$$f(x) \equiv (x-1)(x-a).$$

(a) Sketch the curve y = f(x), indicating the coordinates of any points where the curve crosses the coordinate axes in the cases for which

[5]

i.
$$a > 1$$
,

ii. a < 0.

(b) Show that the coordinates of the turning point of the curve y = f(x) can be written as:

[7]

$$\left(\frac{a+1}{2}, \frac{-(a-1)^2}{4}\right).$$

(c) Hence state the set of values for which f(x) is increasing.

Total: 13

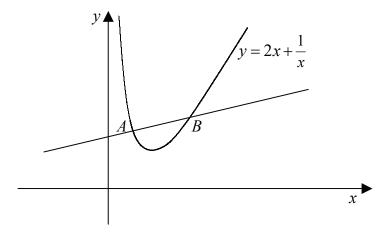
[1]

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8. Figure shows the curve $y = 2x + \frac{1}{x}$ and the normal to the curve at the point $A\left(\frac{1}{2},k\right)$.



(a) Find the value of k.

[2]

[6]

(b) Show that the equation of the normal to the curve at A can be written as

$$2x - 4y + 11 = 0.$$

The normal to the curve at A cuts the curve again at the point B.

(c) Find the coordinates of the point B, giving your answers as exact fractions.

Total: 14

[6]

