

Solomon Practice Paper

Pure Mathematics 4C

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

| Question | Points | Score |
|----------|--------|-------|
| 1 | 6 | |
| 2 | 9 | |
| 3 | 9 | |
| 4 | 10 | |
| 5 | 12 | |
| 6 | 13 | |
| 7 | 16 | |
| Total: | 75 | |

How I can achieve better:

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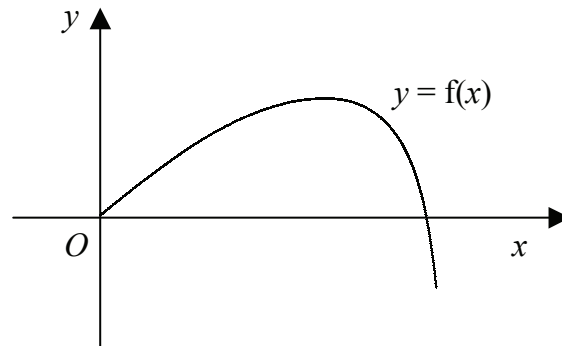


Last updated: *May 5, 2023*



5. Figure shows part of the curve $y = f(x)$ where

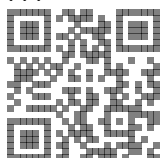
$$f(x) \equiv 2x - \tan(x), \quad x \in \mathbb{R}, \quad 0 \leq x < \frac{\pi}{2}.$$



- (a) Show that there is a root, α , of the equation $f(x) = 0$ in the interval $(1, 1.5)$. [2]
- (b) Use the Newton-Raphson method with an initial value of $x = 1.25$ to find α correct to 2 decimal places and justify the accuracy of your answer. [7]
- (c) Explain with the aid of a diagram why the Newton-Raphson method fails if an initial value of $x = 0.75$ is used when trying to find α . [3]

Total: 12

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6. The complex numbers z and w are defined such that

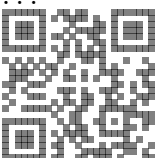
$$\begin{aligned} 3z + w &= 14 \\ z - \mathbf{i}w &= 15 - 9\mathbf{i} \end{aligned}$$

(a) Show that $z = 3 - 4\mathbf{i}$ and find w in the form $a + \mathbf{i}b$, where a and b are real numbers. [6]

(b) Find the square roots of z in the form $c + \mathbf{i}d$, where c and d are real numbers. [7]

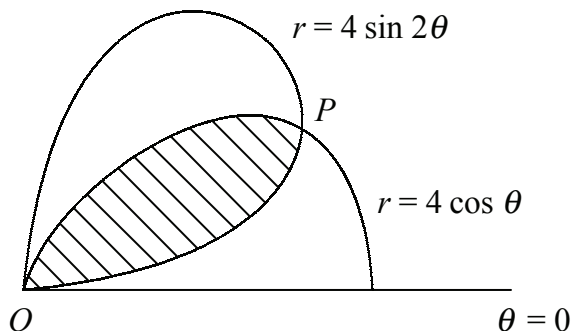
Total: 13

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7. Figure shows the curves with polar equations

$$r = 4 \sin(2\theta), \quad 0 \leq \theta \leq \frac{\pi}{2}$$
$$r = 4 \cos(\theta), \quad 0 \leq \theta \leq \frac{\pi}{2}$$



(a) Find the polar coordinates of the point *P* where the two curves intersect. [5]

(b) Find the exact area of the shaded region bounded by the two curves. [11]

Total: 16

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