

Solomon Practice Paper

Pure Mathematics 4A

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

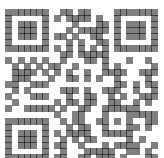
Question	Points	Score
1	6	
2	6	
3	6	
4	7	
5	9	
6	12	
7	14	
8	15	
Total:	75	

How I can achieve better:

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Last updated: May 5, 2023



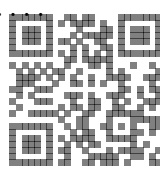
5. (a) Sketch the curve with polar equation [3]

$$r = a \cos(3\theta), \quad a > 0, \quad \text{for } 0 \leq \theta \leq \pi.$$

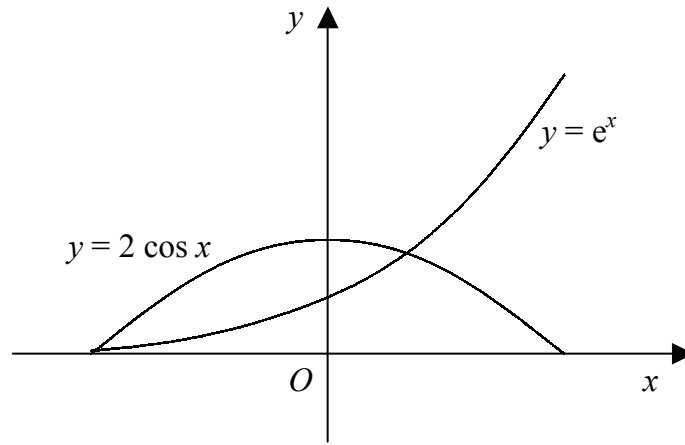
(b) Show that the total area enclosed by the curve $r = a \cos(3\theta)$ is $\frac{\pi a^2}{4}$. [6]

Total: 9

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6. Figure shows the curves $y = 2 \cos(x)$ and $y = e^x$ in the interval $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$.



Given that $f(x) \equiv e^x - 2 \cos(x)$,

- (a) write down the number of solutions of the equation $f(x) = 0$ in the interval $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$. [1]
- (b) Show that the equation $f(x) = 0$ has a solution, α , in the interval $[0, 1]$. [2]
- (c) Using 0.5 as a first approximation to α , use the Newton-Raphson process once to find an improved estimate for α , giving your answer correct to 2 decimal places. [4]
- (d) Show that the estimate of α obtained in part (c) is accurate to 2 decimal places. [2]

There is another root, β , of the equation $f(x) = 0$ in the interval $[-2, -1]$.

- (e) Use linear interpolation once on this interval to estimate the value of β , giving your answer correct to 2 decimal places. [3]

Total: 12

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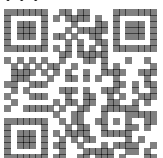
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8. (a) Find the values of p and q such that

[6]

$$x = p \cos(t) + q \sin(t)$$

satisfies the differential equation

$$\frac{d^2x}{dt^2} + 4\frac{dx}{dt} + 3x = \sin(t).$$

(b) Hence find the solution of this differential equation for which $x = 1$ and $\frac{dx}{dt} = 12$ at $t = 0$.

[9]

Total: 15

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