Edexcel (U.K.) Pre 2017

Questions By Topic

C3 Chap08 Differentiation

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5. Sketch the graph of $y = \ln|x|$, stating the coordinates of any points of intersection with the axes.

(3)

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3. The point P lies on the curve with equation $y = \ln\left(\frac{1}{3}x\right)$. The x-coordinate of P is 3.

Find an equation of the normal to the curve at the point P in the form $y = ax + b$, where a and b are constants.

(5)

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blank

1. Differentiate with respect to x

(a) $\ln\left(x^2 + 3x + 5\right)$

(2)

(b) $\dfrac{\cos x}{x^2}$

(3)

Leave blank

1. The point P lies on the curve with equation

$$y = 4e^{2x+1}.$$

The y-coordinate of P is 8.

(a) Find, in terms of ln 2, the x-coordinate of P.

(2)

(b) Find the equation of the tangent to the curve at the point P in the form $y = ax + b$, where a and b are exact constants to be found.

(4)

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4. Find the equation of the tangent to the curve $x = \cos(2y + \pi)$ at $\left(0, \dfrac{\pi}{4}\right)$.

Give your answer in the form $y = ax + b$, where a and b are constants to be found.

(6)

Leave blank

2. Differentiate, with respect to x,

(a) $e^{3x} + \ln 2x,$

(3)

(b) $(5 + x^2)^{\frac{3}{2}}.$

(3)

Q2

(Total 6 marks)

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2. A curve C has equation

$$y = \frac{3}{(5-3x)^2}, \quad x \neq \frac{5}{3}$$

The point P on C has x-coordinate 2. Find an equation of the normal to C at P in the form $ax + by + c = 0$, where a, b and c are integers.

(7)

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4. The point P is the point on the curve $x = 2\tan\left(y + \dfrac{\pi}{12}\right)$ with y-coordinate $\dfrac{\pi}{4}$.

Find an equation of the normal to the curve at P.

(7)

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1. The curve C has equation

$$y = (2x - 3)^5$$

The point P lies on C and has coordinates $(w, -32)$.

Find

(a) the value of w,

(2)

(b) the equation of the tangent to C at the point P in the form $y = mx + c$, where m and c are constants.

(5)

Leave
blank

7. The curve C has equation

$$y = \frac{3 + \sin 2x}{2 + \cos 2x}$$

(a) Show that

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{6\sin 2x + 4\cos 2x + 2}{\left(2 + \cos 2x\right)^2}$$

(4)

(b) Find an equation of the tangent to C at the point on C where $x = \dfrac{\pi}{2}$.

Write your answer in the form $y = ax + b$, where a and b are exact constants.

(4)

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2. A curve C has equation

$$y = e^{2x} \tan x, \quad x \neq (2n+1)\frac{\pi}{2}.$$

(a) Show that the turning points on C occur where $\tan x = -1$.

(6)

(b) Find an equation of the tangent to C at the point where $x = 0$.

(2)

Leave blank

8. (a) Given that

$$\frac{\mathrm{d}}{\mathrm{d}x}(\cos x) = -\sin x$$

show that $\dfrac{\mathrm{d}}{\mathrm{d}x}(\sec x) = \sec x \tan x$.

(3)

Given that

$$x = \sec 2y$$

(b) find $\dfrac{\mathrm{d}x}{\mathrm{d}y}$ in terms of y.

(2)

(c) Hence find $\dfrac{\mathrm{d}y}{\mathrm{d}x}$ in terms of x.

(4)

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3. The curve C has equation

$$x = 2 \sin y.$$

(a) Show that the point $P\left(\sqrt{2}, \dfrac{\pi}{4}\right)$ lies on C.

(1)

(b) Show that $\dfrac{dy}{dx} = \dfrac{1}{\sqrt{2}}$ at P.

(4)

(c) Find an equation of the normal to C at P. Give your answer in the form $y = mx + c$, where m and c are exact constants.

(4)

4.
$$f(x) = 3e^x - \tfrac{1}{2}\ln x - 2, \quad x > 0.$$

(a) Differentiate to find $f'(x)$.

(3)

The curve with equation $y = f(x)$ has a turning point at P. The x-coordinate of P is α.

(b) Show that $\alpha = \tfrac{1}{6}e^{-\alpha}$.

(2)

The iterative formula

$$x_{n+1} = \tfrac{1}{6}e^{-x_n}, \quad x_0 = 1,$$

is used to find an approximate value for α.

(c) Calculate the values of x_1, x_2, x_3 and x_4, giving your answers to 4 decimal places.

(2)

(d) By considering the change of sign of $f'(x)$ in a suitable interval, prove that $\alpha = 0.1443$ correct to 4 decimal places.

(2)

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3.

Figure 1

Figure 1 shows a sketch of the curve C which has equation

$$y = e^{x\sqrt{3}} \sin 3x \ , \quad -\frac{\pi}{3} \leqslant x \leqslant \frac{\pi}{3}$$

(a) Find the x coordinate of the turning point P on C, for which $x > 0$
  Give your answer as a multiple of π.

(6)

(b) Find an equation of the normal to C at the point where $x = 0$

(3)

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1. Differentiate with respect to x, giving your answer in its simplest form,

(a) $x^2 \ln(3x)$

(4)

(b) $\dfrac{\sin 4x}{x^3}$

(5)

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5. Given that

$$x = \sec^2 3y, \qquad 0 < y < \frac{\pi}{6}$$

(a) find $\dfrac{dx}{dy}$ in terms of y.

(2)

(b) Hence show that

$$\frac{dy}{dx} = \frac{1}{6x(x-1)^{\frac{1}{2}}}$$

(4)

(c) Find an expression for $\dfrac{d^2y}{dx^2}$ in terms of x. Give your answer in its simplest form.

(4)

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3. A curve C has equation

$$y = x^2 e^x.$$

(a) Find $\dfrac{dy}{dx}$, using the product rule for differentiation.

(3)

(b) Hence find the coordinates of the turning points of C.

(3)

(c) Find $\dfrac{d^2 y}{dx^2}$.

(2)

(d) Determine the nature of each turning point of the curve C.

(2)

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1. (a) Find the value of $\dfrac{\mathrm{d}y}{\mathrm{d}x}$ at the point where $x = 2$ on the curve with equation

$$y = x^2 \sqrt{(5x - 1)}.$$

(6)

(b) Differentiate $\dfrac{\sin 2x}{x^2}$ with respect to x.

(4)

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5. (i) Differentiate with respect to x

    (a) $y = x^3 \ln 2x$

    (b) $y = (x + \sin 2x)^3$

(6)

Given that $x = \cot y$,

(ii) show that $\dfrac{\mathrm{d}y}{\mathrm{d}x} = \dfrac{-1}{1 + x^2}$

(5)

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7. (a) Differentiate with respect to x,

(i) $x^{\frac{1}{2}} \ln(3x)$

(ii) $\dfrac{1-10x}{(2x-1)^5}$, giving your answer in its simplest form.

(6)

(b) Given that $x = 3\tan 2y$ find $\dfrac{\mathrm{d}y}{\mathrm{d}x}$ in terms of x.

(5)

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4. (i) The curve C has equation

$$y = \frac{x}{9 + x^2}.$$

Use calculus to find the coordinates of the turning points of C.

(6)

(ii) Given that

$$y = (1 + e^{2x})^{\frac{3}{2}},$$

find the value of $\dfrac{\mathrm{d}y}{\mathrm{d}x}$ at $x = \dfrac{1}{2}\ln 3$.

(5)

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8. (a) Express $2\cos 3x - 3\sin 3x$ in the form $R\cos(3x+\alpha)$, where R and α are constants, $R > 0$ and $0 < \alpha < \dfrac{\pi}{2}$. Give your answers to 3 significant figures.

(4)

$$\mathrm{f}(x) = \mathrm{e}^{2x}\cos 3x$$

(b) Show that $\mathrm{f}'(x)$ can be written in the form

$$\mathrm{f}'(x) = R\,\mathrm{e}^{2x}\cos(3x+\alpha)$$

where R and α are the constants found in part (a).

(5)

(c) Hence, or otherwise, find the smallest positive value of x for which the curve with equation $y = \mathrm{f}(x)$ has a turning point.

(3)

5.

Figure 1

Figure 1 shows a sketch of the curve C with the equation $y = (2x^2 - 5x + 2)e^{-x}$.

(a) Find the coordinates of the point where C crosses the y-axis.

(1)

(b) Show that C crosses the x-axis at $x = 2$ and find the x-coordinate of the other point where C crosses the x-axis.

(3)

(c) Find $\dfrac{dy}{dx}$.

(3)

(d) Hence find the exact coordinates of the turning points of C.

(5)

Leave
blank

7.
$$f(x) = \frac{4x-5}{(2x+1)(x-3)} - \frac{2x}{x^2-9}, \qquad x \neq \pm 3, \; x \neq -\frac{1}{2}$$

(a) Show that
$$f(x) = \frac{5}{(2x+1)(x+3)}$$

(5)

The curve C has equation $y = f(x)$. The point $P\left(-1, -\frac{5}{2}\right)$ lies on C.

(b) Find an equation of the normal to C at P.

(8)

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7. A curve C has equation

$$y = 3\sin 2x + 4\cos 2x, \ -\pi \leqslant x \leqslant \pi.$$

The point $A(0, 4)$ lies on C.

(a) Find an equation of the normal to the curve C at A.

(5)

(b) Express y in the form $R\sin(2x + \alpha)$, where $R > 0$ and $0 < \alpha < \dfrac{\pi}{2}$.

Give the value of α to 3 significant figures.

(4)

(c) Find the coordinates of the points of intersection of the curve C with the x-axis. Give your answers to 2 decimal places.

(4)

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4. (a) Differentiate with respect to x

   (i) $x^2 e^{3x+2}$,

   (4)

   (ii) $\dfrac{\cos(2x^3)}{3x}$.

   (4)

   (b) Given that $x = 4\sin(2y + 6)$, find $\dfrac{dy}{dx}$ in terms of x.

   (5)

Leave blank

6. (a) Differentiate with respect to x,

(i) $e^{3x}(\sin x + 2\cos x)$,

(3)

(ii) $x^3 \ln(5x+2)$.

(3)

Given that $y = \dfrac{3x^2 + 6x - 7}{(x+1)^2}$, $x \neq -1$,

(b) show that $\dfrac{dy}{dx} = \dfrac{20}{(x+1)^3}$.

(5)

(c) Hence find $\dfrac{d^2y}{dx^2}$ and the real values of x for which $\dfrac{d^2y}{dx^2} = -\dfrac{15}{4}$.

(3)

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