

Pure Mathematics 2

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Past Paper Collection

Last updated: January 21, 2025

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Please check the examination details below before entering your candidate information			
Candidate surname		Other names	
Pearson Edexcel International Advanced Level		Centre Number <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div>	Candidate Number <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div>
<h2 style="margin: 0;">Tuesday 18 June 2019</h2>			
Morning (Time: 1 hour 30 minutes)		Paper Reference WMA12/01	
<h2 style="margin: 0;">Mathematics</h2> <h3 style="margin: 0;">International Advanced Subsidiary/Advanced Level</h3> <h3 style="margin: 0;">Pure Mathematics P2</h3>			
You must have: Mathematical Formulae and Statistical Tables (Lilac), calculator			Total Marks <div style="border: 1px solid black; width: 40px; height: 40px; margin: 0 auto;"></div>

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

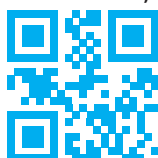
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- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
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Turn over ►

Leave
blank**Question 1 continued**

Q1

(Total 4 marks)

$$x^2 + y^2 + 4x - 10y - 21 = 0$$

Find

- (a)
 - (i) the coordinates of the centre of C ,
 - (ii) the exact value of the radius of C .

(3)

The point $P(5, 4)$ lies on C .

- (b) Find the equation of the tangent to C at P , writing your answer in the form $y = mx + c$, where m and c are constants to be found.

(4)

Q2

(Total 7 marks)

$$(x-4)^2 \geq 2x-9 \tag{3}$$
$$2^n + 1 \text{ is a prime number for all values of } n, n \in \mathbb{N} \quad (1)$$

Q3

(Total 4 marks)

- $$\left(2 - \frac{1}{4}x\right)^6$$

$$\left(2 - \frac{1}{4}x\right)^6 + \left(2 + \frac{1}{4}x\right)^6 = a + bx^2$$

(3)

Leave
blank**Question 4 continued**

Q4

(Total 7 marks)

Q5

Q6

Q7

- (5)

Q8

1

- (4)

Q9

10.

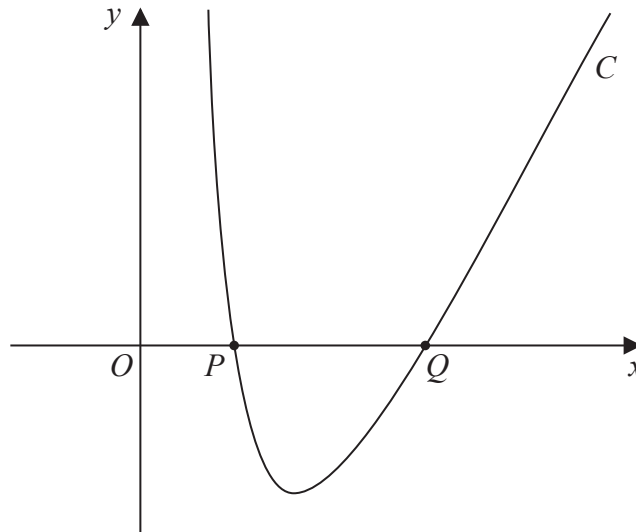


Figure 1

Figure 1 shows a sketch of part of the curve C with equation $y = f(x)$ where

$$f(x) = \frac{36}{x^2} + 2x - 13 \quad x > 0$$

Using calculus,

- (a) find the range of values of x for which $f(x)$ is increasing, (4)

- (b) show that $\int_2^9 \left(\frac{36}{x^2} + 2x - 13 \right) dx = 0$ (4)

The point $P(2, 0)$ and the point $Q(6, 0)$ lie on C .

Given $\int_2^6 \left(\frac{36}{x^2} + 2x - 13 \right) dx = -8$

- (c) (i) state the value of $\int_6^9 \left(\frac{36}{x^2} + 2x - 13 \right) dx$
- (ii) find the value of the constant k such that $\int_2^6 \left(\frac{36}{x^2} + 2x + k \right) dx = 0$ (3)

Q10

END

TOTAL FOR PAPER IS 75 MARKS

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Pearson Edexcel International Advanced Level	<div style="display: flex; justify-content: space-between;"> <div style="text-align: center;"> Centre Number <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> </div> <div style="text-align: center;"> Candidate Number <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> <div style="border: 1px solid black; width: 40px; height: 20px; display: inline-block;"></div> </div> </div>
<div style="border: 1px solid black; padding: 10px; font-size: 1.5em; font-weight: bold;">Wednesday 6 November 2019</div>	
Morning (Time: 1 hour 30 minutes)	Paper Reference WMA12/01
<div style="border: 1px solid black; padding: 10px;"> Mathematics International Advanced Subsidiary/Advanced Level Pure Mathematics P2 </div>	
You must have: Mathematical Formulae and Statistical Tables (Lilac), calculator	Total Marks <div style="border: 1px solid black; width: 60px; height: 40px; margin: 0 auto;"></div>

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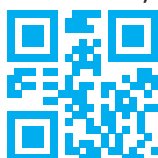
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Turn over ►

(4)

(2)

Q1

- (b) Find, according to these models, the total amount of money that would be given to local charity by the adult population of the town from 2019 to 2032 inclusive. Give your answer to the nearest £1 000
- (3)**

Leave
blank**Question 2 continued**

Q2

(Total 6 marks)

- $$\left(1 + \frac{x}{4}\right)^{12}$$

(3)

- $$\left(\frac{x^2 + 8}{x^5}\right)\left(1 + \frac{x}{4}\right)^{12}$$

(3)

Leave
blank**Question 3 continued****Q3****(Total 6 marks)**

(a) State the remainder when $f(x)$ is divided by $(x - 3)$. (1)

(b) show that $a = -17$ (2)

Leave
blank

Question 4 continued

Q4

5. (a) Given $0 < a < 1$, sketch the curve with equation

$$y = a^x$$

showing the coordinates of the point at which the curve crosses the y -axis.

(2)

x	2	2.5	3	3.5	4
y	4.25	6.427	9.125	12.34	16.06

The table above shows corresponding values of x and y for $y = x^2 + \left(\frac{1}{2}\right)^x$

The values of y are given to 4 significant figures as appropriate.

Using the trapezium rule with all the values of y in the given table,

- (b) obtain an estimate for $\int_2^4 \left(x^2 + \left(\frac{1}{2}\right)^x \right) dx$

(3)

Using your answer to part (b) and making your method clear, estimate

- (c) $\int_2^4 \left(x(x-3) + \left(\frac{1}{2}\right)^x \right) dx$

(2)

Leave
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Question 5 continued

Leave
blank**Question 5 continued****Q5****(Total 7 marks)**

6.

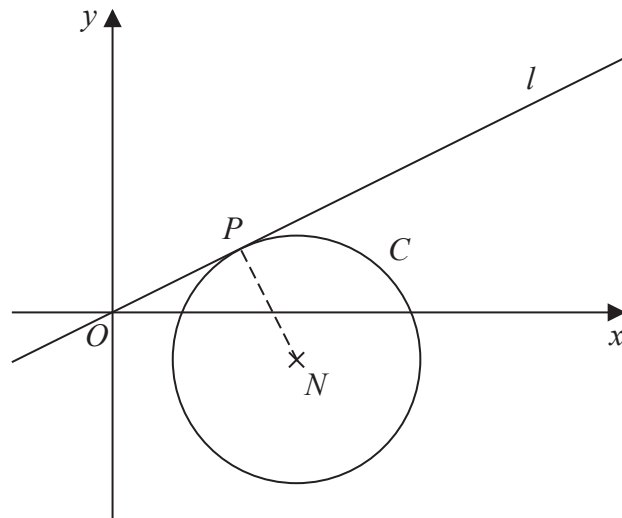


Figure 1

Figure 1 shows a sketch of a circle C with centre $N(4, -1)$.

The line l with equation $y = \frac{1}{2}x$ is a tangent to C at the point P .

Find

- (a) the equation of line PN in the form $y = mx + c$, where m and c are constants, (2)
- (b) the equation of C . (5)

Q6

$$(i) \quad \log_a \left(\frac{\sqrt{a}}{b} \right) \tag{2}$$

$$(ii) \quad \frac{\log_a a^2 b}{\log_a b^3} \tag{2}$$

$$(iii) \sum_{n=1}^{50} (k + \log_a b^n) \tag{3}$$

Leave
blank**Question 7 continued**

Q7

(Total 7 marks)

8. Solutions relying on calculator technology are not acceptable in this question.

(i)

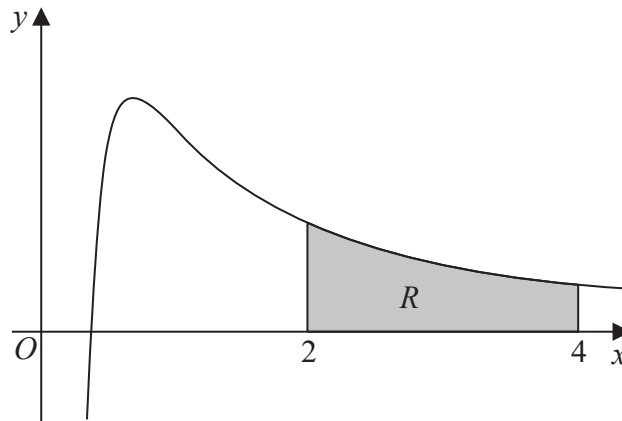


Figure 2

Figure 2 shows a sketch of part of a curve with equation

$$y = \frac{8\sqrt{x} - 5}{2x^2} \quad x > 0$$

The region R , shown shaded in Figure 2, is bounded by the curve, the line with equation $x = 2$, the x -axis and the line with equation $x = 4$

Find the exact area of R .

(5)

(ii) Find the value of the constant k such that

$$\int_{-3}^6 \left(\frac{1}{2}x^2 + k \right) dx = 55$$

(4)

Leave
blank**Question 8 continued**

Q8

(Total 9 marks)

Q9

(Total 12 marks)

Q10

TOTAL FOR PAPER IS 75 MARKS

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Candidate surname		Other names	
Pearson Edexcel		Centre Number	Candidate Number
International		<input type="text"/>	<input type="text"/>
Advanced Level		<input type="text"/>	<input type="text"/>
Wednesday 15 January 2020			
Morning (Time: 1 hour 30 minutes)		Paper Reference WMA12/01	
Mathematics			
International Advanced Subsidiary/Advanced Level			
Pure Mathematics P2			
You must have: Mathematical Formulae and Statistical Tables (Lilac), calculator			Total Marks

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Turn over ►

The values of y are given to 2 decimal places as appropriate.

x	2	5	8	11	14
y	2	3.32	4	4.46	4.81

Using the trapezium rule with all the values of y in the given table,

- (a) obtain an estimate for $\int_2^{14} \log_2(2x)dx$, giving your answer to one decimal place. (3)

Using your answer to part (a) and making your method clear, estimate

$$\begin{aligned} \text{(b) (i)} \quad & \int_2^{14} \frac{\log_2(4x^2)}{5} dx \\ \text{(ii)} \quad & \int_2^{14} \log_2\left(\frac{2}{x}\right) dx \end{aligned} \tag{4}$$

Q1

(Total 7 marks)

- (4)

- $$\left(\frac{1}{81} + \frac{1}{x^6}\right)(3+ax)^6 \quad (3)$$

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Q2

$$f(x) = 6x^3 + 17x^2 + 4x - 12$$

(a) Use the factor theorem to show that $(2x + 3)$ is a factor of $f(x)$.

(2)

(b) Hence, using algebra, write $f(x)$ as a product of three linear factors.

(4)

(c) Solve, for $\frac{\pi}{2} < \theta < \pi$, the equation

$$6 \tan^3 \theta + 17 \tan^2 \theta + 4 \tan \theta - 12 = 0$$

giving your answers to 3 significant figures.

(2)

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Q3

A Cartesian coordinate system with a horizontal x -axis and a vertical y -axis. The origin is labeled O . A horizontal line segment is drawn at $y = 17$ on the y -axis. A curve starts at a point on the y -axis below $y = 17$ and increases, intersecting the horizontal line at $y = 17$. The region R is the shaded area bounded by the y -axis, the horizontal line $y = 17$, and the curve.

Figure 1 shows a sketch of the curve with equation

The finite region R , shown shaded in Figure 1, is bounded by the curve, the y -axis and the line with equation $y = 17$

(6)

[illegible]

Q4

Solutions relying on calculator technology are not acceptable.

(3)

(5)

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Q5

$$x^2 + y^2 + 6x - 4y - 14 = 0$$

(a) Find

- (i) the coordinates of the centre of C ,
- (ii) the exact radius of C .

(3)

The line with equation $y = k$, where k is a constant, is a tangent to C .

(b) Find the possible values of k .

(2)

The line with equation $y = p$, where p is a negative constant, is a chord of C .

Given that the length of this chord is 4 units,

(c) find the value of p .

(3)

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Q6

(3)

(4)

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Q7

- $$(b) \sum_{n=1}^{59} u_n \tag{3}$$

Q8

(Total 7 marks)

9. (a) Sketch the curve with equation

$$y = 3 \times 4^x$$

showing the coordinates of any points of intersection with the coordinate axes.

(2)

The curve with equation $y = 6^{1-x}$ meets the curve with equation $y = 3 \times 4^x$ at the point P .

- (b) Show that the x coordinate of P is $\frac{\log_{10} 2}{\log_{10} 24}$

(5)

Q9

(Total 7 marks)

$$y = 4x^3 - 9x + \frac{k}{x} \quad x > 0$$

The point P with x coordinate $\frac{1}{2}$ lies on C .

(a) show that $k = -\frac{3}{2}$ (4)

(b) Determine the nature of the stationary point at P , justifying your answer. (2)

(c) Using algebra, find the x coordinate of this second stationary point. (4)

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Q10

END

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International		<input type="text"/>	<input type="text"/>
Advanced Level		<input type="text"/>	<input type="text"/>
Wednesday 21 October 2020			
Morning (Time: 1 hour 30 minutes)		Paper Reference WMA12/01	
Mathematics			
International Advanced Subsidiary/Advanced Level			
Pure Mathematics P2			
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Information

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Turn over ►

- $$\left(2 - \frac{x}{4}\right)^{10}$$

(4)

- $$\left(3 - \frac{1}{x}\right)^2 \left(2 - \frac{x}{4}\right)^{10}$$

Leave
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Question 1 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Q1

$$y = \frac{2^x}{\sqrt{(5x^2 + 3)}}$$

x	-0.25	0	0.25	0.5	0.75
y	0.462		0.653		0.698

$$\int_{-0.25}^{0.75} \frac{2^x}{\sqrt{(5x^2 + 3)}} dx$$

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Q2

(Total 4 marks)

Q3

(Total 10 marks)

- (3)

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Question 4 continued

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Q4

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Question 5 continued

Q5

(Total 11 marks)

6.

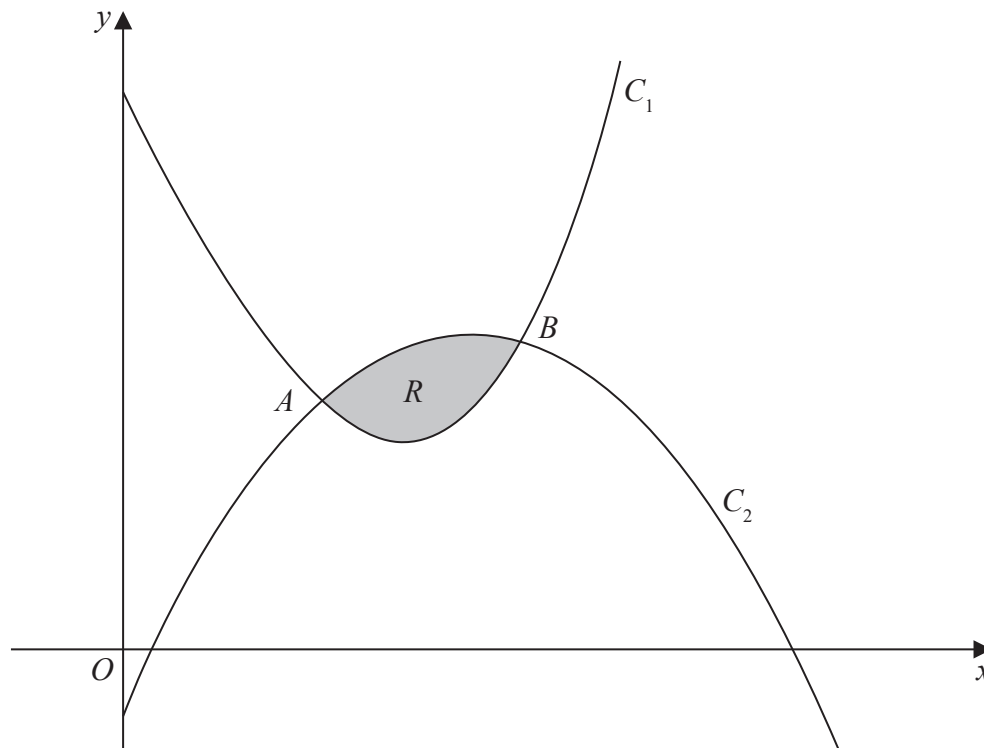
**Figure 1**

Figure 1 shows a sketch of part of the curves C_1 and C_2 with equations

$$\begin{aligned} C_1 : y &= x^3 - 6x + 9 & x &\geq 0 \\ C_2 : y &= -2x^2 + 7x - 1 & x &\geq 0 \end{aligned}$$

The curves C_1 and C_2 intersect at the points A and B as shown in Figure 1.

The point A has coordinates $(1, 4)$.

Using algebra and showing all steps of your working,

(a) find the coordinates of the point B .

(4)

The finite region R , shown shaded in Figure 1, is bounded by C_1 and C_2

(b) Use algebraic integration to find the exact area of R .

(5)

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Q6

$$\tan \theta + \frac{1}{\tan \theta} \equiv \frac{1}{\sin \theta \cos \theta} \quad \theta \neq \frac{n\pi}{2} \quad n \in \mathbb{Z} \quad (3)$$
$$3 \cos^2(2x + 10^\circ) = 1$$

(Solutions based entirely on graphical or numerical methods are not acceptable.) (4)

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Q7

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Question 8 continued

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Q8

$$\log_3(x+5) - 4 = \log_3(2x-1) \quad (4)$$
$$3^{y+3} \times 2^{1-2y} = 108$$
$$0.75^y = 2 \tag{4}$$

(b) Hence find the value of y , giving your answer to 3 decimal places. (2)

Q9

END

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Morning (Time: 1 hour 30 minutes)		Paper Reference WMA12/01	
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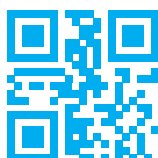
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Turn over ►

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(Total 6 marks)

Q1

$$y = x^3 - x^2 - 16x + 2$$

- (a) Using calculus, find the x coordinates of the stationary points of the curve. (4)
- (b) Justify, by further calculus, the nature of all of the stationary points of the curve. (3)

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Q2

$$7^{x+2} = 3$$

giving your answer in the form $x = \log_7 a$ where a is a rational number in its simplest form.

(3)

(ii) Using the laws of logarithms, solve

$$1 + \log_2 y + \log_2 (y + 4) = \log_2 (5 - y)$$

(5)

[illegible]

(Total 8 marks)

Q3

- (4)

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Q4

- (3)

- (1)

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Q5

$$\frac{3 \sin \theta \cos \theta}{2 \sin \theta - 1} = 5 \tan \theta \quad \sin \theta \neq \frac{1}{2}$$
$$3\sin^3\theta + 10\sin^2\theta - 8\sin\theta = 0$$

(b) Hence solve, for $-\frac{\pi}{4} < x < \frac{\pi}{4}$

$$\frac{3 \sin 2x \cos 2x}{2 \sin 2x - 1} = 5 \tan 2x$$

(4)

Q6

(Total 8 marks)

7.

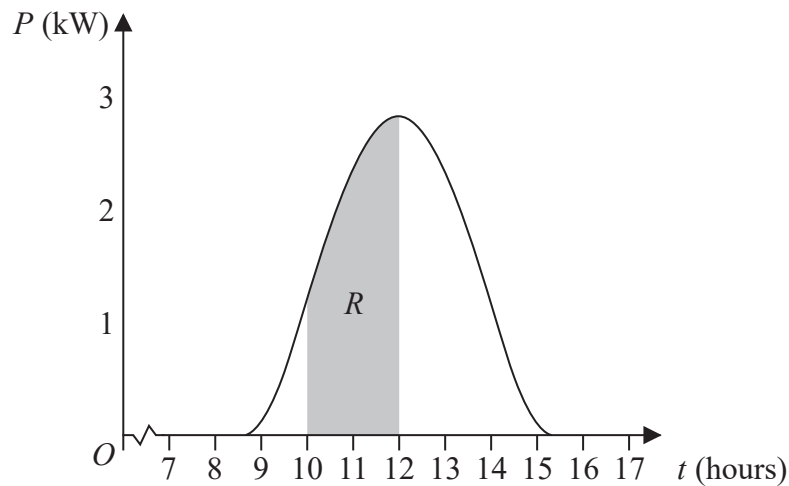


Figure 1

Solar panels are installed on the roof of a building.

The power, P , produced on a particular day, in kW, can be modelled by the equation

$$P = 0.95 + 2^{t-12} + 2^{12-t} - (t-12)^2 \quad 8.5 \leq t \leq 15.2$$

where t is the time in hours after midnight. The graph of P against t is shown in Figure 1.

A table of values of t and P is shown below, with the values of P given to 4 significant figures where appropriate.

Time, t (hours)	10	10.5	11	11.5	12
Power, P (kW)		1.882	2.45		2.95

- (a) Use the given equation to complete the table, giving the values of P to 4 significant figures where appropriate.

(2)

The amount of energy, in kWh, produced between 10:00 and 12:00 can be found by calculating the area of region R , shown shaded in Figure 1.

- (b) Use the trapezium rule, with all the values of P in the completed table, to find an estimate for the amount of energy produced between 10:00 and 12:00. Give your answer to 2 decimal places.

(4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Q7

$$\begin{aligned} a_{n+1} &= 2(a_n + 3)^2 - 7 \\ a_1 &= p - 3 \end{aligned}$$

(a) Find an expression for a_2 in terms of p , giving your answer in simplest form. (1)

(b) find the possible values of a_2 (6)

Q8

(Total 7 marks)

$$(x - k)^2 + (y - 2k)^2 = k + 7$$

where k is a positive constant.

(a) Write down, in terms of k ,

- (i) the coordinates of the centre of C ,
- (ii) the radius of C .

(2)

Given that the point $P(2,3)$ lies on C

- (b) (i) show that $5k^2 - 17k + 6 = 0$
- (ii) hence find the possible values of k .

(3)

The tangent to the circle at P intersects the x -axis at point T .

Given that $k < 2$

- (c) calculate the exact area of triangle OPT .

(5)

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Question 9 continued

Q9

(Total 10 marks)

Q10

END

TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information

Candidate surname		Other names	
Pearson Edexcel		Centre Number	Candidate Number
International Advanced Level		<input type="text"/>	<input type="text"/>
Time 1 hour 30 minutes		Paper reference	WMA12/01
Mathematics International Advanced Subsidiary/Advanced Level Pure Mathematics P2			
You must have: Mathematical Formulae and Statistical Tables (Yellow), calculator			Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.
- Good luck with your examination



Turn over ►

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(Total 7 marks)

Q1

2.

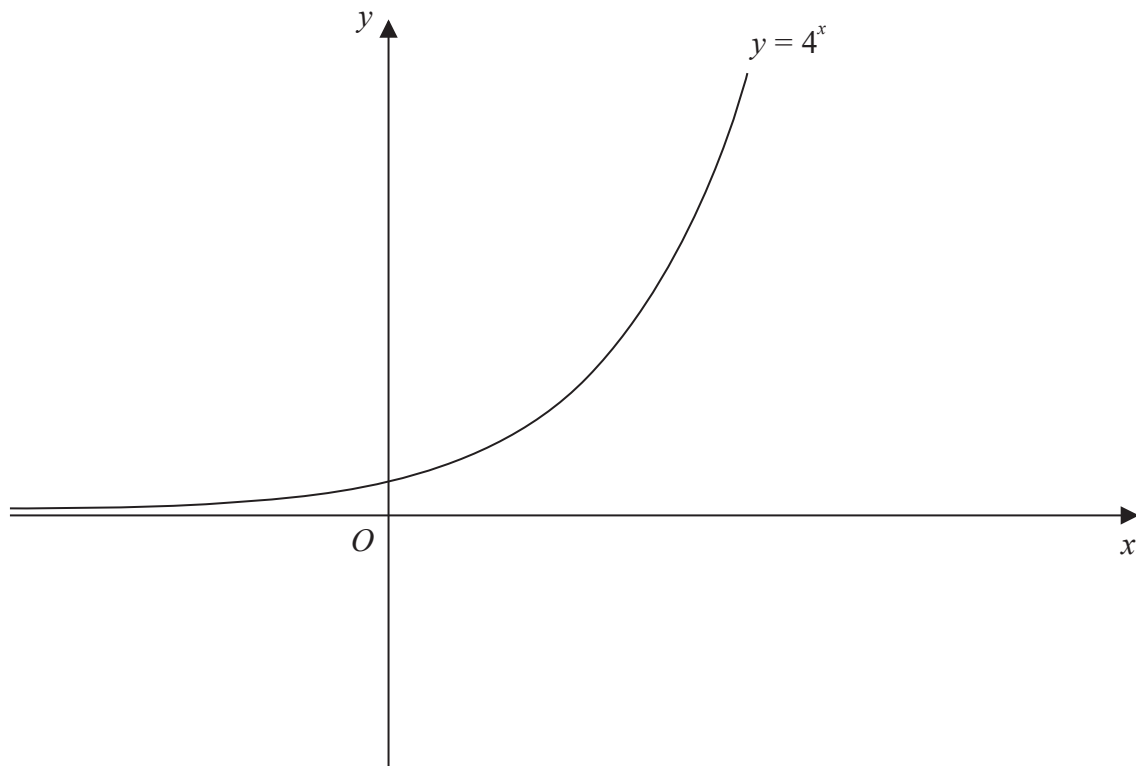
**Figure 1**

Figure 1 shows a sketch of the curve with equation $y = 4^x$

A copy of Figure 1, labelled Diagram 1, is shown on the next page.

(a) On Diagram 1, sketch the curve with equation

(i) $y = 2^x$

(ii) $y = 4^x - 6$

Label clearly the coordinates of any points of intersection with the coordinate axes.

(4)

The curve with equation $y = 2^x$ meets the curve with equation $y = 4^x - 6$ at the point P .

(b) Using algebra, find the exact coordinates of P .

(4)

A graph of the exponential function $y = 4^x$ is shown on a Cartesian coordinate system. The x-axis and y-axis are labeled, and the origin is marked with O . The curve passes through the y-axis at $(0, 1)$ and increases rapidly as x increases. The equation $y = 4^x$ is labeled next to the curve.

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Q2

(2)

(3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Q3

- $$\left(2 + \frac{x}{8}\right)^{13}$$

(4)

- (3)

(1)

Q4

(Total 8 marks)

5.

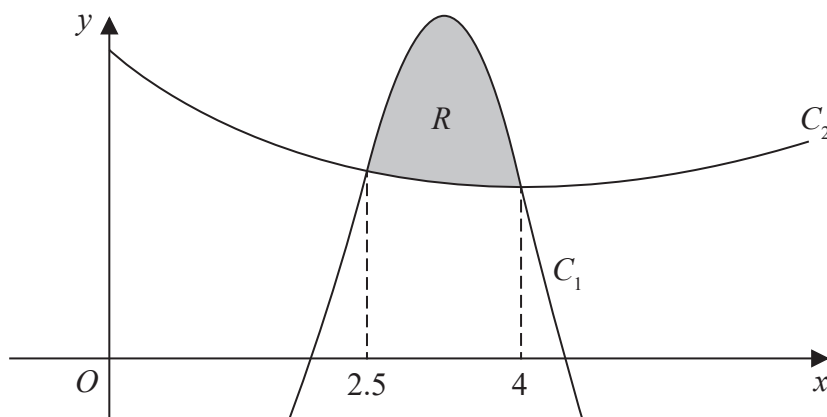


Figure 2

Figure 2 shows a sketch of part of the graph of the curves C_1 and C_2

The curves intersect when $x = 2.5$ and when $x = 4$

A table of values for some points on the curve C_1 is shown below, with y values given to 3 decimal places as appropriate.

x	2.5	2.75	3	3.25	3.5	3.75	4
y	5.453	7.764	9.375	9.964	9.367	7.626	5

Using the trapezium rule with all the values of y in the table,

- (a) find, to 2 decimal places, an estimate for the area bounded by the curve C_1 , the line with equation $x = 2.5$, the x -axis and the line with equation $x = 4$

(4)

The curve C_2 has equation

$$y = x^{\frac{3}{2}} - 3x + 9 \quad x > 0$$

- (b) Find $\int \left(x^{\frac{3}{2}} - 3x + 9 \right) dx$

(3)

The region R , shown shaded in Figure 2, is bounded by the curves C_1 and C_2

- (c) Use the answers to part (a) and part (b) to find, to one decimal place, an estimate for the area of the region R .

(3)

Q5

(Total 10 marks)

(4)

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Question 6 continued

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Question 6 continued

Q6

(Total 7 marks)

$$3 \log_3(2x - 1) = 2 + \log_3(14x - 25)$$

show that

$$2x^3 - 3x^2 - 30x + 56 = 0 \quad (4)$$

(b) Show that -4 is a root of this cubic equation. (2)

(c) Hence, using algebra and showing each step of your working, solve

$$3\log_3(2x-1) = 2 + \log_3(14x-25) \quad (4)$$

Q7

(Total 10 marks)

Solutions relying entirely on calculator technology are not acceptable.

- $$3 \sin(\theta + 30^\circ) = 7 \cos(\theta + 30^\circ)$$

(4)

- $$3 \sin^3 x = 5 \sin x - 7 \sin x \cos x$$

$$\sin x (a \cos^2 x + b \cos x + c) = 0$$

(b) Hence solve for $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$ the equation

(6)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Q8

(Total 10 marks)

A 3D diagram of a rectangular prism. The front face is a rectangle with a horizontal base labeled $l\text{ cm}$ and a vertical height labeled $h\text{ cm}$. The depth of the prism is indicated by a dashed line from the bottom-left corner of the front face to the bottom-left corner of the back face, labeled $l\text{ cm}$. The back face is a rectangle of the same size as the front face. All edges are drawn with solid lines, except for the hidden edges (the bottom-left vertical edge and the bottom-left horizontal edge of the back face) which are dashed.

Figure 3 shows a sketch of a square based, open top box.

Given that the volume of the box is $250\,000\text{ cm}^3$

- $$S = \frac{250\,000}{h} + 2000\sqrt{h} \quad (3)$$

- (b) Use algebraic differentiation to show that S has a stationary point when $h = 250^k$ where k is a rational constant to be found.
- (5)**

- (c) Justify by further differentiation that this value of h gives the minimum external surface area of the box.
- (2)**

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Question 9 continued

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(Total 10 marks)

END

TOTAL FOR PAPER IS 75 MARKS

Q9

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				
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Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes **Paper reference** **WMA12/01**

Mathematics
International Advanced Subsidiary/Advanced Level
Pure Mathematics P2

You must have:
 Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

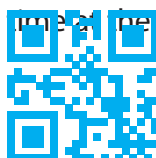
- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 – *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
 – *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.



Turn over ►

Q1

Q2

(Total 5 marks)

3.

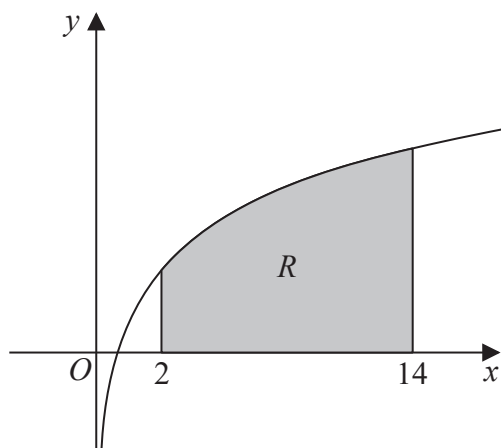
**Figure 1**

Figure 1 shows a sketch of part of the curve with equation $y = \log_{10} x$

The region R , shown shaded in Figure 1, is bounded by the curve, the line with equation $x = 2$, the x -axis and the line with equation $x = 14$

Using the trapezium rule with four strips of equal width,

(a) show that the area of R is approximately 10.10 (3)

(b) Explain how the trapezium rule could be used to obtain a more accurate estimate for the area of R . (1)

(c) Using the answer to part (a) and making your method clear, estimate the value of

(i) $\int_2^{14} \log_{10} \sqrt{x} \, dx$

(ii) $\int_2^{14} \log_{10} 100x^3 \, dx$

(4)

Q3

(Total 8 marks)

Q4

- extracted 480 tonnes of silver from the mine in year 1
- extracted 465 tonnes of silver from the mine in year 2
- extracted 450 tonnes of silver from the mine in year 3

(a) Find the mass of silver extracted in year 14

(b) show that

$$N^2 - 65N + 1036 = 0$$

(c) Hence, state the value of N .

Q5

- find the exact value of p . (4)

Q6

Q7

(Total 10 marks)

8. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

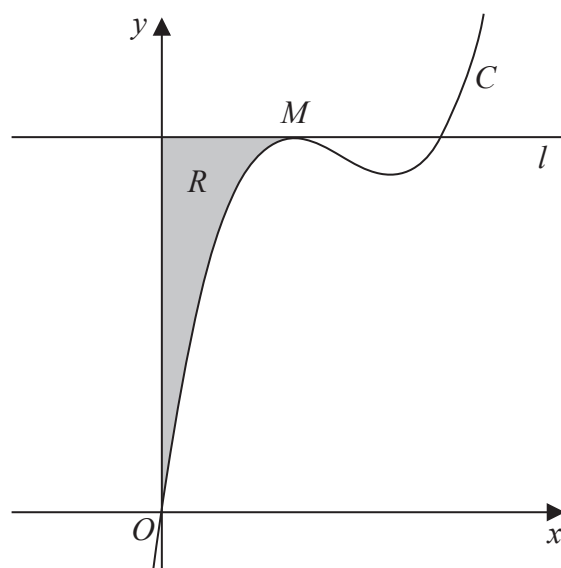


Figure 2

Figure 2 shows a sketch of part of the curve C with equation

$$y = \frac{4}{3}x^3 - 11x^2 + kx \quad \text{where } k \text{ is a constant}$$

The point M is the maximum turning point of C and is shown in Figure 2.

Given that the x coordinate of M is 2

(a) show that $k = 28$ (3)

(b) Determine the range of values of x for which y is increasing. (2)

The line l passes through M and is parallel to the x -axis.

The region R , shown shaded in Figure 2, is bounded by the curve C , the line l and the y -axis.

(c) Find, by algebraic integration, the exact area of R . (5)

Q8

(Total 10 marks)

- $$\frac{x+y}{2} \geq \sqrt{xy}$$

(b) Prove by counter-example that this inequality does not hold when x and y are both negative.

Q9

Solutions relying entirely on calculator technology are not acceptable.

- $$\tan^2\left(2x + \frac{\pi}{4}\right) = 3 \quad (5)$$

- $$(2 \sin \theta - \cos \theta)^2 = 1$$

giving your answers, as appropriate, to one decimal place.

(5)

(Total 10 marks)

Q10

END

TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				
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Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper reference **WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

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Instructions

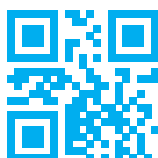
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- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
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Advice

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- Try to answer every question.
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- If you change your mind about an answer, cross it out and put your new answer and any working underneath.



Turn over ►

- $$y = 2^{5-\sqrt{x}}$$

x	5	5.5	6	6.5	7
y	6.792	6.298	5.858	5.466	5.113

$$\int_5^7 2^{5-\sqrt{x}} \, dx$$

(3)

- (i) $\int_5^7 2^{6-\sqrt{x}} \, dx$

(4)

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Question 1 continued

This image shows a full page of blank, lined paper. It features approximately 28 horizontal blue or grey lines spaced evenly apart, typical of standard notebook paper. The lines extend across the entire width of the page, leaving small margins at the top and bottom. There are no vertical lines, text, or other markings present.

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Q1

Solutions relying entirely on calculator technology are not acceptable.

$$y = 27x^{\frac{1}{2}} - x^{\frac{3}{2}} - 20 \quad x > 0$$

- (a) Find $\frac{dy}{dx}$, giving each term in simplest form. (2)
- (b) Hence find the coordinates of the stationary point of C . (4)
- (c) Find $\frac{d^2y}{dx^2}$ and hence determine the nature of the stationary point of C . (2)

Q2

(Total 8 marks)

- $$\left(2 - \frac{kx}{4}\right)^8$$

(4)

$$f(x) = (5 - 3x) \left(2 - \frac{kx}{4} \right)^8$$

(3)

This image shows a full page of blank, lined paper. It features approximately 28 horizontal blue or grey lines spaced evenly apart, typical of standard notebook paper. The lines extend across the entire width of the page, leaving small margins at the top and bottom. There are no vertical lines, text, or other markings present.

Q3

(Total 7 marks)

(5)

Q4

(Total 5 marks)

Q5

A circle is shown in the Cartesian plane with center O at the origin $(0,0)$. Three points are marked on the circle: $P(23, 14)$ in the first quadrant, $Q(15, -30)$ in the fourth quadrant, and $R(-7, -26)$ in the third quadrant.

The points $P(23, 14)$, $Q(15, -30)$ and $R(-7, -26)$ lie on the circle C , as shown in Figure 1.

- Given that the point S lies on C such that the distance QS is greatest,

- (c) find an equation of the tangent to C at S , giving your answer in the form $ax + by + c = 0$, where a , b and c are integers to be found.
- (3)**

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Question 6 continued

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Question 6 continued

Q6

(Total 8 marks)

Solutions relying entirely on calculator technology are not acceptable.

- $$3 \sin(2x - 15^\circ) = \cos(2x - 15^\circ)$$

(4)

- $$4 \sin^2 \theta + 8 \cos \theta = 3$$

(4)

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Q7

Given that

- (a) show that the post is driven an **additional** 62 mm into the ground with the 20th hit. **(1)**

Given that for each subsequent hit after the 20th hit

- (c) find the value of r , giving your answer to 3 decimal places. (2)

(d) Find, showing all steps in your working, the smallest possible value of N . (4)

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Question 8 continued

This image shows a full page of blank, lined paper. It features approximately 20 evenly spaced horizontal grey lines across its entire width, providing a guide for handwriting or typing. The background is a clean, solid white color.

Q8

9.

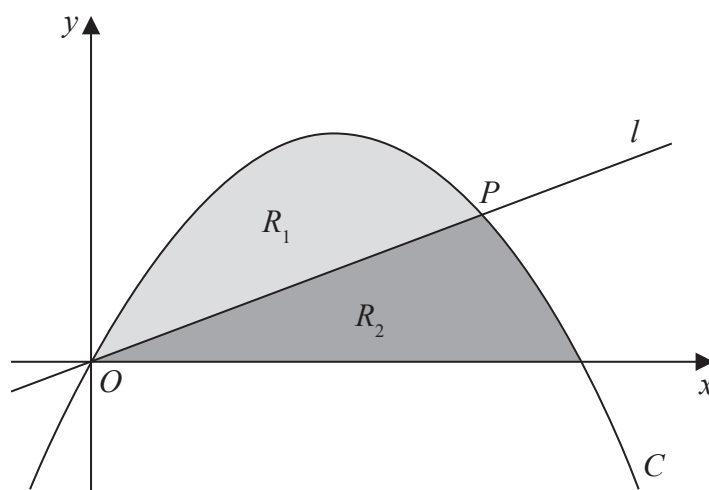
**Figure 2**

Figure 2 shows

- the curve C with equation $y = x - x^2$
- the line l with equation $y = mx$, where m is a constant and $0 < m < 1$

The line and the curve intersect at the origin O and at the point P .

- (a) Find, in terms of m , the coordinates of P .

(2)

The region R_1 , shown shaded in Figure 2, is bounded by C and l .

- (b) Show that the area of R_1 is

$$\frac{(1-m)^3}{6}$$

(5)

The region R_2 , also shown shaded in Figure 2, is bounded by C , the x -axis and l .

Given that the area of R_1 is equal to the area of R_2

- (c) find the exact value of m .

(3)

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Q9

(1)

(4)

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Question 10 continued

[illegible]

(Total 5 marks)

Q10

END

TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information

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Centre Number					Candidate Number				
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Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper reference **WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

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Instructions

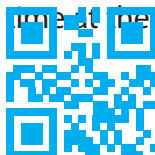
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Information

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Turn over ►

- $$\left(2 + \frac{3}{8}x\right)^{10}$$

(4)

Q1

2.

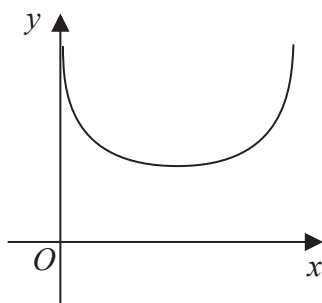
**Figure 1**

Figure 1 shows the graph of

$$y = 1 - \log_{10}(\sin x) \quad 0 < x < \pi$$

where x is in radians.

The table below shows some values of x and y for this graph, with values of y given to 3 decimal places.

x	0.5	1	1.5	2	2.5	3
y	1.319		1.001		1.223	1.850

(a) Complete the table above, giving values of y to 3 decimal places.

(2)

(b) Use the trapezium rule with all the y values in the completed table to find, to 2 decimal places, an estimate for

$$\int_{0.5}^3 (1 - \log_{10}(\sin x)) dx$$

(3)

(c) Use your answer to part (b) to find an estimate for

$$\int_{0.5}^3 (3 + \log_{10}(\sin x)) dx$$

(3)

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Question 2 continued

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Q2

(Total 8 marks)

- (5)

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Question 3 continued

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Question 3 continued

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Q3

(Total 7 marks)

Give your answers in fully simplified surd form.

$$\begin{aligned} a - b &= 8 \\ \log_4 a + \log_4 b &= 3 \end{aligned}$$

(6)

Q4

(Total 6 marks)

Solutions relying entirely on calculator technology are not acceptable.

$$3 \tan(\theta + 43^\circ) = 2 \cos(\theta + 43^\circ)$$

(6)

Q5

- the common ratio is r
- $u_2 + u_3 = 6$
- $u_4 = 8$

$$3r^2 - 4r - 4 = 0$$

(b) find u_1

(c) find S_∞

(2)

Q6

$$f(x) = Ax^3 + 6x^2 - 4x + B$$

where A and B are constants.

Given that

- $(x + 2)$ is a factor of $f(x)$
- $\int_3^5 f(x) dx = 176$

find the value of A and the value of B .

(7)

Q7

Solutions relying entirely on calculator technology are not acceptable.

$$y = 256x^4 - 304x - 35 + \frac{27}{x^2} \quad x \neq 0$$

(3)

(5)

Q8

The equation for carbon-14 dating an item is given by

$$N = k\lambda^t$$

where

- N grams is the amount of carbon-14 **currently** present in the item
- k grams was the **initial** amount of carbon-14 present in the item
- t is the number of years since the item was made
- λ is a constant, with $0 < \lambda < 1$

- (a) Sketch the graph of N against t for $k = 1$ (2)

Given that it takes 5700 years for the amount of carbon-14 to reduce to half its initial value,

- (b) show that the value of the constant λ is 0.999878 to 6 decimal places. (2)

Given that Item A

- is known to have had 15 grams of carbon-14 present initially
- is thought to be 3250 years old

- (c) calculate, to 3 significant figures, how much carbon-14 the equation predicts is currently in Item *A*.
- (2)

Item *B* is known to have initially had 25 grams of carbon-14 present, but only 18 grams now remain.

- (d) Use algebra to calculate the age of Item *B* to the nearest 100 years.

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Question 9 continued

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Question 9 continued

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Q9

10. The circle C has centre $X(3, 5)$ and radius r

The line l has equation $y = 2x + k$, where k is a constant.

(a) Show that l and C intersect when

$$5x^2 + (4k - 26)x + k^2 - 10k + 34 - r^2 = 0$$

(3)

Given that l is a tangent to C ,

(b) show that $5r^2 = (k + p)^2$, where p is a constant to be found.

(3)

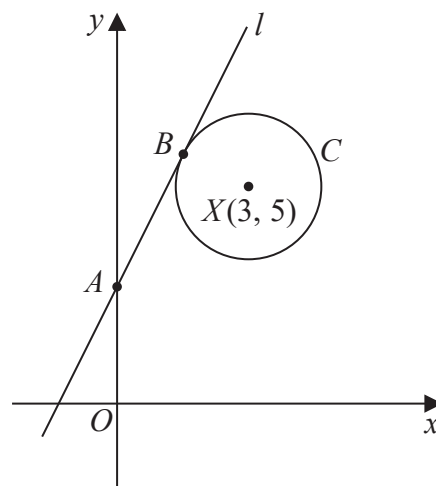


Figure 2

The line l

- cuts the y -axis at the point A
- touches the circle C at the point B

as shown in Figure 2.

Given that $AB = 2r$

(c) find the value of k

(6)

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Question 10 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Q10

(Total 12 marks)

END

TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information

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Centre Number					Candidate Number				
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Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper reference **WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.



Turn over ►

1. Given that a, b and c are integers greater than 0 such that

- $c = b + 2$
- $a + b + c = 10$

Prove, by exhaustion, that the product of a , b and c is always even.

You may use the table below to illustrate your answer.

(3)

You may not need to use all rows of this table.

a	b	c
	1	
	2	

Question 1 continued

(Total for Question 1 is 3 marks)

Question 2 continued

Question 2 continued

Question 2 continued

(Total for Question 2 is 7 marks)

3. A sequence a_1, a_2, a_3, \dots is defined by

$$a_n = \cos^2\left(\frac{n\pi}{3}\right)$$

Find the exact values of

- (a) (i) a_1
- (ii) a_2
- (iii) a_3

(3)

(b) Hence find the exact value of

$$\sum_{n=1}^{50} \left\{ n + \cos^2 \left(\frac{n}{3} \right) \right\}$$

You must make your method clear.

(4)

Question 3 continued

(Total for Question 3 is 7 marks)

4. The weight of a baby mammal is monitored over a 16-month period.

The weight of the mammal, w kg, is given by

$$w = \log_a(t + 5) - \log_a 4 \quad 2 \leq t \leq 18$$

where t is the age of the mammal in months and a is a constant.

Given that the weight of the mammal was 10kg when $t = 3$

- (a) show that $a = 1.072$ correct to 3 decimal places. (3)

Using $a = 1.072$

- (b) find an equation for t in terms of w (3)

- (c) find the value of t when $w = 15$, giving your answer to 3 significant figures. (2)

Question 4 continued

(Total for Question 4 is 8 marks)

5. In this question you must show detailed reasoning.

Solutions relying entirely on calculator technology are not acceptable.

(a) Show that the equation

$$(3 \cos \theta - \tan \theta) \cos \theta = 2$$

can be written as

$$3 \sin^2 \theta + \sin \theta - 1 = 0 \quad (3)$$

(b) Hence solve for $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$

$$(3 \cos 2x - \tan 2x) \cos 2x = 2 \quad (5)$$

Question 5 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 5 continued

Question 5 continued

(Total for Question 5 is 8 marks)

6. The curve C_1 has equation $y = f(x)$.

A table of values of x and y for $y = f(x)$ is shown below, with the y values rounded to 4 decimal places where appropriate.

x	0	0.5	1	1.5	2
y	3	2.6833	2.4	2.1466	1.92

(a) Use the trapezium rule with all the values of y in the table to find an approximation for

$$\int_0^2 f(x) \, dx$$

giving your answer to 3 decimal places.

(3)

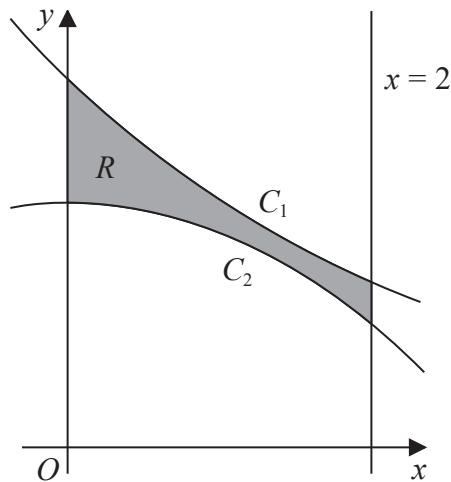


Figure 1

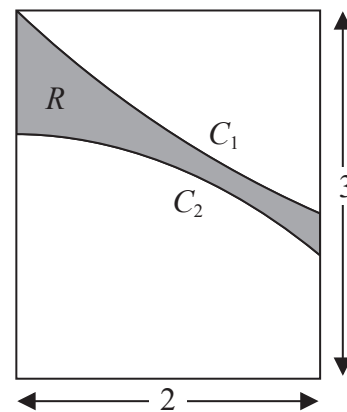


Figure 2

The region R , shown shaded in Figure 1, is bounded by

- the curve C_1
- the curve C_2 with equation $y = 2 - \frac{1}{4}x^2$
- the line with equation $x = 2$
- the y -axis

The region R forms part of the design for a logo shown in Figure 2.

The design consists of the shaded region R inside a rectangle of width 2 and height 3

Using calculus and the answer to part (a),

(b) calculate an estimate for the percentage of the logo which is shaded.

(4)

Question 6 continued

Question 6 continued

Question 6 continued

(Total for Question 6 is 7 marks)

Question 7 continued

Question 7 continued

Question 7 continued

(Total for Question 7 is 9 marks)

Question 8 continued

(Total for Question 8 is 7 marks)

9. In this question you must show detailed reasoning.

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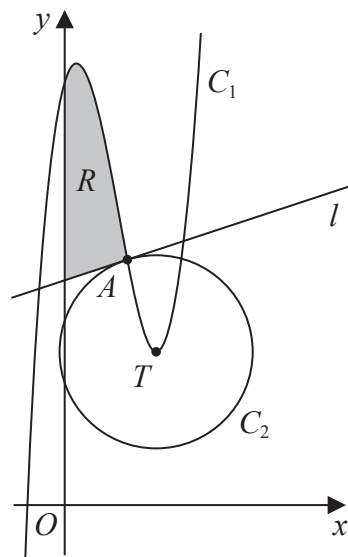


Figure 3

Figure 3 shows

- the curve C_1 with equation $y = x^3 - 5x^2 + 3x + 14$
- the circle C_2 with centre T

The point T is the minimum turning point of C_1

Using Figure 3 and calculus,

- (a) find the coordinates of T (3)

The curve C_1 intersects the circle C_2 at the point A with x coordinate 2

- (b) Find an equation of the circle C_2 (3)

The line l shown in Figure 3, is the tangent to circle C_2 at A

- (c) Show that an equation of l is

$$y = \frac{1}{3}x + \frac{22}{3} \quad (3)$$

The region R , shown shaded in Figure 3, is bounded by C_1 , l and the y -axis.

- (d) Find the exact area of R . (3)

Question 9 continued

Question 9 continued

Question 9 continued

(Total for Question 9 is 12 marks)

10. Given $a = \log_2 3$

(i) write, in simplest form, in terms of a ,

(a) $\log_2 9$

$$(b) \log_2 \left(\frac{\sqrt{3}}{16} \right)$$

(3)

(ii) Solve

$$3^x \times 2^{x+4} = 6$$

giving your answer, in simplest form, in terms of a .

(4)

Question 10 continued

Question 10 continued

(Total for Question 10 is 7 marks)

TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				

Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes **Paper reference** **WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

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Instructions

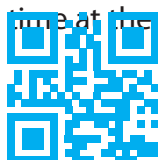
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Turn over ►

1.

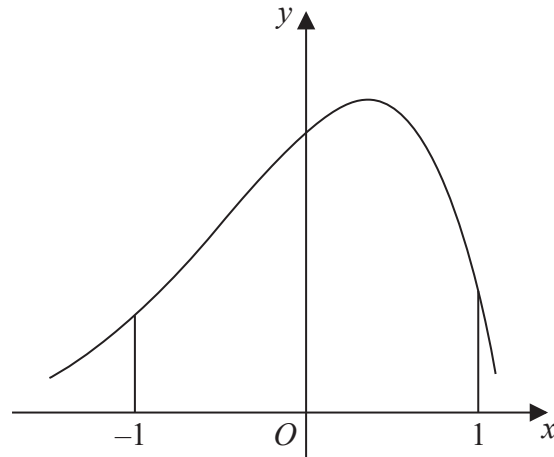


Figure 1

Figure 1 shows a sketch of part of the curve with equation $y = f(x)$

The table below shows some corresponding values of x and y for this curve.

The values of y are given to 3 decimal places.

x	-1	-0.5	0	0.5	1
y	2.287	4.470	6.719	7.291	2.834

Using the trapezium rule with all the values of y in the given table,

(a) obtain an estimate for

$$\int_{-1}^1 f(x) \, dx$$

giving your answer to 2 decimal places.

(3)

(b) Use your answer to part (a) to estimate

(i) $\int_{-1}^1 (f(x) - 2) \, dx$

(ii) $\int_1^3 f(x-2) \, dx$

(3)

Question 1 continued

(Total for Question 1 is 6 marks)

2.

In this question you must show all stages of your working.

Solutions based entirely on calculator technology are not acceptable.

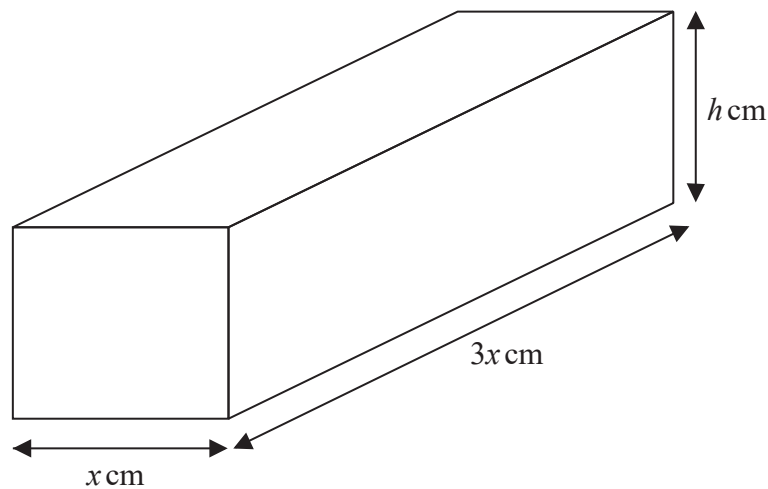


Figure 2

A brick is in the shape of a cuboid with width $x \text{ cm}$, length $3x \text{ cm}$ and height $h \text{ cm}$, as shown in Figure 2.

The volume of the brick is 972 cm^3

(a) Show that the surface area of the brick, $S \text{ cm}^2$, is given by

$$S = 6x^2 + \frac{2592}{x} \quad (3)$$

(b) Find $\frac{dS}{dx}$ (1)

(c) Hence find the value of x for which S is stationary. (2)

(d) Find $\frac{d^2S}{dx^2}$ and hence show that the value of x found in part (c) gives the minimum value of S . (2)

(e) Hence find the minimum surface area of the brick. (1)

Question 2 continued

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Question 2 continued

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Question 2 continued

(Total for Question 2 is 9 marks)

3.

$$f(x) = \left(2 + \frac{kx}{8}\right)^7 \quad \text{where } k \text{ is a non-zero constant}$$

- (a) Find the first 4 terms, in ascending powers of x , of the binomial expansion of $f(x)$.
Give each term in simplest form.

(4)

Given that, in the binomial expansion of $f(x)$, the coefficients of x , x^2 and x^3 are the first 3 terms of an arithmetic progression,

- (b) find, using algebra, the possible values of k .

(Solutions relying entirely on calculator technology are not acceptable.)

(3)

Question 3 continued

(Total for Question 3 is 7 marks)

4. (i) Using the laws of logarithms, solve

$$\log_3(4x) + 2 = \log_3(5x + 7) \quad (3)$$

(ii) Given that

$$\sum_{r=1}^2 \log_a(y^r) = \sum_{r=1}^2 (\log_a y)^r \quad y > 1, a > 1, y \neq a$$

find y in terms of a , giving your answer in simplest form. (3)

Question 4 continued

(Total for Question 4 is 6 marks)

5.

$$f(x) = x^3 + (p + 3)x^2 - x + q$$

where p and q are constants and $p > 0$

Given that $(x - 3)$ is a factor of $f(x)$

(a) show that

$$9p + q = -51 \quad (2)$$

Given also that when $f(x)$ is divided by $(x + p)$ the remainder is 9

(b) show that

$$3p^2 + p + q - 9 = 0 \quad (2)$$

(c) Hence find the value of p and the value of q . (3)

(d) Hence find a quadratic expression $g(x)$ such that

$$f(x) = (x - 3)g(x) \quad (2)$$

Question 5 continued

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Question 5 continued

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Question 5 continued

(Total for Question 5 is 9 marks)

6. The circle C has equation

$$x^2 + y^2 + 8x - 4y = 0$$

(a) Find

- (i) the coordinates of the centre of C ,
- (ii) the exact radius of C .

(3)

The point P lies on C .

Given that the tangent to C at P has equation $x + 2y + 10 = 0$

(b) find the coordinates of P

(4)

(c) Find the equation of the normal to C at P , giving your answer in the form $y = mx + c$ where m and c are integers to be found.

(3)

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Question 6 continued

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Question 6 continued

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Question 6 continued

(Total for Question 6 is 10 marks)

7. A geometric sequence has first term a and common ratio r , where $r > 0$

Given that

- the 3rd term is 20
- the 5th term is 12.8

(a) show that $r = 0.8$

(1)

(b) Hence find the value of a .

(2)

Given that the sum of the first n terms of this sequence is greater than 156

(c) find the smallest possible value of n .

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(4)

Question 7 continued

(Total for Question 7 is 7 marks)

8. In this question you must show all stages of your working.

Solutions based entirely on calculator technology are not acceptable.

- (i) Solve, for $-\frac{\pi}{2} < x < \pi$, the equation

$$5 \sin(3x + 0.1) + 2 = 0$$

giving your answers, **in radians**, to 2 decimal places.

(4)

- (ii) Solve, for $0 < \theta < 360^\circ$, the equation

$$2 \tan \theta \sin \theta = 5 + \cos \theta$$

giving your answers, **in degrees**, to one decimal place.

(5)

Question 8 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 8 continued

[illegible]

Question 8 continued

(Total for Question 8 is 9 marks)

9. In this question you must show all stages of your working.

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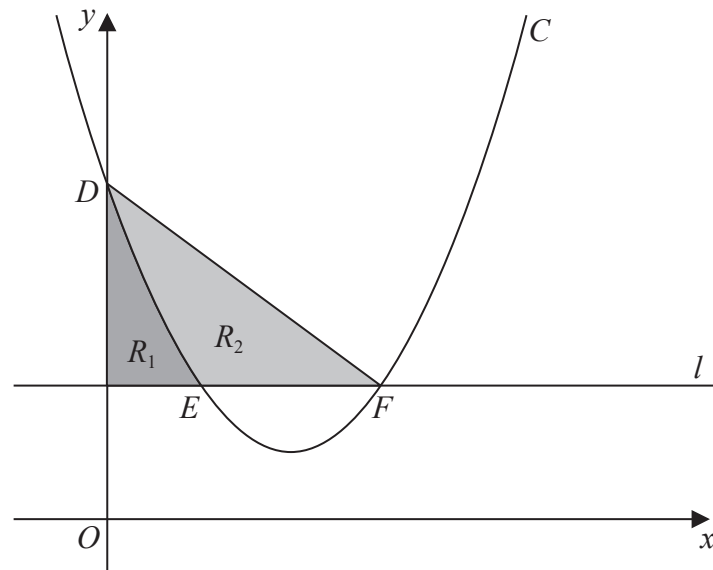


Figure 3

Figure 3 shows

- the curve C with equation $y = x^2 - 4x + 5$
- the line l with equation $y = 2$

The curve C intersects the y -axis at the point D .

(a) Write down the coordinates of D .

(1)

The curve C intersects the line l at the points E and F , as shown in Figure 3.

(b) Find the x coordinate of E and the x coordinate of F .

(2)

Shown shaded in Figure 3 is

- the region R_1 which is bounded by C , l and the y -axis
- the region R_2 which is bounded by C and the line segments EF and DF

Given that $\frac{\text{area of } R_1}{\text{area of } R_2} = k$, where k is a constant,

(c) use algebraic integration to find the exact value of k , giving your answer as a simplified fraction.

(5)

Question 9 continued

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Question 9 continued

[illegible]

Question 9 continued

(Total for Question 9 is 8 marks)

10. A student was asked to prove by exhaustion that

if n is an integer then $2n^2 + n + 1$ is **not** divisible by 3

The start of the student's proof is shown in the box below.

Consider the case when $n = 3k$

$$2n^2 + n + 1 = 18k^2 + 3k + 1 = 3(6k^2 + k) + 1$$

which is not divisible by 3

Complete this proof.

(4)

Question 10 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 10 continued

(Total for Question 10 is 4 marks)

TOTAL FOR PAPER IS 75 MARKS

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Pearson Edexcel International Advanced Level

Thursday 18 May 2023

Morning (Time: 1 hour 30 minutes) **Paper reference** **WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

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Instructions

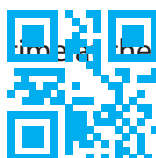
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Information

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- There are 11 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
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Advice

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- Try to answer every question.
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Turn over ►

- 1.** The continuous curve C has equation $y = f(x)$.

A table of values of x and y for $y = f(x)$ is shown below.

x	4.0	4.2	4.4	4.6	4.8	5.0
y	9.2	8.4556	3.8512	5.0342	7.8297	8.6

Use the trapezium rule with all the values of y in the table to find an approximation for

$$\int_4^5 f(x) \, dx$$

giving your answer to 3 decimal places.

(3)

Question 1 continued

(Total for Question 1 is 3 marks)

2.

In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

$$f(x) = 4x^3 - 8x^2 + 5x + a$$

where a is a constant.

Given that $(2x - 3)$ is a factor of $f(x)$,

(a) use the factor theorem to show that $a = -3$

(2)

(b) Hence show that the equation $f(x) = 0$ has only one real root.

(4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 2 continued

(Total for Question 2 is 6 marks)

3. A circle C has centre $(2, 5)$

Given that the point $P(8, -3)$ lies on C

- (a) (i) find the radius of C

- (ii) find an equation for C

(3)

- (b) Find the equation of the tangent to C at P giving your answer in the form $ax + by + c = 0$ where a , b and c are integers to be found.

(4)

Question 3 continued

(Total for Question 3 is 7 marks)

4. The binomial expansion, in ascending powers of x , of

$$(3 + px)^5$$

where p is a constant, can be written in the form

$$A + Bx + Cx^2 + Dx^3 \dots$$

where A, B, C and D are constants.

(a) Find the value of A

(1)

Given that

- $B = 18D$
- $p < 0$

(b) find

- (i) the value of p
- (ii) the value of C

(6)

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Question 4 continued

[illegible]

Question 4 continued

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Question 4 continued

(Total for Question 4 is 7 marks)

5. Use the laws of logarithms to solve

$$\log_2(16x) + \log_2(x + 1) = 3 + \log_2(x + 6)$$

(5)

Question 5 continued

(Total for Question 5 is 5 marks)

6. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

A software developer released an app to download.

The numbers of downloads of the app each month, in thousands, for the first three months after the app was released were

$$2k - 15 \quad k \quad k + 4$$

where k is a constant.

Given that the numbers of downloads each month are modelled as a geometric series,

- (a) show that $k^2 - 7k - 60 = 0$

- (b) predict the number of downloads in the 4th month. (4)

The **total** number of all downloads of the app is predicted to exceed 3 million for the first time in the N th month.

- (c) Calculate the value of N according to the model. (3)

Question 6 continued

[illegible]

Question 6 continued

[illegible]

Question 6 continued

(Total for Question 6 is 9 marks)

7. The height of a river above a fixed point on the riverbed was monitored over a 7-day period.

The height of the river, H metres, t days after monitoring began, was given by

$$H = \frac{\sqrt{t}}{20}(20 + 6t - t^2) + 17 \quad 0 \leq t \leq 7$$

Given that H has a stationary value at $t = \alpha$

- (a) use calculus to show that α satisfies the equation

$$5\alpha^2 - 18\alpha - 20 = 0 \quad (5)$$

- (b) Hence find the value of α , giving your answer to 3 decimal places. (1)

- (c) Use further calculus to prove that H is a maximum at this value of α . (2)

Question 7 continued

(Total for Question 7 is 8 marks)

8. (i) A student writes the following statement:

“When a and b are consecutive **prime** numbers, $a^2 + b^2$ is never a multiple of 10”

Prove by counter example that this statement is **not** true.

(2)

- (ii) Given that x and y are even integers greater than 0 and less than 6, prove by exhaustion, that

$$1 < x^2 - \frac{xy}{4} < 15$$

(3)

Question 8 continued

(Total for Question 8 is 5 marks)

Question 9 continued

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Question 9 continued

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Question 9 continued

(Total for Question 9 is 7 marks)

10. The curve C has equation

$$y = \frac{(x - k)^2}{\sqrt{x}} \quad x > 0$$

where k is a **positive** constant.

(a) Show that

$$\int_1^{16} \frac{(x - k)^2}{\sqrt{x}} \, dx = ak^2 + bk + \frac{2046}{5}$$

where a and b are integers to be found.

(5)

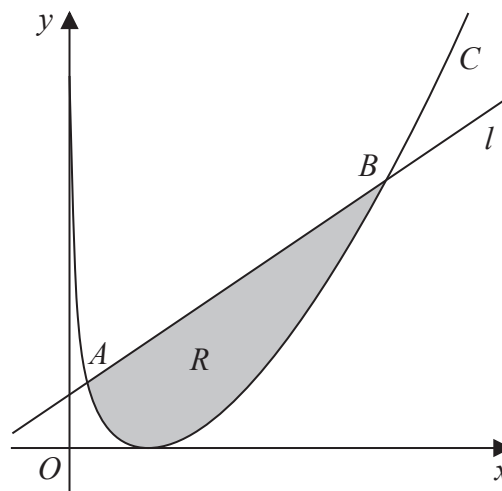


Figure 1

Figure 1 shows a sketch of the curve C and the line l .

Given that l intersects C at the point $A(1, 9)$ and at the point $B(16, q)$ where q is a constant,

(b) show that $k = 4$

(2)

The region R , shown shaded in Figure 1, is bounded by C and l

Using the answers to parts (a) and (b),

(c) find the area of region R

(3)

Question 10 continued

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Question 10 continued

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Question 10 continued

(Total for Question 10 is 10 marks)

11. A sequence u_1, u_2, u_3, \dots is defined by

$$u_{n+1} = b - au_n$$

$$u_1 = 3$$

where a and b are constants.

(a) Find, in terms of a and b ,

$$(i) \quad u_2$$
$$(ii) \quad u_3$$

(2)

Given

- $\sum_{n=1}^3 u_n = 153$

- $b = a + 9$

(b) show that

$$a^2 - 5a - 66 = 0$$

(3)

(c) Hence find the larger possible value of u_2

(3)

Question 11 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 11 continued

(Total for Question 11 is 8 marks)

TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information

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Centre Number					Candidate Number				
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Pearson Edexcel International Advanced Level

Friday 13 October 2023

Afternoon (Time: 1 hour 30 minutes) **Paper reference** **WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

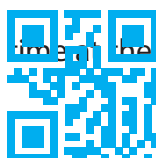
- Use **black** ink or ball-point pen.
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- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
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– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.



Turn over ►

1. Given that a, b and c are integers greater than 0 such that

- $c = 3a + 1$
- $a + b + c = 15$

prove, by exhaustion, that the product abc is always a multiple of 4

You may use the table below to illustrate your answer.

(3)

You may not need to use all rows of this table.

[illegible][illegible]

Question 1 continued

(Total for Question 1 is 3 marks)

2. A sequence u_1, u_2, u_3, \dots is defined by

$$u_1 = 3$$

$$u_{n+1} = 2 - \frac{4}{u_n}$$

(a) Find the value of u_2 , the value of u_3 and the value of u_4

(3)

(b) Find the value of

$$\sum_{r=1}^{100} u_r$$

(2)

Question 2 continued

(Total for Question 2 is 5 marks)

3. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

- (a) Solve, for $0 < \theta \leq 360^\circ$ the equation

$$2 \tan \theta + 3 \sin \theta = 0$$

giving your answers, as appropriate, to one decimal place.

(5)

- (b) Hence, or otherwise, find the smallest positive solution of

$$2 \tan(2x + 40^\circ) + 3 \sin(2x + 40^\circ) = 0$$

giving your answer to one decimal place.

(2)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 3 continued

(Total for Question 3 is 7 marks)

4.

In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

$$f(x) = 4x^3 + ax^2 - 29x + b$$

where a and b are constants.

Given that $(2x + 1)$ is a factor of $f(x)$,

(a) show that

$$a + 4b = -56 \tag{2}$$

Given also that when $f(x)$ is divided by $(x - 2)$ the remainder is -25

(b) find a second simplified equation linking a and b . (2)

(c) Hence, using algebra and showing your working,

(i) find the value of a and the value of b ,

(ii) fully factorise $f(x)$.

Question 4 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 4 continued

[illegible]

Question 4 continued

(Total for Question 4 is 9 marks)

5.

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

(i) Solve

$$3^a = 70$$

giving the answer to 3 decimal places.

(2)

(ii) Find the exact value of b such that

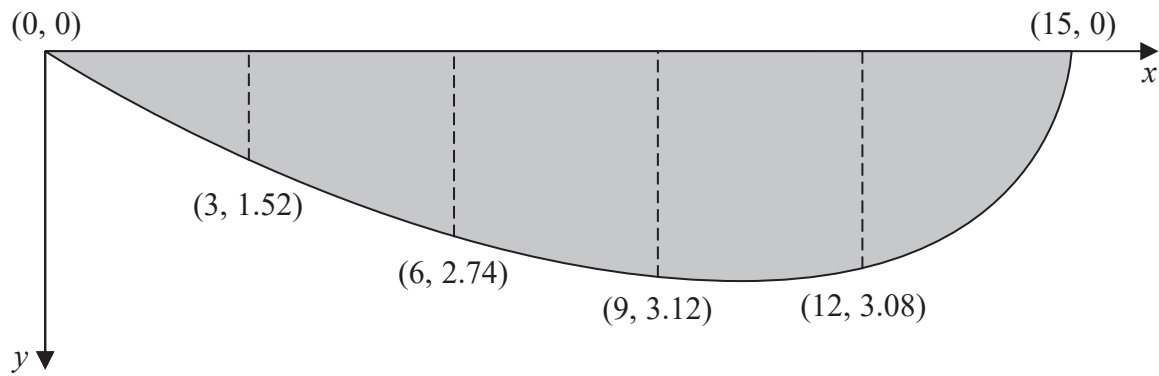
$$4 + 3 \log_3 b = \log_3 5b$$

(4)

Question 5 continued

(Total for Question 5 is 6 marks)

6.

**Figure 1**

A river is being studied.

At one particular place, the river is 15 m wide.

The depth, y metres, of the river is measured at a point x metres from one side of the river.

Figure 1 shows a plot of the cross-section of the river and the coordinate values (x, y)

- (a) Use the trapezium rule with all the y values given in Figure 1 to estimate the cross-sectional area of the river. (3)

The water in the river is modelled as flowing at a constant speed of 1.5 m s^{-1} across the whole of the cross-section.

- (b) Use the model and the answer to part (a) to estimate the volume of water flowing through this section of the river each minute, giving your answer in m^3 to 2 significant figures. (2)

Assuming the model,

- (c) state, giving a reason for your answer, whether your answer for part (b) is an overestimate or an underestimate of the true volume of water flowing through this section of the river each minute. (1)

Question 6 continued

(Total for Question 6 is 6 marks)

7.

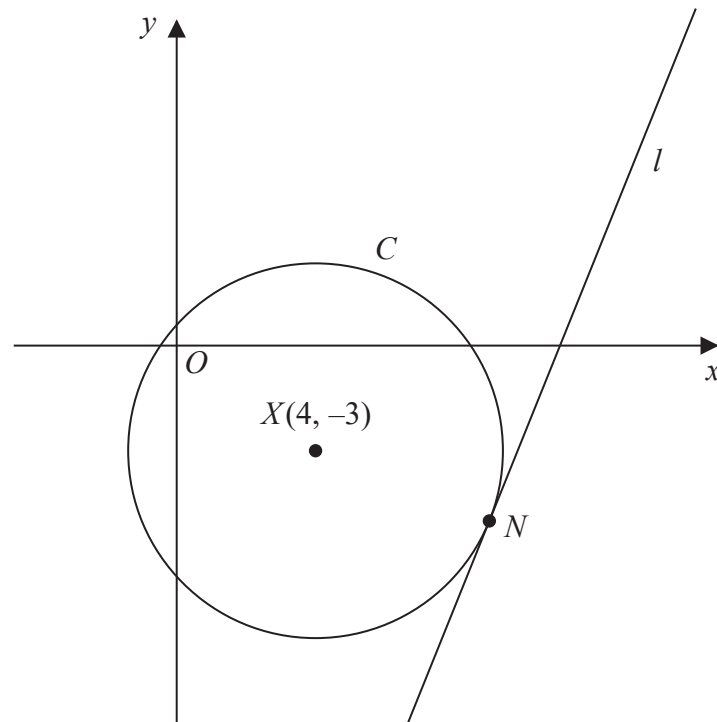


Figure 2

Figure 2 shows a sketch of

- the circle C with centre $X(4, -3)$
- the line l with equation $y = \frac{5}{2}x - \frac{55}{2}$

Given that l is the tangent to C at the point N ,

(a) show that an equation for the straight line passing through X and N is

$$2x + 5y + 7 = 0 \quad (3)$$

(b) Hence find

- the coordinates of N ,
- an equation for C .

(5)

Question 7 continued

[illegible]

Question 7 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 7 continued

(Total for Question 7 is 8 marks)

8. In a large theatre there are n rows of seats, where n is a constant.

The number of seats in the first row is a , where a is a constant.

In each subsequent row there are 4 more seats than in the previous row so that

- in the 2nd row there are $(a + 4)$ seats
- in the 3rd row there are $(a + 8)$ seats
- the number of seats in each row form an **arithmetic** sequence

Given that the **total** number of seats in the first 10 rows is 360

(a) find the value of a . (2)

Given also that the total number of seats in the n rows is 2146

(b) show that

$$n^2 + 8n - 1073 = 0 \quad (2)$$

(c) Hence

- state the number of rows of seats in the theatre,
- find the maximum number of seats in any one row.

(3)

Question 8 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 8 continued

[illegible]

Question 8 continued

(Total for Question 8 is 7 marks)

9.

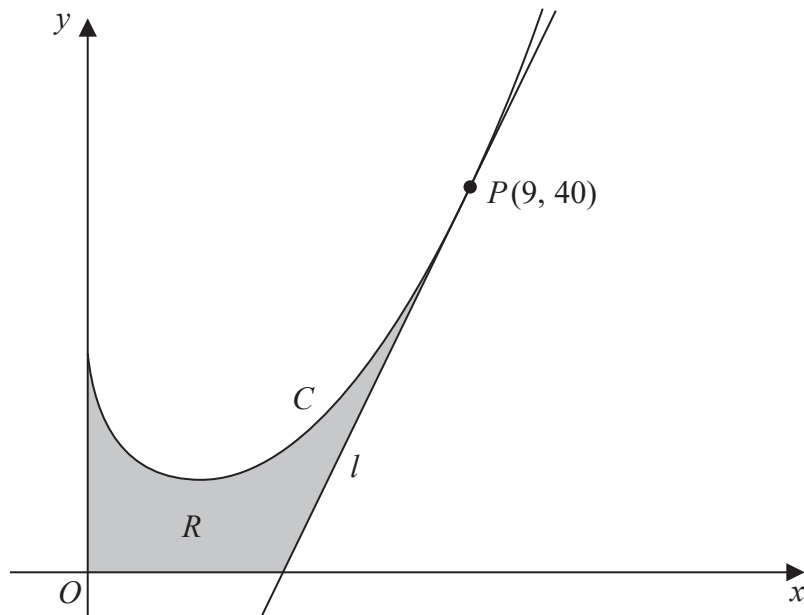


Figure 3

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

Figure 3 shows a sketch of part of the curve C with equation

$$y = \frac{2}{3}x^2 - 9\sqrt{x} + 13 \quad x \geq 0$$

(a) Find, using calculus, the range of values of x for which y is increasing.

(4)

The point P lies on C and has coordinates $(9, 40)$.

The line l is the tangent to C at the point P .

The finite region R , shown shaded in Figure 3, is bounded by the curve C , the line l , the x -axis and the y -axis.

(b) Find, using calculus, the exact area of R .

(8)

Question 9 continued

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Question 9 continued

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Question 9 continued

(Total for Question 9 is 12 marks)

10. (i) (a) Find, in ascending powers of x , the 2nd, 3rd and 5th terms of the binomial expansion of

$$(3 + 2x)^6 \tag{3}$$

For a particular value of x , these three terms form consecutive terms in a geometric series.

(b) Find this value of x . (3)

(ii) In a **different** geometric series,

- the first term is $\sin^2 \theta$
- the common ratio is $2 \cos \theta$
- the sum to infinity is $\frac{8}{5}$

(a) Show that

$$5 \cos^2 \theta - 16 \cos \theta + 3 = 0 \quad (3)$$

(b) Hence find the exact value of the 2nd term in the series. (3)

Question 10 continued

[illegible]

Question 10 continued

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Question 10 continued

[illegible]

Question 10 continued

(Total for Question 10 is 12 marks)

TOTAL FOR PAPER IS 75 MARKS

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Pearson Edexcel International Advanced Level

Tuesday 16 January 2024

Afternoon (Time: 1 hour 30 minutes) **Paper reference** **WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

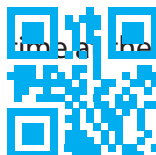
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Advice

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- Try to answer every question.
- Check your answers if you have time at the end.



Turn over ►

1. $f(x) = ax^3 + 3x^2 - 8x + 2$ where a is a constant

Given that when $f(x)$ is divided by $(x - 2)$ the remainder is 3, find the value of a .

(3)

Question 1 continued

(Total for Question 1 is 3 marks)

2. Find the coefficient of the term in x^7 of the binomial expansion of

$$\left(\frac{3}{8} + 4x\right)^{12}$$

giving your answer in simplest form.

(3)

Question 2 continued

(Total for Question 2 is 3 marks)

3. The circle C

- has centre $A(3, 5)$
- passes through the point $B(8, -7)$

(a) Find an equation for C .

(3)

The points M and N lie on C such that MN is a chord of C .

Given that MN

- lies above the x -axis
- is parallel to the x -axis
- has length $4\sqrt{22}$

(b) find an equation for the line passing through points M and N .

(3)

Question 3 continued

(Total for Question 3 is 6 marks)

4. (a) Sketch the curve with equation

$$y = a^{-x} + 4$$

where a is a constant and $a > 1$

On your sketch show

- the coordinates of the point of intersection of the curve with the y -axis
- the equation of the asymptote to the curve.

(3)

x	-4	-1.5	1	3.5	6	8.5
y	13	6.280	4.577	4.146	4.037	4.009

The table above shows corresponding values of x and y for $y = 3^{-\frac{1}{2}x} + 4$

The values of y are given to four significant figures, as appropriate.

Using the trapezium rule with all the values of y in the table,

(b) find an approximate value for

$$\int_{-4}^{8.5} \left(3^{-\frac{1}{2}x} + 4 \right) dx$$

giving your answer to two significant figures.

(3)

(c) Using the answer to part (b), find an approximate value for

(i) $\int_{-4}^{8.5} \left(3^{-\frac{1}{2}x} \right) dx$

(ii) $\int_{-4}^{8.5} \left(3^{-\frac{1}{2}x} + 4 \right) dx + \int_{-8.5}^4 \left(3^{\frac{1}{2}x} + 4 \right) dx$

(3)

Question 4 continued

Question 4 continued

[illegible]

Question 4 continued

(Total for Question 4 is 9 marks)

5. (i) Find the value of

$$\sum_{r=1}^{\infty} 6 \times (0.25)^r$$

(3)

(ii) A sequence u_1, u_2, u_3, \dots is defined by

$$\begin{aligned} u_1 &= 3 \\ u_{n+1} &= \frac{u_n - 3}{u_n - 2} \quad n \in \mathbb{N} \end{aligned}$$

(a) Show that this sequence is periodic.

(2)

(b) State the order of this sequence.

(1)

(c) Hence find

$$\sum_{n=1}^{70} u_n$$

(2)

Question 5 continued

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Question 5 continued

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Question 5 continued

(Total for Question 5 is 8 marks)

6. (a) Given that

$$2 \log_4(x+3) + \log_4 x = \log_4(4x+2) + \frac{1}{2}$$

show that

$$x^3 + 6x^2 + x - 4 = 0 \quad (4)$$

(b) Given also that -1 is a root of the equation

$$x^3 + 6x^2 + x - 4 = 0$$

(i) use algebra to find the other two roots of the equation. (3)

(ii) Hence solve

$$2 \log_4(x+3) + \log_4 x = \log_4(4x+2) + \frac{1}{2} \quad (1)$$

Question 6 continued

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Question 6 continued

(Total for Question 6 is 8 marks)

7. Wheat is grown on a farm.

- In year 1, the farm produced 300 tonnes of wheat.
- In year 12, the farm is predicted to produce 4 000 tonnes of wheat.

Model *A* assumes that the amount of wheat produced on the farm will increase by the same amount each year.

- (a) Using model *A*, find the amount of wheat produced on the farm in year 4. Give your answer to the nearest 10 tonnes.

(3)

Model *B* assumes that the amount of wheat produced on the farm will increase by the same percentage each year.

- (b) Using model *B*, find the amount of wheat produced on the farm in year 2. Give your answer to the nearest 10 tonnes.

(3)

- (c) Calculate, according to the two models, the difference between the total amounts of wheat predicted to be produced on the farm from year 1 to year 12 inclusive. Give your answer to the nearest 10 tonnes.

(3)

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Question 7 continued

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Question 7 continued

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Question 7 continued

(Total for Question 7 is 9 marks)

8. (i) Use a counter example to show that the following statement is **false**

“ $n^2 + 3n + 1$ is prime for all $n \in \mathbb{N}$ ”

(2)

(ii) Use algebra to prove by exhaustion that for all $n \in \mathbb{N}$

$n^2 - 2$ is **not** a multiple of 4”

(4)

Question 8 continued

(Total for Question 8 is 6 marks)

9. In this question you must show detailed reasoning.

Solutions relying entirely on calculator technology are not acceptable.

(i) Solve, for $0 \leq x < 360^\circ$, the equation

$$\sin x \tan x = 5$$

giving your answers to one decimal place.

(6)

(ii)

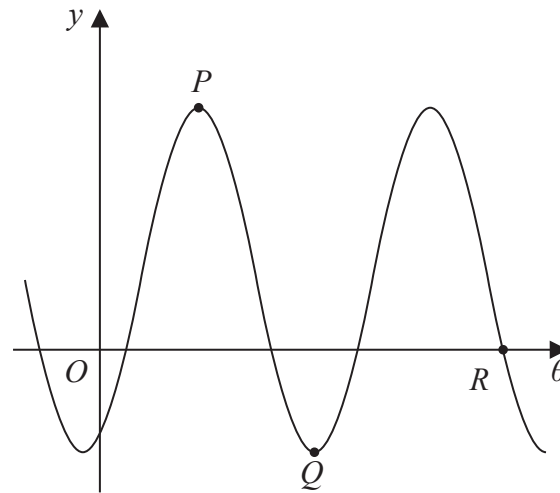


Figure 1

Figure 1 shows a sketch of part of the curve with equation

$$y = A \sin \left(2\theta - \frac{3\pi}{8} \right) + 2$$

where A is a constant and θ is measured in radians.

The points P , Q and R lie on the curve and are shown in Figure 1.

Given that the y coordinate of P is 7

(a) state the value of A , (1)

(b) find the exact coordinates of Q , (3)

(c) find the value of θ at R , giving your answer to 3 significant figures. (4)

Question 9 continued

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Question 9 continued

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Question 9 continued

(Total for Question 9 is 14 marks)

10.

In this question you must show detailed reasoning.

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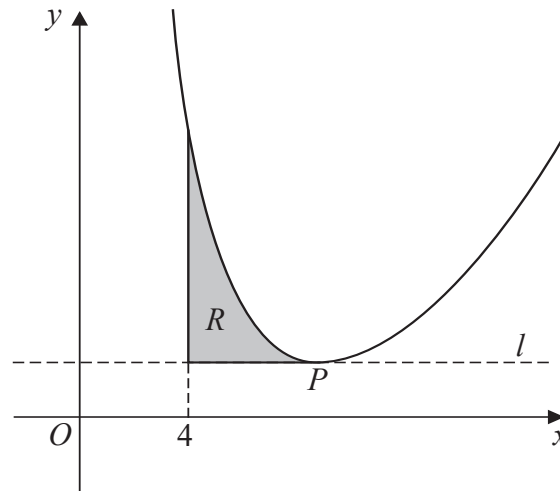


Figure 2

Figure 2 shows a sketch of the curve with equation

$$y = \frac{1}{2}x^2 + \frac{1458}{\sqrt{x^3}} - 74 \quad x > 0$$

The point P is the only stationary point on the curve.

- (a) Use calculus to show that the x coordinate of P is 9

(4)

The line l passes through the point P and is parallel to the x -axis.

The region R , shown shaded in Figure 2, is bounded by the curve, the line l and the line with equation $x = 4$

- (b) Use algebraic integration to find the exact area of R .

(5)

Question 10 continued

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Question 10 continued

(Total for Question 10 is 9 marks)

TOTAL FOR PAPER IS 75 MARKS

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Pearson Edexcel International Advanced Level

Tuesday 14 May 2024

Morning (Time: 1 hour 30 minutes)

Paper reference **WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

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Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.



1. (a) Find the first four terms, in ascending powers of x , of the binomial expansion of

$$\left(1 - \frac{1}{6}x\right)^9$$

giving each term in simplest form.

(3)

- (b) Hence find the coefficient of x^3 in the expansion of

$$(10x + 3)\left(1 - \frac{1}{6}x\right)^9$$

giving the answer in simplest form.

(2)

Question 1 continued

(Total for Question 1 is 5 marks)

2. In this question you must show all stages of your working. Solutions relying entirely on calculator technology are not acceptable.

In an arithmetic series,

- the sixth term is 2
- the sum of the first ten terms is -80

For this series,

- (a) find the value of the first term and the value of the common difference. (4)

- (b) Hence find the smallest value of n for which

$$S_n > 8000 \quad (3)$$

Question 2 continued

(Total for Question 2 is 7 marks)

3. In this question you must show all stages of your working. Solutions relying entirely on calculator technology are not acceptable.

(i) Using the laws of logarithms, solve

$$2\log_2(2-x) = 4 + \log_2(x+10) \quad (5)$$

(ii) Find the value of

$$\log_{\sqrt{a}} a^6$$

where a is a positive constant greater than 1

(1)

Question 3 continued

(Total for Question 3 is 6 marks)

4.

$$f(x) = (x - 2)(2x^2 + 5x + k) + 21$$

where k is a constant.

(a) State the remainder when $f(x)$ is divided by $(x - 2)$

(1)

Given that $(2x - 1)$ is a factor of $f(x)$

(b) show that $k = 11$

(2)

(c) Hence

(i) fully factorise $f(x)$,

(ii) find the number of real solutions of the equation

$$f(x) = 0$$

giving a reason for your answer.

(5)

Question 4 continued

[illegible]

Question 4 continued

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Question 4 continued

(Total for Question 4 is 8 marks)

5.

In this question you must show detailed reasoning.

(a) Given that x and y are positive numbers such that

$$(x-y)^3 > x^3 - y^3$$

prove that

$$y > x$$

(4)

(b) Using a counter example, show that the result in part (a) is not true for all real numbers.

(2)

Question 5 continued

(Total for Question 5 is 6 marks)

6. (a) Sketch the curve with equation

$$y = a^x + 4$$

where a is a positive constant greater than 1

On your sketch, show

- the coordinates of the point of intersection of the curve with the y -axis
- the equation of the asymptote of the curve

(3)

x	2	2.3	2.6	2.9	3.2	3.5
y	0	0.3246	0.8629	1.6643	2.7896	4.3137

The table shows corresponding values of x and y for

$$y = 2^x - 2x$$

with the values of y given to 4 decimal places as appropriate.

Using the trapezium rule with all the values of y in the given table,

(b) obtain an estimate for $\int_2^{3.5} (2^x - 2x) \, dx$, giving your answer to 2 decimal places.

(3)

(c) Using your answer to part (b) and making your method clear, estimate

(i) $\int_2^{3.5} (2^x + 2x) \, dx$

(ii) $\int_2^{3.5} (2^{x+1} - 4x) \, dx$

(3)

Question 6 continued

Question 6 continued

[illegible]

Question 6 continued

(Total for Question 6 is 9 marks)

7. The circle C_1 has equation

$$x^2 + y^2 + 8x - 10y = 29$$

- (a) (i) Find the coordinates of the centre of C_1
- (ii) Find the exact value of the radius of C_1

(3)

In part (b) you must show detailed reasoning.

The circle C_2 has equation

$$(x-5)^2 + (y+8)^2 = 52$$

- (b) Prove that the circles C_1 and C_2 neither touch nor intersect.

(3)

Question 7 continued

[illegible]

Question 7 continued

[illegible]

Question 7 continued

(Total for Question 7 is 6 marks)

8. In this question you must show all stages of your working. Solutions relying entirely on calculator technology are not acceptable.

- (i) Solve, for $0 < x \leq \pi$, the equation

$$5 \sin x \tan x + 13 = \cos x$$

giving your answer in radians to 3 significant figures.

(5)

- (ii) The temperature inside a greenhouse is monitored on one particular day.

The temperature, $H^{\circ}\text{C}$, inside the greenhouse, t hours after midnight, is modelled by the equation

$$H = 10 + 12 \sin(kt + 18)^\circ \quad 0 \leq t < 24$$

where k is a constant.

Use the equation of the model to answer parts (a) to (c).

Given that

- the temperature inside the greenhouse was 20°C at 6 am
- $0 < k < 20$

- (a) find all possible values for k , giving each answer to 2 decimal places.

(4)

Given further that $0 < k < 10$

- (b) find the maximum temperature inside the greenhouse,

(1)

- (c) find the time of day at which this maximum temperature occurs.

Give your answer to the nearest minute.

(2)

Question 8 continued

Question 8 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 8 continued

(Total for Question 8 is 12 marks)

9.

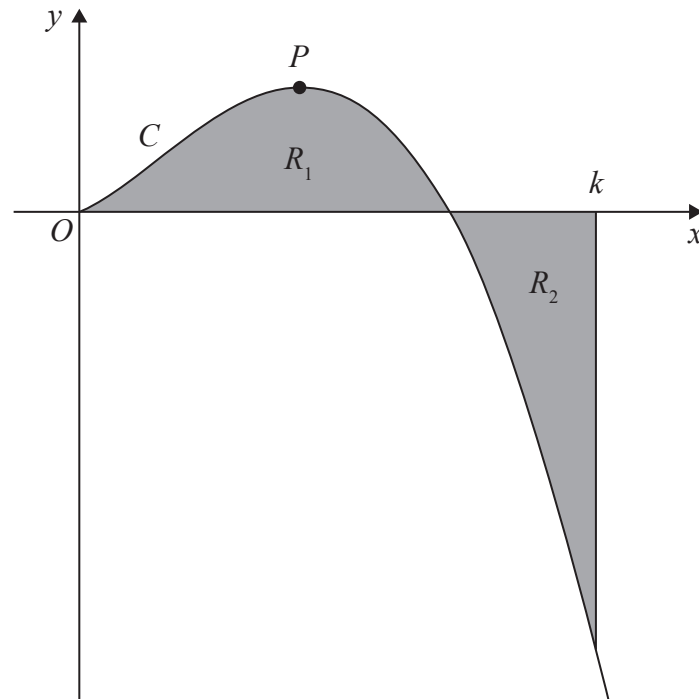
**Figure 1**

Figure 1 is a sketch of the curve C with equation

$$y = 2x^{\frac{3}{2}}(4 - x) \quad x \geq 0$$

The point P is the stationary point of C .

(a) Find, using calculus, the x coordinate of P .

(4)

The region R_1 , shown shaded in Figure 1, is bounded by C and the x -axis.

The region R_2 , also shown shaded in Figure 1, is bounded by C , the x -axis and the line with equation $x = k$, where k is a constant.

Given that the area of R_1 is equal to the area of R_2

(b) find, using calculus, the exact value of k .

(4)

Question 9 continued

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Question 9 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 9 continued

(Total for Question 9 is 8 marks)

10.

In this question you must show all stages of your working. Solutions relying entirely on calculator technology are not acceptable.

The number of dormice and the number of voles on an island are being monitored.

Initially there are 2000 dormice on the island.

A model predicts that the number of dormice will increase by 3% each year, so that the numbers of dormice on the island at the end of each year form a geometric sequence.

- (a) Find, according to the model, the number of dormice on the island 6 years after monitoring began. Give your answer to 3 significant figures.

(2)

The number of voles on the island is being monitored over the same period of time.

Given that

- 4 years after monitoring began there were 3690 voles on the island
- 7 years after monitoring began there were 3470 voles on the island
- the number of voles on the island at the end of each year is modelled as a geometric sequence

- (b) find the equation of this model in the form

$$N = ab^t$$

where N is the number of voles, t years after monitoring began and a and b are constants. Give the value of a and the value of b to 2 significant figures.

(3)

When $t = T$, the number of dormice on the island is equal to the number of voles on the island.

- (c) Find, according to the models, the value of T , giving your answer to one decimal place.

(3)

Question 10 continued

Question 10 continued

(Total for Question 10 is 8 marks)

TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information

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Pearson Edexcel International Advanced Level

Tuesday 15 October 2024

Morning (Time: 1 hour 30 minutes) **Paper reference WMA12/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Pure Mathematics P2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 11 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.



Turn over ►

1. A continuous curve has equation $y = f(x)$.

A table of values of x and y for $y = f(x)$ is shown below.

x	0.5	1.75	3	4.25	5.5
y	3.479	6.101	7.448	6.823	5.182

Using the trapezium rule with all the values of y in the given table,

- (a) find an estimate for

$$\int_{0.5}^{5.5} f(x) \, dx$$

giving your answer to one decimal place.

(3)

- (b) Using your answer to part (a) and making your method clear, estimate

$$\int_{0.5}^{5.5} (f(x) + 4x) \, dx$$

(2)

Question 1 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(Total for Question 1 is 5 marks)

2. A sequence of numbers u_1, u_2, u_3, \dots is defined by

$$u_1 = 7$$

$$u_{n+1} = (-1)^n u_n + k$$

where k is a constant.

(a) Show that $u_5 = 7$

(3)

Given that $\sum_{r=1}^4 u_r = 30$

(b) find the value of k .

(2)

(c) Hence find the value of $\sum_{r=1}^{150} u_r$

(2)

Question 2 continued

(Total for Question 2 is 7 marks)

3.

$$f(x) = 2x^3 - x^2 + Ax + B$$

where A and B are integers.

Given that when $f(x)$ is divided by $(x + 3)$ the remainder is 55

(a) show that

$$3A - B = -118$$

(2)

Given also that $(2x - 5)$ is a factor of $f(x)$,

(b) find the value of A and the value of B .

(3)

(c) Hence find the quotient when $f(x)$ is divided by $(x - 7)$

(2)

Question 3 continued

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Question 3 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 3 continued

(Total for Question 3 is 7 marks)

4. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

The curve C has equation

$$y = 4x^{\frac{1}{2}} + 9x^{-\frac{1}{2}} + 3 \quad x > 0$$

- (a) Find $\frac{dy}{dx}$ giving each term in simplest form. (2)
- (b) Hence find the x coordinate of the stationary point of C . (2)
- (c) (i) Find $\frac{d^2y}{dx^2}$ giving each term in simplest form.
- (ii) Hence determine the nature of the stationary point of C , giving a reason for your answer. (2)
- (d) State the range of values of x for which y is decreasing. (1)

Question 4 continued

(Total for Question 4 is 7 marks)

5. (a) Find, in terms of a , the first 3 terms, in ascending powers of x , of the binomial expansion of

$$(2 + ax)^6$$

where a is a non-zero constant. Give each term in simplest form.

(3)

$$f(x) = \left(3 + \frac{1}{x}\right)^2 (2 + ax)^6$$

Given that the constant term in the expansion of $f(x)$ is 576

- (b) find the value of a .

(4)

Question 5 continued

(Total for Question 5 is 7 marks)

6.

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

Using the laws of logarithms, solve

$$\log_4(12 - 2x) = 2 + 2\log_4(x + 1)$$

(5)

Question 6 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(Total for Question 6 is 5 marks)

7. Jem pays money into a savings scheme, A , over a period of 300 months.

Jem pays £20 into scheme A in month 1, £20.50 in month 2, £21 in month 3 and so on, so that the amounts Jem pays each month form an arithmetic sequence.

- (a) Show that Jem pays £69.50 into scheme A in month 100 (1)
- (b) Find the **total** amount that Jem pays into scheme A over the period of 300 months. (2)

Kim pays money into a different savings scheme, B , over the same period of 300 months.

In a model, the amounts Kim pays into scheme B increase by the same percentage each month, so that the amounts Kim pays each month form a geometric sequence.

Given that Kim pays

- £20 into scheme B in month 1
 - £250 into scheme B in month 300
- (c) use the model to calculate, to the nearest £10, the difference between the total amount paid into scheme A and the total amount paid into scheme B over the period of 300 months.
- (3)**

Question 7 continued

Question 7 continued

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Question 7 continued

(Total for Question 7 is 6 marks)

8.

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

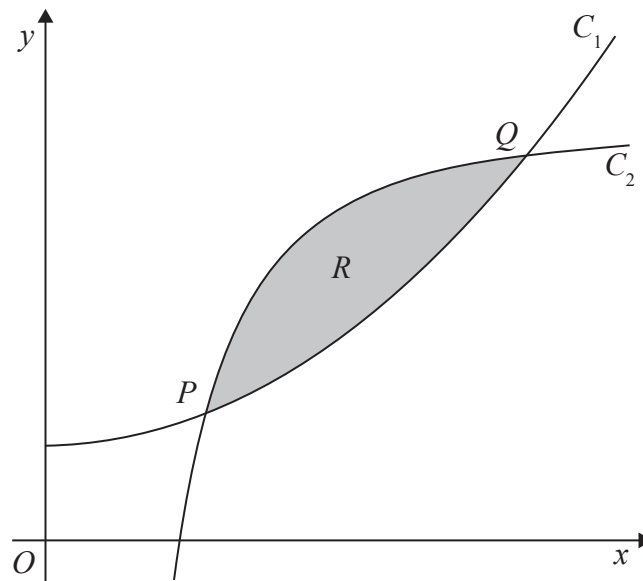


Figure 1

Figure 1 shows a sketch of part of the curve C_1 with equation

$$y = x^2 + 3 \quad x > 0$$

and part of the curve C_2 with equation

$$y = 13 - \frac{9}{x^2} \quad x > 0$$

The curves C_1 and C_2 intersect at the points P and Q as shown in Figure 1.

(a) Use algebra to find the x coordinate of P and the x coordinate of Q .

(4)

The finite region R , shown shaded in Figure 1, is bounded by C_1 and C_2

(b) Use algebraic integration to find the exact area of R .

(4)

Question 8 continued

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Question 8 continued

[illegible]

Question 8 continued

(Total for Question 8 is 8 marks)

9.

In this question you must show detailed reasoning.

Solutions relying entirely on calculator technology are not acceptable.

(a) Show that the equation

$$2 \tan \theta = 3 \cos \theta$$

can be written as

$$3 \sin^2 \theta + 2 \sin \theta - 3 = 0$$

(3)

(b) Hence solve, for $-\pi < x < \pi$, the equation

$$2 \tan\left(2x + \frac{\pi}{3}\right) = 3 \cos\left(2x + \frac{\pi}{3}\right)$$

giving your answers to 3 significant figures.

(4)

Question 9 continued

(Total for Question 9 is 7 marks)

10. The circle C has equation

$$x^2 + y^2 + 4x - 30y + 209 = 0$$

(a) Find

- (i) the coordinates of the centre of C ,
- (ii) the exact value of the radius of C .

(3)

The line L has equation $y = mx + 1$, where m is a constant.

Given that L is the tangent to C at the point P ,

(b) show that

$$2m^2 - 7m - 22 = 0$$

(3)

(c) Hence find the possible pairs of coordinates of P .

(4)

Question 10 continued

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Question 10 continued

[illegible]

Question 10 continued

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(Total for Question 10 is 10 marks)

11. (i) Prove by counter example that the statement

“If n is a prime number then $3^n + 2$ is also a prime number.”

is false.

(2)

(ii) Use proof by exhaustion to prove that if m is an integer that is **not** divisible by 3, then

$$m^2 - 1$$

is divisible by 3

(4)

Question 11 continued

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Question 11 continued

(Total for Question 11 is 6 marks)

TOTAL FOR PAPER IS 75 MARKS