Pearson Edexcel IAL (Further) Mathematics

Pure Mathematics 2

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Past Paper Collection



Last updated: January 21, 2025

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Please check the examination details below before entering your candidate information							
Candidate surname	Other names						
Pearson Edexcel International Advanced Level	re Number Candidate Number						
Tuesday 18 June	e 2019						
Morning (Time: 1 hour 30 minutes)	Paper Reference WMA12/01						
Mathematics							
International Advanced Su Pure Mathematics P2	bsidiary/Advanced Level						
You must have: Mathematical Formulae and Statistical	Tables (Lilac), calculator						

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

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- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
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 - use this as a guide as to how much time to spend on each question.

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Turn over ▶

Answer all questions. Write your answers in the spaces provided.

1. A sequence a_1, a_2, a_3, \dots is defined by

$$a_{n+1} = 4 - a_n$$
$$a_1 = 3$$

Find the value of

- (a) (i) a_2
 - (ii) *a*₁₀₇

(2)

(b) $\sum_{n=1}^{200} (2a_n - 1)$

(2)

	Leave blank
Question 1 continued	Oldrik
	01
	Q1
(Total 4 marks)	

2.	A circle	C has	equation

$$x^2 + y^2 + 4x - 10y - 21 = 0$$

Find

- (a) (i) the coordinates of the centre of C,
 - (ii) the exact value of the radius of C.

(3)

The point P(5, 4) lies on C.

(b) Find the equation of the tangent to C at P, writing your answer in the form y = mx + c, where m and c are constants to be found.

(4)

Question 2 continued	Leave blank
(Total	Q2

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3. (i) Use algebra to prove that for all real values of x	
$\left(x-4\right)^{2}\geqslant2x-9$	(3)
(ii) Show that the following statement is untrue.	
$2^{n} + 1$ is a prime number for all values of $n, n \in \mathbb{N}$	(1)

euestion 3 continued	

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blank

4.	(a)	Find the f	irst four	terms, i	n ascending	powers of <i>x</i>	, of the	binomial	expansion of

$$\left(2-\frac{1}{4}x\right)^6$$

(4)

(b) Given that x is small, so terms in x^4 and higher powers of x may be ignored, show

$$\left(2 - \frac{1}{4}x\right)^6 + \left(2 + \frac{1}{4}x\right)^6 = a + bx^2$$

where a and b are constants to be found.

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Question 4 continued	Dialik
	Q4
(Total 7 marks)	

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5.	A company	i makeca	narticular	tune	of watch
J.	A company	makes a	particular	type	or water.

The annual profit made by the company from sales of these watches is modelled by the equation

$$P = 12x - x^{\frac{3}{2}} - 120$$

where P is the annual profit measured in thousands of pounds and £x is the selling price of the watch.

According to this model,

(a)	find,	using	calculus,	the	maximum	possible	annual	profit

(6)

(b)	Justify, also	using	calculus,	that th	e profit	you	have	found	is a	maximum
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(2)

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Question 5 continued	Ula.
	Q5
(Total 8 marks)	

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6.	$f(x) = kx^3 - 15x^2 - 32x - 12$ where k is a constant		blank
	Given $(x-3)$ is a factor of $f(x)$,		
	(a) show that $k = 9$	(2)	
	(b) Using algebra and showing each step of your working, fully factorise $f(x)$.	(4)	
	(c) Solve, for $0 \le \theta < 360^{\circ}$, the equation		
	$9\cos^{3}\theta - 15\cos^{2}\theta - 32\cos\theta - 12 = 0$		
	giving your answers to one decimal place.	(2)	

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Question 6 continued	

Question 6 continued	bla

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Question 6 continued	Diank
	Q6
(Total 8 marks)	

7.	Kim starts working for a company.	blank
	• In year 1 her annual salary will be £16200	
	• In year 10 her annual salary is predicted to be £31 500	
	Model A assumes that her annual salary will increase by the same amount each year.	
	(a) According to model A, determine Kim's annual salary in year 2. (3)	
	Model B assumes that her annual salary will increase by the same percentage each year.	
	(b) According to model B, determine Kim's annual salary in year 2. Give your answer to the nearest £10(3)	
	(c) Calculate, according to the two models, the difference between the total amounts that Kim is predicted to earn from year 1 to year 10 inclusive. Give your answer to the nearest £10	
	(3)	
		1

Question 7 continued	Leave blank
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Question 7 continued	Leave blank

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Question 7 continued	Diank
	Q 7
(Total 9 marks)	

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8.	(i)	Find the exact solution of the equation
		$8^{2x+1} = 6$
		giving your answer in the form $a + b \log_2 3$, where a and b are constants to be found. (4)
	(ii)	Using the laws of logarithms, solve
		$\log_5(7 - 2y) = 2\log_5(y + 1) - 1$ (5)
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Question 8 continued	bla

Question 8 continued	Leave blank

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Question 8 continued	Dialik
	06
	Q8
(Total 9 marks)	

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9. (a) Show that the equation	blank
$\cos\theta - 1 = 4\sin\theta\tan\theta$	
can be written in the form	
$5\cos^2\theta - \cos\theta - 4 = 0$	
au	
(b) Hence solve, for $0 \le x < \frac{\pi}{2}$	
$\cos 2x - 1 = 4\sin 2x \tan 2x$	
giving your answers, where appropriate, to 2 decimal places.	
(4)	

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Question 9 continued	

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Question 9 continued	

Question 9 continued		Le
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	<u>C</u>	Q 9

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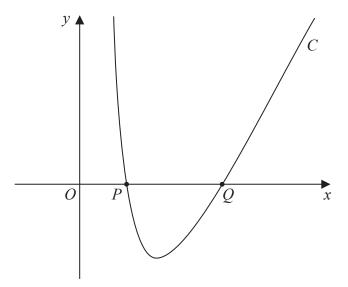


Figure 1

Figure 1 shows a sketch of part of the curve C with equation y = f(x) where

$$f(x) = \frac{36}{x^2} + 2x - 13 \qquad x > 0$$

Using calculus,

(a) find the range of values of x for which f(x) is increasing,

(4)

(b) show that
$$\int_{2}^{9} \left(\frac{36}{x^2} + 2x - 13 \right) dx = 0$$

(4)

(3)

The point P(2, 0) and the point Q(6, 0) lie on C.

Given
$$\int_{2}^{6} \left(\frac{36}{x^2} + 2x - 13 \right) dx = -8$$

(c) (i) state the value of
$$\int_{6}^{9} \left(\frac{36}{x^2} + 2x - 13 \right) dx$$

(ii) find the value of the constant k such that $\int_{2}^{6} \left(\frac{36}{x^{2}} + 2x + k \right) dx = 0$	
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Question 10 continued	

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Question 10 continued	Olank
	Q10
(Total 11 marks)	
TOTAL FOR PAPER IS 75 MARKS	

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Wednesday 6 No	ovember 2019	
Morning (Time: 1 hour 30 minutes)	Paper Reference WMA12/01	
Mathematics		
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1. A curve C has equation $y = 2x^2(x - 5)$		
(a) Find, using calculus, the x coordinates of the stationary points of C .		
	(4)	
(b) Hence find the values of x for which y is increasing.	(2)	
	(2)	

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Question 1 continued	Dialik
	Q1
(Total 6 marks)	

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2.	The adult population of a town at the start of 2019 is 25 000	blaı
	A model predicts that the adult population will increase by 2% each year, so that the number of adults in the population at the start of each year following 2019 will form a geometric sequence.	
	(a) Find, according to the model, the adult population of the town at the start of 2032 (3)	
	It is also modelled that every member of the adult population gives £5 to local charity at the start of each year.	
	(b) Find, according to these models, the total amount of money that would be given to local charity by the adult population of the town from 2019 to 2032 inclusive. Give your answer to the nearest £1000	
	(3)	

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Question 2 continued	
	Q2
(Total 6 marks)	

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hl	ank	

3.	(a) Find the first 4 terms, in ascending powers of	of x , in the binomial expansion of
	$\left(1+\frac{x}{4}\right)^{12}$	

giving each coefficient in its simplest form.

(3)

(b) Find the term independent of x in the expansion of

$$\left(\frac{x^2+8}{x^5}\right)\left(1+\frac{x}{4}\right)^{12}$$

(3)

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Question 3 continued	biank
	Q3
(Total 6 marks)	
(Total o mai ks)	

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4.	$f(x) = (x - 3)(3x^2 + x + a) - 35$ where a is a constant	
	(a) State the remainder when $f(x)$ is divided by $(x-3)$.	(1)
	Given $(3x - 2)$ is a factor of $f(x)$,	
	(b) show that $a = -17$	(2)
	(c) Using algebra and showing each step of your working, fully factorise $f(x)$.	(5)

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Question 4 continued	

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Question 4 continued	

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Question 4 continued	biank
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	Q4
(Total 8 marks)	

5. (a) Given 0 < a < 1, sketch the curve with equation

$$y = a^x$$

showing the coordinates of the point at which the curve crosses the y-axis.

(2)

х	2	2.5	3	3.5	4
У	4.25	6.427	9.125	12.34	16.06

The table above shows corresponding values of x and y for $y = x^2 + \left(\frac{1}{2}\right)^x$

The values of y are given to 4 significant figures as appropriate.

Using the trapezium rule with all the values of y in the given table,

(b) obtain an estimate for
$$\int_{2}^{4} \left(x^{2} + \left(\frac{1}{2} \right)^{x} \right) dx$$
 (3)

Using your answer to part (b) and making your method clear, estimate

(c)
$$\int_{2}^{4} \left(x(x-3) + \left(\frac{1}{2}\right)^{x} \right) \mathrm{d}x$$
 (2)

Question 5 continued	Lea blar
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Question 5 continued	biank
	Q5
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(Total 7 marks)	

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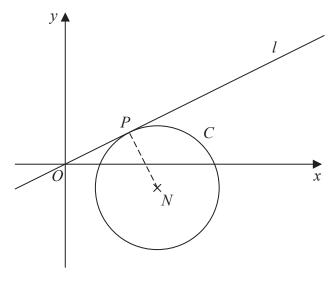


Figure 1

Figure 1 shows a sketch of a circle C with centre N(4, -1).

The line *l* with equation $y = \frac{1}{2}x$ is a tangent to *C* at the point *P*.

Find

- (a) the equation of line PN in the form y = mx + c, where m and c are constants, (2)
- (b) the equation of C.

(5)

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Question 6 continued	

Question 6 continued	Leav

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7 .	Given	$\log h = k$	find i	n simplest fo	orm in terms	of k
/ •	OIVCII	$\log_a v = \kappa$	111114, 1	n simpiest ic		or n ,

(i)
$$\log_a \left(\frac{\sqrt{a}}{b} \right)$$

(2)

(ii)
$$\frac{\log_a a^2 b}{\log_a b^3}$$

(2)

$$(iii) \sum_{n=1}^{50} (k + \log_a b^n)$$

(3)

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Question 7 continued	John
	Q7
(Total 7 marks)	

8. Solutions relying on calculator technology are not acceptable in this question.



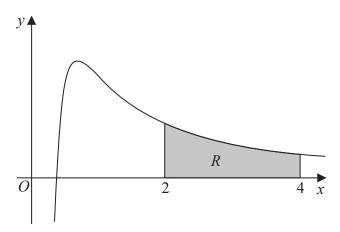


Figure 2

Figure 2 shows a sketch of part of a curve with equation

$$y = \frac{8\sqrt{x} - 5}{2x^2} \qquad x > 0$$

The region R, shown shaded in Figure 2, is bounded by the curve, the line with equation x = 2, the x-axis and the line with equation x = 4

Find the exact area of R.

(5)

(ii) Find the value of the constant k such that

$$\int_{-3}^{6} \left(\frac{1}{2} x^2 + k \right) \mathrm{d}x = 55$$

(4)

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Question 8 continued	

Question 8 continued	Leave blank

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Question 8 continued	blank
	Q8
(Total 9 marks)	
(Lower / marks)	

9.	Solutions based entirely on graphical or numerical methods are not acceptable in
	this question.

(i) Solve, for $0 \leqslant \theta < 180^{\circ}$, the equation

$$3\sin(2\theta-10^\circ)=1$$

giving your answers to one decimal place.

(4)

(ii) The first three terms of an arithmetic sequence are

$$\sin \alpha$$
, $\frac{1}{\tan \alpha}$ and $2\sin \alpha$

where α is a constant.

(a) Show that $2\cos\alpha = 3\sin^2\alpha$

(3)

Given that $\pi < \alpha < 2\pi$,

(b) find, showing all working, the value of α to 3 decimal places.

(5)

Question 9 continued	Leav blan

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Question 9 continued	
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Question 9 continued	Dialik
	Q9
(Total 12 marks)	

10.	The	curve	C	has	equation
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$$y = ax^3 - 3x^2 + 3x + b$$

where a and b are constants.

Given that

- the point (2, 5) lies on C
- the gradient of the curve at (2, 5) is 7
- (a) find the value of a and the value of b.

(4)

	(b)	Prove	that	C	has	no	turning	points
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(3)

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Question 10 continued	

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Question 10 continued	
	Q10
(Total 7 marks) TOTAL FOR PAPER IS 75 MARKS	

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Wednesday 1	5 Janu	ary 2020			
Morning (Time: 1 hour 30 minutes	s) Paper f	Reference WMA12/01			
Mathematics International Advanced Subsidiary/Advanced Level Pure Mathematics P2					
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Turn over ▶

1. The table below shows corresponding values of x and y for $y = \log_2(2x)$

The values of y are given to 2 decimal places as appropriate.

х	2	5	8	11	14
y	2	3.32	4	4.46	4.81

Using the trapezium rule with all the values of y in the given table,

(a) obtain an estimate for
$$\int_{2}^{14} \log_{2}(2x) dx$$
, giving your answer to one decimal place. (3)

Using your answer to part (a) and making your method clear, estimate

(b) (i)
$$\int_{2}^{14} \frac{\log_2(4x^2)}{5} dx$$

(ii)
$$\int_{2}^{14} \log_2\left(\frac{2}{x}\right) dx$$
 (4)

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Question 1 continued	Olalik
	Q1
(Total 7 marks)	

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2. One of the terms in the binomial expansion of $(3 + ax)^6$, where a is a	constant, is $540x^4$
(a) Find the possible values of a.	(4)
(b) Hence find the term independent of x in the expansion of	. ,
$\left(\frac{1}{81} + \frac{1}{x^6}\right)(3 + ax)^6$	(3)

P2_2020_01_QP

Question 2 continued	Leave
	Q2
(Total 7 marks)	

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3	•	10	(x)	=	$6x^{3}$ -	+ [$1/x^2$	+ .	4x	— !	12

(a) Use the factor theorem to show that (2x + 3) is a factor of f(x).

(2)

(b) Hence, using algebra, write f(x) as a product of three linear factors.

(4)

(c) Solve, for $\frac{\pi}{2} < \theta < \pi$, the equation

$$6\tan^3\theta + 17\tan^2\theta + 4\tan\theta - 12 = 0$$

giving your answers to 3 significant figures.

(2)

P2_2020_01_QP

Question 3 continued	Leave blank
	Q3
(Total 8 marks)	

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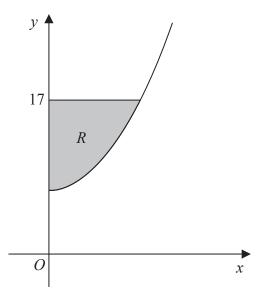


Figure 1

Figure 1 shows a sketch of the curve with equation

$$y = 2x^2 + 7$$

$$x \geqslant 0$$

The finite region R, shown shaded in Figure 1, is bounded by the curve, the y-axis and the line with equation y = 17

Find the exact area of R.

(6)

Question 4 continued	blar
	Q4
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In this question you must show all stages of your working.	blank
Solutions relying on calculator technology are not acceptable.	
A colony of bees is being studied.	
The number of bees in the colony at the start of the study was 30000	
Three years after the start of the study, the number of bees in the colony is 34000	
A model predicts that the number of bees in the colony will increase by $p\%$ each year, so that the number of bees in the colony at the end of each year of study forms a geometric sequence.	
Assuming the model,	
(a) find the value of p, giving your answer to 2 decimal places. (3)	
According to the model, at the end of N years of study the number of bees in the colony exceeds 75000	
(b) Find, showing all steps in your working, the smallest integer value of N . (5)	
	Solutions relying on calculator technology are not acceptable. A colony of bees is being studied. The number of bees in the colony at the start of the study was 30 000 Three years after the start of the study, the number of bees in the colony is 34 000 A model predicts that the number of bees in the colony will increase by p% each year, so that the number of bees in the colony at the end of each year of study forms a geometric sequence. Assuming the model, (a) find the value of p, giving your answer to 2 decimal places. (3) According to the model, at the end of N years of study the number of bees in the colony exceeds 75 000 (b) Find, showing all steps in your working, the smallest integer value of N.

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Question 5 continued	Dialik
	Q5
(Total 8 marks)	

6. The circle C has equation	
$x^2 + y^2 + 6x - 4y - 14 = 0$	
(a) Find	
(i) the coordinates of the centre of C ,	
(ii) the exact radius of C .	(2)
	(3)
The line with equation $y = k$, where k is a constant, is a tangent to C .	
(b) Find the possible values of k .	(2)
The line with equation $y = p$, where p is a negative constant, is a chord of C .	
Given that the length of this chord is 4 units,	
(c) find the value of p .	(3)

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Question 6 continued	
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Question 6 continued	Leave blank

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Question 6 continued	blank
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	Q6
(Total 8 marks)	

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7. (a) Show that the equation		blar
$8 \tan \theta = 3 \cos \theta$		
may be rewritten in the form		
$3\sin^2\theta + 8\sin\theta - 3 = 0$		
	(3)	
(b) Hence solve, for $0 \le x \le 90^{\circ}$, the equation		
$8\tan 2x = 3\cos 2x$		
giving your answers to 2 decimal places.		
	(4)	

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Question 7 continued	Dialik
	Q7
(Total 7 marks)	

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8.	(i)	An arithmetic series has first term a and common difference d .	blank
		Prove that the sum to n terms of this series is	
		$\frac{n}{2}\left\{2a+(n-1)d\right\} \tag{3}$	
	(ii)	A sequence $u_1, u_2, u_3,$ is given by	
		$u_n = 5n + 3(-1)^n$	
		Find the value of	
		(a) u_5	
		59	
		(b) $\sum_{n=1}^{59} u_n$ (3)	

Question 8 continued	Leav blan

Question 8 continued	Leave blank

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Question 8 continued	blank
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	Q8
(Total 7 marks)	
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9. (a) Sketch the curve with equation

$$y = 3 \times 4^x$$

showing the coordinates of any points of intersection with the coordinate axes.

(2)

The curve with equation $y = 6^{1-x}$ meets the curve with equation $y = 3 \times 4^x$ at the point P.

(b) Show that the x coordinate of P is $\frac{\log_{10} 2}{\log_{10} 24}$ (5)

Question 9 continued	Leave blank
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Question 9 continued	Leave blank

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Question 9 continued	Dialik
	Q9
(Total 7 marks)	

Leave blank

10.	A curve	c C has	equation
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$$y = 4x^3 - 9x + \frac{k}{x} \qquad x > 0$$

where k is a constant.

The point P with x coordinate $\frac{1}{2}$ lies on C.

Given that P is a stationary point of C,

(a) show that $k = -\frac{3}{2}$

(4)

(b) Determine the nature of the stationary point at P, justifying your answer.

(2)

The curve *C* has a second stationary point.

(c) Using algebra, find the x coordinate of this second stationary point.

(4)

Question 10 continued	Leav blanl

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Question 10 continued	
	010
	Q10
(Total 10 marks)	
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Wednesday 21 October 2020				
Morning (Time: 1 hour 30 minutes)	Paper Reference WMA12/01			
Mathematics International Advanced Subsidiary/Advanced Level Pure Mathematics P2				
You must have: Mathematical Formulae and Statistical Tables (Lilac), calculator Total Marks				

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

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- There are 9 questions in this question paper. The total mark for this paper is 75.
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1.	(a)	Find the first 4 terms,	in ascending powers	s of x , of the binomial expansion of	

 $\left(2-\frac{x}{4}\right)^{10}$

giving each term in its simplest form.

(4)

(b) Hence find the constant term in the series expansion of

$$\left(3 - \frac{1}{x}\right)^2 \left(2 - \frac{x}{4}\right)^{10}$$

(3)

Question 1 continued	blan

Question 1 continued	blan

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(Total 7 marks)	

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2.

$$y = \frac{2^x}{\sqrt{(5x^2 + 3)}}$$

(a) Complete the table below, giving the values of y to 3 decimal places.

x	-0.25	0	0.25	0.5	0.75
у	0.462		0.653		0.698

(1)

(b) Use the trapezium rule, with all the values of y from the completed table, to find an approximate value for

$$\int_{-0.25}^{0.75} \frac{2^x}{\sqrt{(5x^2+3)}} \, \mathrm{d}x$$

(3)

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Question 2 continued	blank
	Q2
(Total 4 marks)	

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3.	$f(x) = ax^3 - x^2 + bx + 4$	blar
	where a and b are constants.	
	When $f(x)$ is divided by $(x + 4)$, the remainder is -108	
	(a) Use the remainder theorem to show that	
	16a + b = 24 (2)	
	Given also that $(2x - 1)$ is a factor of $f(x)$,	
	(b) find the value of a and the value of b. (3)	
	(c) Find $f'(x)$. (1)	
	(d) Hence find the exact coordinates of the stationary points of the curve with equation $y = f(x)$.	
	(4)	
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The	e points P and Q have coordinates $(-11, 6)$ and $(-3, 12)$ respectively.	
Giv	wen that PQ is a diameter of the circle C ,	
(a)	(i) find the coordinates of the centre of C,	
	(ii) find the radius of C.	(4)
(b)	Hence find an equation of C.	(2)
(c)	Find an equation of the tangent to C at the point Q giving your answer in form $ax + by + c = 0$ where a , b and c are integers to be found.	the (3)

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Question 4 continued	

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Question 4 continued	

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Question 4 continued	
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(Total 9 marks)	

5.	Ben is saving for the deposit for a house over a period of 60 months.	bla
	Ben saves £100 in the first month and in each subsequent month, he saves £5 more than the previous month, so that he saves £105 in the second month, £110 in the third month, and so on, forming an arithmetic sequence.	
	(a) Find the amount Ben saves in the 40th month. (2)	
	(b) Find the total amount Ben saves over the 60-month period. (3)	
	Lina is also saving for a deposit for a house.	
	Lina saves £600 in the first month and in each subsequent month, she saves £10 less than the previous month, so that she saves £590 in the second month, £580 in the third month, and so on, forming an arithmetic sequence.	
	Given that, after n months, Lina will have saved exactly £18200 for her deposit,	
	(c) form an equation in n and show that it can be written as	
	$n^2 - 121n + 3640 = 0 (3)$	
	(d) Solve the equation in part (c).	
	(e) State, with a reason, which of the solutions to the equation in part (c) is not a sensible value for n.	
	(1)	

Question 5 continued	bla

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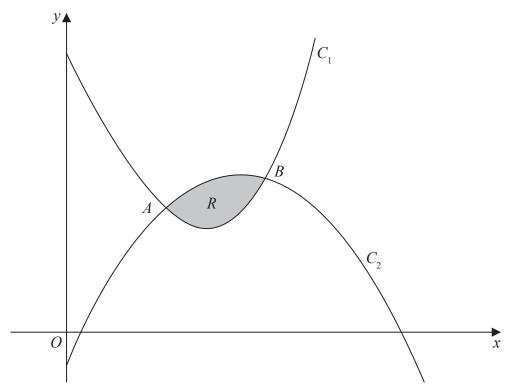


Figure 1

Figure 1 shows a sketch of part of the curves $C_{\scriptscriptstyle 1}$ and $C_{\scriptscriptstyle 2}$ with equations

$$C_1: y = x^3 - 6x + 9$$
 $x \ge 0$
 $C_2: y = -2x^2 + 7x - 1$ $x \ge 0$

The curves C_1 and C_2 intersect at the points A and B as shown in Figure 1.

The point A has coordinates (1, 4).

Using algebra and showing all steps of your working,

(a) find the coordinates of the point B.

(4)

The finite region R, shown shaded in Figure 1, is bounded by $C_{\scriptscriptstyle 1}$ and $C_{\scriptscriptstyle 2}$

(b) Use algebraic integration to find the exact area of R.

(5)

Question 6 continued	Leave blank

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Question 6 continued	blank
	Q6
(Total 9 marks)	
(Total 9 marks)	

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7. (i) Show that

$$\tan \theta + \frac{1}{\tan \theta} \equiv \frac{1}{\sin \theta \cos \theta} \qquad \theta \neq \frac{n\pi}{2} \quad n \in \mathbb{Z}$$
(3)

(ii) Solve, for $0 \le x < 90^{\circ}$, the equation

$3\cos^2(2x+10^\circ)=1$				
giving your answers in degrees to one decimal place.				
(Solutions based entirely on graphical or numerical methods are not acceptable.)	(4)			

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Question 7 continued	Olank
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(Total 7 marks)	

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- **8.** A geometric series has first term a and common ratio r.
 - (a) Prove that the sum of the first n terms of this series is given by

$$S_n = \frac{a(1 - r^n)}{1 - r}$$

The second term of a geometric series is -320 and the fifth term is $\frac{512}{25}$

(b) Find the value of the common ratio.

(2)

(3)

(c) Hence find the sum of the first 13 terms of the series, giving your answer to 2 decimal places.

(3)

Question 8 continued	Leav blan

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Question 8 continued	blank

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Question 8 continued	blank
	Q8
(Total 8 marks)	

	P2_2020_1	0_QP
9. (i) Find the exact value of x for which		Leave blank
$\log_3(x+5) - 4 = \log_3(2x-1)$	(4)	
(ii) Given that	(-)	
$3^{y+3} \times 2^{1-2y} = 108$		
(a) show that		
$0.75^{y} = 2$	(4)	
(b) Hence find the value of y, giving your answer to 3 decimal places.	(2)	

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TOTAL FOR PAPER IS 75 MARKS END	

Please check the examination details below before entering your candidate information				
Candidate surname		Other names		
Pearson Edexcel International Advanced Level	Centre Numbe	r Cano	lidate Number	
Monday 18 Ja	anuary	2021		
Morning (Time: 1 hour 30 minute	es) Paper	Reference WM	12/01	
Mathematics				
International Advance Pure Mathematics P2	d Subsidia	ry/Advanced	l Level	
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Turn over ▶

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1.	$f(x) = x^4 + ax^3 - 3x^2 + bx + 5$	blan
	where a and b are constants.	
	When $f(x)$ is divided by $(x + 1)$, the remainder is 4	
	(a) Show that $a + b = -1$	
	(2)	
	When $f(x)$ is divided by $(x-2)$, the remainder is -23	
	(b) Find the value of a and the value of b . (4)	

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(Total 6 marks)	
(Total V marks)	

A curve has equation	
$y = x^3 - x^2 - 16x + 2$	
(a) Using calculus, find the x coordinates of the stationary points of the curve.	(4)
(b) Justify, by further calculus, the nature of all of the stationary points of the cu	(3)

Question 2 continued	Leave blank
	Q2
(Total 7 marks)	

. (1)	Solve
		$7^{x+2} = 3$
		giving your answer in the form $x = \log_7 a$ where a is a rational number in its simplest form.
		(3)
(ii)	Using the laws of logarithms, solve
		$1 + \log_2 y + \log_2 (y + 4) = \log_2 (5 - y) $ (5)

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Question 3 continued	blank
	Q3
(Total 8 marks)	

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4. (a) Find the first three terms, in ascending powers of x, of the binomial expansion	of	Leave
$(2+px)^6$		
where p is a constant. Give each term in simplest form.	(4)	
Given that in the expansion of		
$\left(3-\frac{1}{2}x\right)\left(2+px\right)^6$		
the coefficient of x^2 is $-\frac{3}{4}$		
(b) find the possible values of p.	(4)	

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Question 4 continued	

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(Total 8 marks)	

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$3x+1\geqslant 2\sqrt{3x}$	(3)
(ii) Show that the following statement is not true.	
"The sum of three consecutive prime numbers is always a multiple of 5"	(1)

Question 5 continued	Leave
	Q5
(Total 4 marks)	
(Total 4 marks)	

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6. (a) Show that the equation

$$\frac{3\sin\theta\cos\theta}{2\sin\theta - 1} = 5\tan\theta \qquad \sin\theta \neq \frac{1}{2}$$

can be written in the form

$$3\sin^3\theta + 10\sin^2\theta - 8\sin\theta = 0$$

(4)

(b) Hence solve, for $-\frac{\pi}{4} < x < \frac{\pi}{4}$

$$\frac{3\sin 2x\cos 2x}{2\sin 2x - 1} = 5\tan 2x$$

giving your answers to 3 decimal places where appropriate.

(4)

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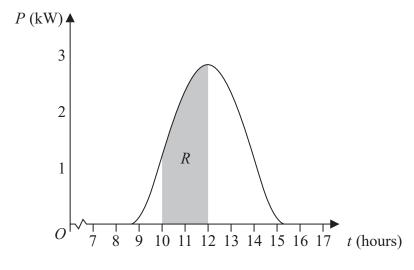


Figure 1

Solar panels are installed on the roof of a building.

The power, P, produced on a particular day, in kW, can be modelled by the equation

$$P = 0.95 + 2^{t-12} + 2^{12-t} - (t-12)^2$$
 8.5 $\leq t \leq 15.2$

where t is the time in hours after midnight. The graph of P against t is shown in Figure 1.

A table of values of t and P is shown below, with the values of P given to 4 significant figures where appropriate.

Time, t (hours)	10	10.5	11	11.5	12
Power, P (kW)		1.882	2.45		2.95

(a) Use the given equation to complete the table, giving the values of P to 4 significant figures where appropriate.

(2)

The amount of energy, in kWh, produced between 10:00 and 12:00 can be found by calculating the area of region R, shown shaded in Figure 1.

(b) Use the trapezium rule, with all the values of P in the completed table, to find an estimate for the amount of energy produced between 10:00 and 12:00. Give your answer to 2 decimal places.

(4)

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Question 7 continued	Dialik
	Q7
(Total 6 marks)	

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8. A sequence a_1, a_2, a_3, \dots is defined by

$$a_{n+1} = 2(a_n + 3)^2 - 7$$
$$a_1 = p - 3$$

where p is a constant.

(a) Find an expression for a_2 in terms of p, giving your answer in simplest form.

(1)

Given that $\sum_{n=1}^{3} a_n = p + 15$

(b) find the possible values of a_2

(6)

Question 8 continued	Leav

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(Total 7 marks)	

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9.	A circle	C has	equation
<i>-</i> •	11 011010	CHub	equation

$$(x-k)^2 + (y-2k)^2 = k+7$$

where k is a positive constant.

- (a) Write down, in terms of k,
 - (i) the coordinates of the centre of C,
 - (ii) the radius of C.

(2)

Given that the point P(2,3) lies on C

- (b) (i) show that $5k^2 17k + 6 = 0$
 - (ii) hence find the possible values of k.

(3)

The tangent to the circle at P intersects the x-axis at point T.

Given that k < 2

(c) calculate the exact area of triangle OPT.

(5)

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10. In this question you must show detailed reasoning.

Owen wants to train for 12 weeks in preparation for running a marathon.

During the 12-week period he will run every Sunday and every Wednesday.

- On Sunday in week 1 he will run 15 km
- On Sunday in week 12 he will run 37 km

He considers two different 12-week training plans.

In training plan A, he will increase the distance he runs each Sunday by the same amount.

(a) Calculate the distance he will run on Sunday in week 5 under training plan A.

(3)

In training plan B, he will increase the distance he runs each Sunday by the same percentage.

(b) Calculate the distance he will run on Sunday in week 5 under training plan *B*. Give your answer in km to one decimal place.

(3)

Owen will also run a fixed distance, x km, each Wednesday over the 12-week period.

Given that

- x is an integer
- the total distance that Owen will run on Sundays and Wednesdays over the 12 weeks will not exceed 360 km
- (c) (i) find the maximum value of x, if he uses training plan A,

(ii)	find	the	maximum	value	of x ,	if he	uses	training p	olan <i>B</i> .	
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(5)

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TOTAL FOR PAPER IS 75 MARK	

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Mathematics		
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- Good luck with your examination

Turn over ▶

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1.	Adina is saving money to buy a new computer. She saves £5 in week 1, £5.25 in week 2, £5.50 in week 3 and so on until she has enough money, in total, to buy the computer.	DIAIIK
	She decides to model her savings using either an arithmetic series or a geometric series.	
	Using the information given,	
	(a) (i) state with a reason whether an arithmetic series or a geometric series should be used,	
	(ii) write down an expression, in terms of n , for the amount, in pounds (£), saved in week n .	
	(3)	
	Given that the computer Adina wants to buy costs £350	
	(b) find the number of weeks it will take for Adina to save enough money to buy the	
	computer. (4)	

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Question 1 continued	
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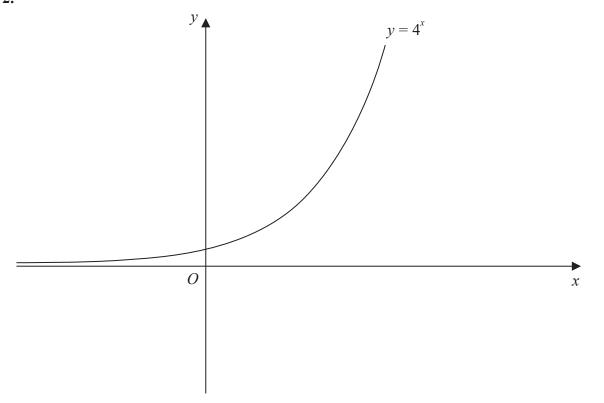


Figure 1

Figure 1 shows a sketch of the curve with equation $y = 4^x$

A copy of Figure 1, labelled Diagram 1, is shown on the next page.

(a) On Diagram 1, sketch the curve with equation

(i)
$$y = 2^x$$

(ii)
$$y = 4^x - 6$$

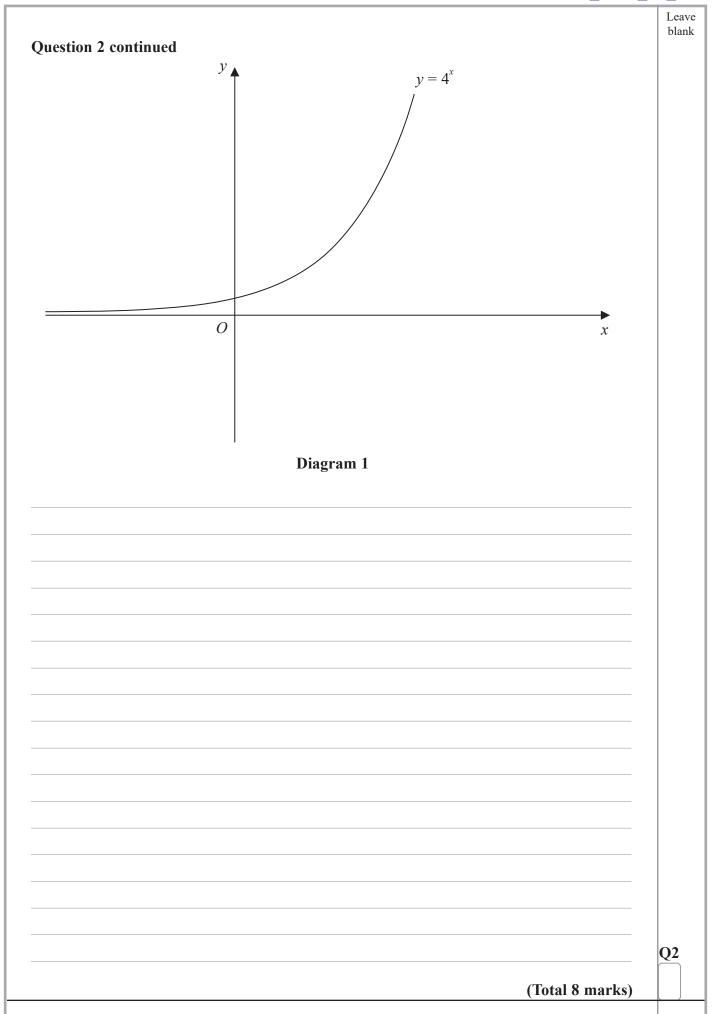
Label clearly the coordinates of any points of intersection with the coordinate axes.

(4)

The curve with equation $y = 2^x$ meets the curve with equation $y = 4^x - 6$ at the point P.

(b) Using algebra, find the exact coordinates of P.

(4)



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3. (i) Prove that for all single digit prime numbers, p ,	
$p^3 + p$ is a multiple of 10	
(2	2)
(ii) Show, using algebra, that for $n \in \mathbb{N}$	
$(n+1)^3 - n^3$ is not a multiple of 3	
(3	3)
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4. (a) Find, in ascending powers of x , up to and including the term in x^3 , the b expansion of	inomial
$\left(2+\frac{x}{8}\right)^{13}$	
fully simplifying each coefficient.	(4)
(b) Use the answer to part (a) to find an approximation for 2.0125 ¹³	
Give your answer to 3 decimal places.	(3)
Without calculating 2.0125 ¹³	
(c) state, with a reason, whether the answer to part (b) is an overestimate underestimate.	e or an
direct estimate.	(1)

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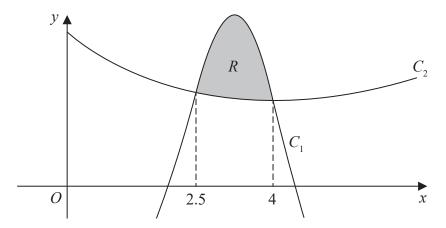


Figure 2

Figure 2 shows a sketch of part of the graph of the curves ${\cal C}_{\scriptscriptstyle 1}$ and ${\cal C}_{\scriptscriptstyle 2}$

The curves intersect when x = 2.5 and when x = 4

A table of values for some points on the curve C_1 is shown below, with y values given to 3 decimal places as appropriate.

х	2.5	2.75	3	3.25	3.5	3.75	4
У	5.453	7.764	9.375	9.964	9.367	7.626	5

Using the trapezium rule with all the values of y in the table,

(a) find, to 2 decimal places, an estimate for the area bounded by the curve C_1 , the line with equation x = 2.5, the x-axis and the line with equation x = 4

(4)

The curve C_2 has equation

$$y = x^{\frac{3}{2}} - 3x + 9 \qquad x > 0$$

(b) Find
$$\int \left(x^{\frac{3}{2}} - 3x + 9\right) dx$$
 (3)

The region R, shown shaded in Figure 2, is bounded by the curves C_1 and C_2

(c) Use the answers to part (a) and part (b) to find, to one decimal place, an estimate for the area of the region R.

(3)

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6. A circle has equation		blar
$x^2 - 6x + y^2 + 8y + k = 0$		
where k is a positive constant.		
Given that the x-axis is a tangent to this circle,		
(a) find the value of k.		
	(3)	
The circle meets the coordinate axes at the points R , S and T .		
(b) Find the exact area of the triangle <i>RST</i> .	(4)	

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	Q6
(Total 7 marks)	

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7.	(a)	Given that			blank
	· /		$3\log_3(2x-1) = 2 + \log_3(14x-25)$		
		show that			
			$2x^3 - 3x^2 - 30x + 56 = 0$	(4)	
	(b)	Show that –4	is a root of this cubic equation.	(2)	

(c) Hence, using algebra and showing each step of your working, solve

$$3\log_3(2x-1) = 2 + \log_3(14x-25)$$
(4)

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Question 7 continued	Leave blank
	Q7
(Total 10 marks)	

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8.	In this question you must show all stages of your working.
	Solutions relying entirely on calculator technology are not acceptable.

(i) Solve, for $0 < \theta < 360^{\circ}$, the equation

$$3\sin(\theta + 30^\circ) = 7\cos(\theta + 30^\circ)$$

giving your answers to one decimal place.

(4)

(ii) (a) Show that the equation

$$3\sin^3 x = 5\sin x - 7\sin x\cos x$$

can be written in the form

$$\sin x(a\cos^2 x + b\cos x + c) = 0$$

where a, b and c are constants to be found.

(b) Hence solve for $-\frac{\pi}{2} \leqslant x \leqslant \frac{\pi}{2}$ the equation

$$3\sin^3 x = 5\sin x - 7\sin x\cos x$$

(6)

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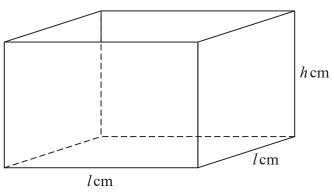


Figure 3

Figure 3 shows a sketch of a square based, open top box.

The height of the box is h cm, and the base edges each have length l cm.

Given that the volume of the box is 250 000 cm³

(a) show that the external surface area, $S \text{ cm}^2$, of the box is given by

$$S = \frac{250\,000}{h} + 2000\sqrt{h}$$

(3)

(b) Use algebraic differentiation to show that S has a stationary point when $h = 250^k$ where k is a rational constant to be found.

(5)

(c) Justify by further differentiation that this value of h gives the minimum external surface area of the box.

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Question 9 continued	Leave blank
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Question 9 continued	Lea bla
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(Total 10 mark	(s)

Please check the examination details below before entering your candidate information				
Candidate surname		Other names)	
Centre Number Candidate N	lumber			
Pearson Edexcel Inter	nation	al Advane	ced Level	
Time 1 hour 30 minutes	Paper reference	WMA	12/01	
Mathematics				
International Advanced S	ubsidiar	v/Advanced	Level	
Pure Mathematics P2	,	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		
i die Mathematics i 2				
You must have: Mathematical Formulae and Statistic	al Tables (Ye	llow), calculator	Total Marks	

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

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- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
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Information

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Advice

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- Try to answer every question.
- Check your answers if you have repeated in encountered.

Turn over ▶

1. The first three	e terms, in ascending powers of x, of the binomial expansion of $(1 + kx)^{16}$ are	blar
	$1, -4x$ and px^2	
where k and p	are constants.	
(a) Find, in si	implest form,	
(i) the va	alue of k	
(ii) the va	alue of p (3)	
	$g(x) = \left(2 + \frac{16}{x}\right) (1 + kx)^{16}$	
Using the valu	ue of k found in part (a),	
(b) find the te	erm in x^2 in the expansion of $g(x)$. (3)	

Question 1 continued	Leave blank
	Q1
(Total 6 marks)	

Leave blank

2.	A sequence	is	defined	by

$$u_1 = 6$$
$$u_{n+1} = ku_n + 3$$

where k is a positive constant.

(a) Find, in terms of k, an expression for u_3

(2)

Given that $\sum_{n=1}^{3} u_n = 117$

(b) find the value of k.

(3)

Question 2 continued	

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3.

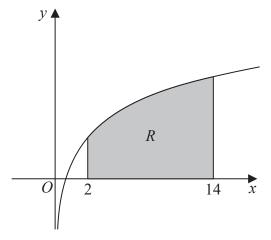


Figure 1

Figure 1 shows a sketch of part of the curve with equation $y = \log_{10} x$

The region R, shown shaded in Figure 1, is bounded by the curve, the line with equation x = 2, the x-axis and the line with equation x = 14

Using the trapezium rule with four strips of equal width,

(a) show that the area of R is approximately 10.10

(3)

(b) Explain how the trapezium rule could be used to obtain a more accurate estimate for the area of *R*.

(1)

(c) Using the answer to part (a) and making your method clear, estimate the value of

$$(i) \quad \int_2^{14} \log_{10} \sqrt{x} \, \mathrm{d}x$$

(ii)
$$\int_{2}^{14} \log_{10} 100 x^3 \, \mathrm{d}x$$

(4)

Question 3 continued	Leave blank

Question 3 continued	Leave

Question 3 continued	Leave blank
	Q3
(Total 8 marks)	

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4.	$f(x) = (x^2 - 2)(2x - 3) - 21$	bi
	(a) State the value of the remainder when $f(x)$ is divided by $(2x-3)$	(1)
	(b) Use the factor theorem to show that $(x-3)$ is a factor of $f(x)$	(2)
	(c) Hence,	
	(i) factorise $f(x)$	
	(ii) show that the equation $f(x) = 0$ has only one real root.	(5)

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Question 4 continued	

Question 4 continued	Leave blank

Question 4 continued	Leav blanl	
	Q4	
(Total 8	marks)	

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5.	A company	that	owned	a	silver	mine

- extracted 480 tonnes of silver from the mine in year 1
- extracted 465 tonnes of silver from the mine in year 2
- extracted 450 tonnes of silver from the mine in year 3

and so on, forming an arithmetic sequence.

(a) Find the mass of silver extracted in year 14

(2)

After a total of 7770 tonnes of silver was extracted, the company stopped mining.

Given that this occurred at the end of year N,

(b) show that

$$N^2 - 65N + 1036 = 0$$

(3)

(c) Hence, state the value of	<i>N</i> .
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(1)

Question 5 continued	Leave blank
	Q5
(Total 6 ma	arks)

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6.	(i)	The circle	$C_{_1}$	has equation
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$$x^2 + y^2 + 10x - 12y = k$$
 where k is a constant

(a) Find the coordinates of the centre of C_1

(2)

(b) State the possible range in values for k.

(2)

(ii) The point P(p, 0), the point Q(-2, 10) and the point R(8, -14) lie on a different circle, C_2

Given that

- *p* is a positive constant
- QR is a diameter of C_2

find the exact value of p.

(4)

Question 6 continued	Leave blank

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Question 6 continued	

Question 6 continued	Leave blank
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	Q6
(Total 8 mar	

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7. (i)	A geometric sequence has first term 4 and common ratio 6	blan
/• (1)	Given that the n^{th} term is greater than 10^{100} , find the minimum possible value of n .	
	(3)	
(ii)	A different geometric sequence has first term a and common ratio r .	
	Given that	
	 the second term of the sequence is -6 the sum to infinity of the series is 25 	
	(a) show that	
	$25r^2 - 25r - 6 = 0$	
	(3)	
	(b) Write down the solutions of	
	$25r^2 - 25r - 6 = 0$	
	(1)	
	Hence,	
	(c) state the value of r , giving a reason for your answer, (1)	
	(d) find the sum of the first 4 terms of the series. (2)	

Question 7 continued	Leave blank

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(Total 10 marks)	

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8. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

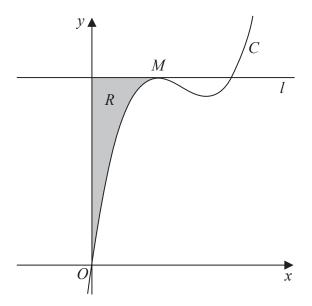


Figure 2

Figure 2 shows a sketch of part of the curve C with equation

$$y = \frac{4}{3}x^3 - 11x^2 + kx$$
 where k is a constant

The point *M* is the maximum turning point of *C* and is shown in Figure 2.

Given that the x coordinate of M is 2

(a) show that k = 28

(3)

(b) Determine the range of values of x for which y is increasing.

(2)

The line l passes through M and is parallel to the x-axis.

The region R, shown shaded in Figure 2, is bounded by the curve C, the line l and the y-axis.

(c) Find, by algebraic integration, the exact area of R.

(5)

Question 8 continued	Leave blank
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		Q8
(Total 10 ma	rke)	
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(a) Prove that for all positive values of x and y ,	
$\frac{x+y}{2} \geqslant \sqrt{xy}$	
2	(3)
(b) Prove by counter-example that this inequality does not hold when x and	v are
both negative.	
	(1)

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Question 9 continued	
	Q9
(Total 4 marks)	

10.	In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

(i) Solve, for
$$-\frac{\pi}{2} < x < \frac{\pi}{2}$$

$$\tan^2\left(2x + \frac{\pi}{4}\right) = 3\tag{5}$$

(ii) Solve, for $0 < \theta < 360^{\circ}$

$$(2\sin\theta - \cos\theta)^2 = 1$$

giving your answers, as appropriate, to one decimal place. (5)

P2_2021_10_QP

Question 10 continued	Leave
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TOTAL FOR PAPER IS 75 MARKS	

Please check the examination details bel	w before entering your o	andidate information
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Centre Number Candidate No	mber	
Pearson Edexcel Inter	national Ac	lvanced Level
Time 1 hour 30 minutes	Paper reference W	MA12/01
Mathematics		0 0
International Advanced Su Pure Mathematics P2	bsidiary/Adv	anced Level
You must have: Mathematical Formulae and Statistica	l Tables (Yellow), ca	Iculator Total Marks

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- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ▶

1. The table below shows corresponding values of x and y for

$$y = 2^{5 - \sqrt{x}}$$

The values of y are given to 3 decimal places.

x	5	5.5	6	6.5	7
y	6.792	6.298	5.858	5.466	5.113

Using the trapezium rule with all the values of y in the given table,

(a) obtain an estimate for

$$\int_{5}^{7} 2^{5-\sqrt{x}} \, \mathrm{d}x$$

giving your answer to 2 decimal places.

(3)

(b) Using your answer to part (a) and making your method clear, estimate

$$(i) \quad \int_5^7 2^{6-\sqrt{x}} \, \mathrm{d}x$$

(ii)
$$\int_{5}^{7} (3 + 2^{5 - \sqrt{x}}) dx$$

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Question 1 continued	Leave blank

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Question 1 continued	
	_
	Q1
(Total 7 marks)	

2. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

The curve C has equation

$$y = 27x^{\frac{1}{2}} - x^{\frac{3}{2}} - 20 \qquad x > 0$$

(a) Find $\frac{dy}{dx}$, giving each term in simplest form.

(2)

(b) Hence find the coordinates of the stationary point of C.

(4)

(c) Find $\frac{d^2y}{dx^2}$ and hence determine the nature of the stationary point of C.

(2)

Question 2 continued	Leave blank
	Q2
(Total 8	marks)

3. (a) Find the first 4 terms, in ascending powers of x, of the binomial expansion of

$$\left(2-\frac{kx}{4}\right)^8$$

where k is a non-zero constant. Give each term in simplest form.

(4)

$$f(x) = (5 - 3x) \left(2 - \frac{kx}{4}\right)^8$$

In the expansion of f(x), the constant term is 3 times the coefficient of x.

(b) Find	l the	value	of <i>k</i> .
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(3)

Question 3 continued		Leave blank
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Question 3 continued	Leave blank

Question 3 continued	Leave blank
	Q3
(Total 7 ma	rks)

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	$\log_3(32 - 12x) = 2\log_3(1 - x) + 3$	
	23	(5)
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Question 4 continued	Leave blank
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(Total 5 mar)	Q4

$f(x) = 3x^3 + Ax^2 + Bx - 10$

where A and B are integers.

Given that

- when f(x) is divided by (x-1) the remainder is k
- when f(x) is divided by (x + 1) the remainder is -10k
- *k* is a constant
- (a) show that

$$11A + 9B = 83$$

(3)

Given also that (3x - 2) is a factor of f(x),

(b) find the value of A and the value of B.

(3)

(c) Hence find the quadratic expression g(x) such that

$$f(x) = (3x - 2)g(x)$$

(2)

Question 5 continued	Leave blank

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Question 5 continued	

Question 5 continued	Leave blank
	Q5
(Total 8 marks)	

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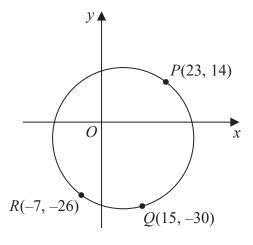


Figure 1

The points P(23, 14), Q(15, -30) and R(-7, -26) lie on the circle C, as shown in Figure 1.

(a) Show that angle $PQR = 90^{\circ}$

(2)

- (b) Hence, or otherwise, find
 - (i) the centre of C,
 - (ii) the radius of C.

(3)

Given that the point S lies on C such that the distance QS is greatest,

(c) find an equation of the tangent to C at S, giving your answer in the form ax + by + c = 0, where a, b and c are integers to be found. (3)

Question 6 continued	Leave blank
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Question 6 continued	
	Q6
(Total 8 marks)	

Leave

7. In this question you must show all stages of your working.	blank
Solutions relying entirely on calculator technology are not acceptable.	
(i) Solve, for $-90^{\circ} < x < 90^{\circ}$, the equation	
$3\sin(2x - 15^{\circ}) = \cos(2x - 15^{\circ})$	
giving your answers to one decimal place. (4)	
(ii) Solve, for $0 < \theta < 2\pi$, the equation	
$4\sin^2\theta + 8\cos\theta = 3$	
giving your answers to 3 significant figures. (4)	

Question 7 continued	Leave blank

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Question 7 continued	

Question 7 continued		Lea
		Q7
	(Total 8 marks)	

(Given that	
	• on the 1st hit, the post is driven 100 mm into the ground	
	• on the 2nd hit, the post is driven an additional 98 mm into the ground	
	• on the 3rd hit, the post is driven an additional 96 mm into the ground	
	• the additional distances the post travels on each subsequent hit form an arithmetic sequence	
	(a) show that the post is driven an additional 62 mm into the ground with the 20th hit. (1)	
	(b) Find the total distance that the post has been driven into the ground after 20 hits. (2)	
(Given that for each subsequent hit after the 20th hit	
	• the additional distances the post travels form a geometric sequence with common ratio r	
	• on the 22nd hit, the post is driven an additional 60 mm into the ground	
	(c) find the value of r , giving your answer to 3 decimal places. (2)	
,	After a total of N hits, the post will have been driven more than 3 m into the ground.	
•	and the same of the mass, and place with have a contract of many a manufacture of the same.	
	(d) Find showing all stone in your working the smallest nessible value of N	
	(d) Find, showing all steps in your working, the smallest possible value of N . (4)	

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	Q8
(Total 9 ma	arks)

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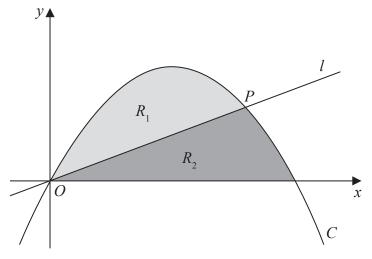


Figure 2

Figure 2 shows

- the curve C with equation $y = x x^2$
- the line *l* with equation y = mx, where *m* is a constant and 0 < m < 1

The line and the curve intersect at the origin O and at the point P.

(a) Find, in terms of m, the coordinates of P.

(2)

The region R_1 , shown shaded in Figure 2, is bounded by C and l.

(b) Show that the area of R_1 is

$$\frac{\left(1-m\right)^3}{6}$$

(5)

The region R_2 , also shown shaded in Figure 2, is bounded by C, the x-axis and l. Given that the area of R_1 is equal to the area of R_2

(c)	find	the	exact	value	of m	
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(3)

Question 9 continued	Leave blank

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Question 9 continued	
	Q9
(Total 10 marks)	

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10. (i) Prove by counter example that the statement	
"if p is a prime number then $2p + 1$ is also a prime number"	
is not true.	(1)
(ii) Use proof by exhaustion to prove that if n is an integer then	
$5n^2 + n + 12$	
is always even.	(4)

Question 10 continued	Leave blank

Question 10 continued	Leave
	Q10
(Total 5 marks)	
TOTAL FOR PAPER IS 75 MARKS	

Please check the examination details below before entering your candidate information Candidate surname Other names			
Candidate surname	Other names		
Centre Number Candidate Nu	umber		
Pearson Edexcel Inter	national Advanced Leve	į	
Time 1 hour 30 minutes	Paper reference WMA12/01		
Mathematics International Advanced Su	thsidiary/∆dyanced Level		
Pure Mathematics P2	absidiai y/Advanced Level		
You must have: Mathematical Formulae and Statistica	al Tables (Yellow), calculator	cs	

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Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have meaning the end.

Figure 1

Turn over ▶

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Find the first four terms, in ascending powers of x , of the binomial expansion of	
$\left(2+\frac{3}{8}x\right)^{10}$	
Give each coefficient as an integer.	(4)

Question 1 continued	Leave blank
(Total 4 marks)	Q1

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2.

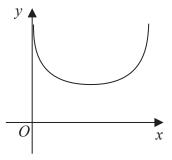


Figure 1

Figure 1 shows the graph of

$$y = 1 - \log_{10}(\sin x) \qquad 0 < x < \pi$$

where x is in radians.

The table below shows some values of x and y for this graph, with values of y given to 3 decimal places.

х	0.5	1	1.5	2	2.5	3
у	1.319		1.001		1.223	1.850

(a) Complete the table above, giving values of y to 3 decimal places.

(2)

(b) Use the trapezium rule with all the y values in the completed table to find, to 2 decimal places, an estimate for

$$\int_{0.5}^{3} (1 - \log_{10}(\sin x)) dx$$

(3)

(c) Use your answer to part (b) to find an estimate for

$$\int_{0.5}^3 \left(3 + \log_{10}(\sin x)\right) \mathrm{d}x$$

(3)

Question 2 continued	Leave blank

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	Q2
(Total 8 mark	(s)

3. (i) Show that the following statement is false:	
" $(n+1)^3 - n^3$ is prime for all $n \in \mathbb{N}$ "	
•	(2)
(ii) Given that the points $A(1, 0)$, $B(3, -10)$ and $C(7, -6)$ lie on a circle, prove that AB is a diameter of this circle.	
	(5)

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(Total 7 marks	Q3 (s)

4.	In this question you must show all stages of your working.	
	Give your answers in fully simplified surd form.	
Giv	ten that a and b are positive constants, solve the simultaneous equations	
	$a - b = 8$ $\log_4 a + \log_4 b = 3$	
	(6)	

Question 4 continued	Lea bla	
	Q4	
(100a)	l 6 marks))

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5.	In this question you must show all stages of your working.
	Solutions relying entirely on calculator technology are not acceptable.
	Solve, for $-180^{\circ} < \theta \leqslant 180^{\circ}$, the equation
	$3\tan(\theta + 43^\circ) = 2\cos(\theta + 43^\circ)$
	(6)

Question 5 continued	Leave blank
	Q5
(Total 6 marks)	

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6.	In a	geometric	sequence	u_{1} ,	u_2 ,	u_{2} ,	

- the common ratio is r
- $u_2 + u_3 = 6$ $u_4 = 8$
- (a) Show that r satisfies

$$3r^2 - 4r - 4 = 0$$

(3)

Given that the geometric sequence has a sum to infinity,

(b) find u_1

(3)

(c) find S_{∞}

(2)

Question 6 continued	Leave blank

Question 6 continued	Leave blank

Question 6 continued	Leave blank
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	Q6
(Total 8 mar	

(7)

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$f(x) = Ax^3 + 6x^2 - 4x + B$
1(11) 1111 011 111 2

where A and B are constants.

Given that

7.

- (x+2) is a factor of f(x)

find the value of A and the value of B.

Question 7 continued		Leave blank
		Q 7
	(Total 7 marks)	

Leave blank

8. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

A curve has equation

$$y = 256x^4 - 304x - 35 + \frac{27}{x^2} \qquad x \neq 0$$

(a) Find
$$\frac{dy}{dx}$$

(3)

(b)	Hence find	the coordinates	of the	stationary	points	of the	curve
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(5)

Question 8 continued	Leave blank
	Q8
(Total 8	8 marks)

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A scientist is using carbon-14 dating to determine the age of some wooden items.	
The equation for carbon-14 dating an item is given by	
$N=k\lambda^{\iota}$	
where	
 N grams is the amount of carbon-14 currently present in the item k grams was the initial amount of carbon-14 present in the item t is the number of years since the item was made λ is a constant, with 0 < λ < 1 	
(a) Sketch the graph of N against t for $k = 1$ (2)	
Given that it takes 5700 years for the amount of carbon-14 to reduce to half its initial value,	
(b) show that the value of the constant λ is 0.999878 to 6 decimal places. (2)	
Given that Item A	
 is known to have had 15 grams of carbon-14 present initially is thought to be 3250 years old 	
(c) calculate, to 3 significant figures, how much carbon-14 the equation predicts is currently in Item A. (2)	
Item <i>B</i> is known to have initially had 25 grams of carbon-14 present, but only 18 grams now remain.	
(d) Use algebra to calculate the age of Item <i>B</i> to the nearest 100 years. (3)	

Question 9 continued	L	Leave blank

Question 9 continued	Leave blank

	Leave blank
Question 9 continued	
	Q9
(Total 9 marks)	

Leave blank

10. The circle C has centre X(3, 5) and radius r

The line *l* has equation y = 2x + k, where *k* is a constant.

(a) Show that l and C intersect when

$$5x^2 + (4k - 26)x + k^2 - 10k + 34 - r^2 = 0$$
(3)

Given that l is a tangent to C,

(b) show that $5r^2 = (k + p)^2$, where p is a constant to be found.

(3)

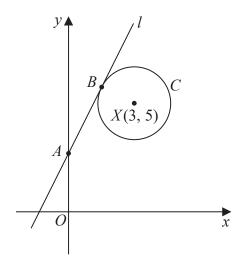


Figure 2

The line *l*

- cuts the y-axis at the point A
- touches the circle C at the point B

as shown in Figure 2.

Given that AB = 2r

(c) find the value of k

Question 10 continued	Leave blank

Question 10 continued	Leave blank

Question 10 continued	Leave
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Question 10 continued	Leave
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TOTAL FOR PAPER IS 75 MARKS	

Please check the examination details below before entering your candidate information			
Candidate surname	Other names		
Centre Number Candidate Number			
Pearson Edexcel Internation	onal Advanced Level		
Time 1 hour 30 minutes Paper refere	MMA12/01		
Mathematics International Advanced Subsidiary/Advanced Level Pure Mathematics P2			
You must have: Mathematical Formulae and Statistical Tables (Yellow), calculator			

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 - there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶

1. Given that a, b and c are integers greater than 0 such that

•
$$c = b + 2$$

•
$$a + b + c = 10$$

Prove, by exhaustion, that the product of a, b and c is always even.

You may use the table below to illustrate your answer.

(3)

You may not need to use all rows of this table.

а	ь	С
	1	
	2	

Question 1 continued
(Total for Question 1 is 3 marks)

2.	A curve C has equation $y = f(x)$ where	
	$f(x) = (2 - kx)^5$	
	and k is a constant.	
	Given that when $f(x)$ is divided by $(4x - 5)$ the remainder is $\frac{243}{32}$	
	(a) show that $k = \frac{2}{5}$	
	3	(2)
	(b) Find the first three terms, in ascending powers of x , of the binomial expansion of	
	$\left(2-\frac{2}{5}x\right)^5$	
	giving each term in simplest form.	(2)
	Using the solution to part (b) and making your method along	(3)
	Using the solution to part (b) and making your method clear, (c) find the gradient of <i>C</i> at the point where <i>x</i> = 0	
	(c) find the gradient of C at the point where $x = 0$	(2)

Question 2 continued

Question 2 continued

Question 2 continued	
(Total for Question 2 is 7 marks	s)

3.	A sequence a_1, a_2, a_3, \dots is defined by	
	$a_n = \cos^2\left(\frac{n\pi}{3}\right)$	
	Find the exact values of	
	(a) (i) a_1	
	(ii) a_2	
	(iii) a_3	(3)
	(b) Hence find the exact value of	(3)
	$\sum_{n=1}^{30} \left\{ n + \cos^2\left(\frac{n}{3}\right) \right\}$	
	You must make your method clear.	(4)

Question 3 continued
(Total for Orestian 2 is 7 months)
(Total for Question 3 is 7 marks)

4.	The weight of a baby mammal is monitored over a 16-month period.	
	The weight of the mammal, wkg, is given by	
	$w = \log_a(t+5) - \log_a 4 \qquad 2 \leqslant t \leqslant 18$	
	where t is the age of the mammal in months and a is a constant.	
	Given that the weight of the mammal was 10 kg when $t = 3$	
	(a) show that $a = 1.072$ correct to 3 decimal places.	(3)
	Using $a = 1.072$	
	(b) find an equation for t in terms of w	
	(a) 6 1 4 1 - 1 - 1 - 6 (- 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -	(3)
	(c) find the value of t when $w = 15$, giving your answer to 3 significant figures.	(2)

Question 4 continued	
(Total for Question 4	is 8 marks)

5. In	this question you must show detailed reasoning.	
Solutions rel	ying entirely on calculator technology are not acceptable.	
(a) Show that the equation	n	
	$(3\cos\theta - \tan\theta)\cos\theta = 2$	
can be written as		
	$3\sin^2\theta + \sin\theta - 1 = 0$	
π	π	(3)
(b) Hence solve for $-\frac{\pi}{2}$	$\leq x \leq \frac{\pi}{2}$	
	$(3\cos 2x - \tan 2x)\cos 2x = 2$	(5)
		(3)

Question 5 continued

Question 5 continued

Question 5 continued	
	(Total for Question 5 is 8 marks)

6. The curve C_1 has equation y = f(x).

A table of values of x and y for y = f(x) is shown below, with the y values rounded to 4 decimal places where appropriate.

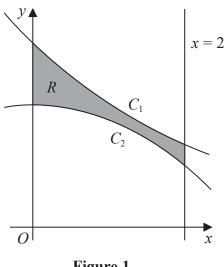
x	0	0.5	1	1.5	2
У	3	2.6833	2.4	2.1466	1.92

(a) Use the trapezium rule with all the values of y in the table to find an approximation for

$$\int_0^2 f(x) dx$$

giving your answer to 3 decimal places.

(3)



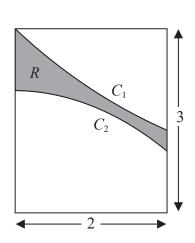


Figure 1

Figure 2

The region *R*, shown shaded in Figure 1, is bounded by

- the curve C_1
- the curve C_2 with equation $y = 2 \frac{1}{4}x^2$
- the line with equation x = 2
- the y-axis

The region *R* forms part of the design for a logo shown in Figure 2.

The design consists of the shaded region R inside a rectangle of width 2 and height 3 Using calculus and the answer to part (a),

(b) calculate an estimate for the percentage of the logo which is shaded.

(4)

Question 6 continued

Question 6 continued

Question 6 continued	
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(Total for Question 6 is 7 marks)	

7. The curve e has equation	The curve C has equ	ıatıor
-----------------------------	---------------------	--------

$$y = \frac{12x^3(x-7) + 14x(13x-15)}{21\sqrt{x}}$$
 $x > 0$

(a) Write the equation of C in the form

$$y = ax^{\frac{7}{2}} + bx^{\frac{5}{2}} + cx^{\frac{3}{2}} + dx^{\frac{1}{2}}$$

where a, b, c and d are fully simplified constants.

(3)

The curve *C* has three turning points.

Using calculus,

(b) show that the x coordinates of the three turning points satisfy the equation

$$2x^3 - 10x^2 + 13x - 5 = 0$$
(3)

Given that the x coordinate of one of the turning points is 1

(c) find, using algebra, the exact x coordinates of the other two turning points.

(Solutions based entirely on calculator technology are not acceptable.)

(3)

Question 7 continued

Question 7 continued

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Ŏ.	. A geometric sequence has first term a and common ratio r				
	Given that $S_{\infty} = 3a$				
	(a) show that $r = \frac{2}{3}$				
	3	(2)			
	Given also that				
	$u_2 - u_4 = 16$				
	where u_k is the k^{th} term of this sequence,				
	(b) find the value of S_{10} giving your answer to one decimal place.				
		(5)			

Question 8 continued
(Total for Question 8 is 7 marks)

9. In this question you must show detailed reasoning.

Solutions relying entirely on calculator technology are not acceptable.

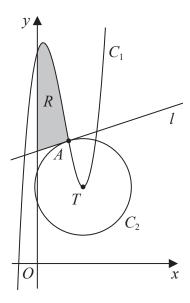


Figure 3

Figure 3 shows

• the curve C_1 with equation $y = x^3 - 5x^2 + 3x + 14$

• the circle C_2 with centre T

The point T is the minimum turning point of C_1

Using Figure 3 and calculus,

(a) find the coordinates of T

(3)

The curve C_1 intersects the circle C_2 at the point A with x coordinate 2

(b) Find an equation of the circle C_2

(3)

The line l shown in Figure 3, is the tangent to circle C_2 at A

(c) Show that an equation of l is

$$y = \frac{1}{3}x + \frac{22}{3} \tag{3}$$

The region R, shown shaded in Figure 3, is bounded by C_1 , l and the y-axis.

(d) Find the exact area of R.

(3)

Question 9 continued

Question 9 continued

Question 9 continued				
(Total for Question 9 is 12 marks)				

10. Given $a = \log_2 3$					
(i) write, in simplest form, in terms of a,					
(a) $\log_2 9$					
(b) $\log_2\left(\frac{\sqrt{3}}{16}\right)$	(3)				
(ii) Solve					
$3^x \times 2^{x+4} = 6$					
giving your answer, in simplest form, in terms of a.	(4)				

Question 10 continued

Question 10 continued
(Total for Question 10 is 7 marks)
TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information				
Candidate surname		Other names		
Centre Number Candidate Number				
Pearson Edexcel Inter	nation	al Advanced Level		
Time 1 hour 30 minutes	Paper reference	WMA12/01		
Mathematics				
International Advanced Subsidiary/Advanced Level Pure Mathematics P2				
You must have: Mathematical Formulae and Statistical Tables (Yellow), calculator Total Marks				

Candidates may use any calculator permitted by Pearson regulations.

Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

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- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
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 use this as a guide as to how much time to spend on each question.

Advice

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- Try to answer every question.
- Check your answers if you have impat the end.

Turn over ▶

1.

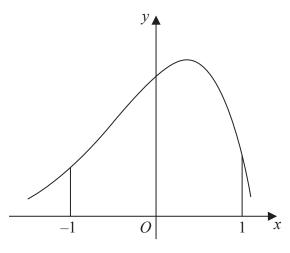


Figure 1

Figure 1 shows a sketch of part of the curve with equation y = f(x)

The table below shows some corresponding values of x and y for this curve.

The values of y are given to 3 decimal places.

х	-1	-0.5	0	0.5	1
у	2.287	4.470	6.719	7.291	2.834

Using the trapezium rule with all the values of y in the given table,

(a) obtain an estimate for

$$\int_{-1}^{1} f(x) dx$$

giving your answer to 2 decimal places.

(3)

(b) Use your answer to part (a) to estimate

(i)
$$\int_{-1}^{1} (f(x)-2) dx$$

(ii)
$$\int_{1}^{3} f(x-2) dx$$

(3)

Question 1 continued
(Total for Question 1 is 6 marks)

2. In this question you must show all stages of your working.

Solutions based entirely on calculator technology are not acceptable.

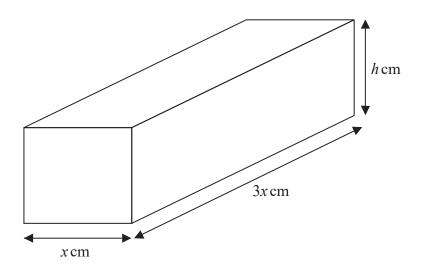


Figure 2

A brick is in the shape of a cuboid with width x cm, length 3x cm and height h cm, as shown in Figure 2.

The volume of the brick is 972 cm³

(a) Show that the surface area of the brick, $S \text{cm}^2$, is given by

$$S = 6x^2 + \frac{2592}{x}$$

(3)

(b) Find
$$\frac{dS}{dx}$$

(1)

(c) Hence find the value of x for which S is stationary.

(2)

(d) Find $\frac{d^2S}{dx^2}$ and hence show that the value of x found in part (c) gives the minimum value of S.

(2)

(e) Hence find the minimum surface area of the brick.

(1)

Question 2 continued		

Question 2 continued		

Question 2 continued		
(Total for Question 2 is 9 marks)		

3.	$f(x) = \left(2 + \frac{kx}{8}\right)^7$ where k is a non-zero constant	
	(a) Find the first 4 terms, in ascending powers of x , of the binomial expansion of $f(x)$. Give each term in simplest form.	(4)
	Given that, in the binomial expansion of $f(x)$, the coefficients of x , x^2 and x^3 are the first 3 terms of an arithmetic progression,	
	(b) find, using algebra, the possible values of k .	
	(Solutions relying entirely on calculator technology are not acceptable.)	(3)

Question 3 continued
(Total for Question 3 is 7 marks)

4. (i) Using the laws of logarithms, solve	
$\log_3(4x) + 2 = \log_3(5x + 7)$	(3)
(ii) Given that	(3)
$\sum_{r=1}^{2} \log_{a} (y^{r}) = \sum_{r=1}^{2} (\log_{a} y)^{r} \qquad y > 1, a > 1, y \neq a$	
find y in terms of a , giving your answer in simplest form.	(3)
	(3)

Question 4 continued		
(Total for Question 4 is 6 marks)		

5.	$f(x) = x^3 + (p+3)x^2 - x + q$	
	where p and q are constants and $p > 0$	
	Given that $(x - 3)$ is a factor of $f(x)$	
	(a) show that	
	9p + q = -51	(2)
	Given also that when $f(x)$ is divided by $(x + p)$ the remainder is 9	()
	(b) show that	
	$3p^2 + p + q - 9 = 0$	(2)
	(c) Hence find the value of p and the value of q .	(3)
	(d) Hence find a quadratic expression $g(x)$ such that	
	f(x) = (x-3)g(x)	(2)

Question 5 continued		

Question 5 continued		
(Total for Question 5 is 9 marks)		

6.	The circle C has equation	
	$x^2 + y^2 + 8x - 4y = 0$	
	(a) Find	
	(i) the coordinates of the centre of C,	
	(ii) the exact radius of C .	(3)
	The point P lies on C .	(3)
	Given that the tangent to C at P has equation $x + 2y + 10 = 0$	
	(b) find the coordinates of <i>P</i>	
		(4)
	(c) Find the equation of the normal to C at P , giving your answer in the form $y = mx + c$ where m and c are integers to be found.	
		(3)

Question 6 continued

Question 6 continued

Question 6 continued
(Total for Question 6 is 10 marks)

7.	A geometric sequence has first term a and common ratio r , where $r > 0$	
	Given that	
	• the 3rd term is 20	
	• the 5th term is 12.8	
	(a) show that $r = 0.8$	
		(1)
	(b) Hence find the value of a.	(2)
	Given that the sum of the first n terms of this sequence is greater than 156	(-)
	(c) find the smallest possible value of n .	
	(Solutions based entirely on graphical or numerical methods are not acceptable.)	
		(4)

Question 7 continued
(Total for Question 7 is 7 marks)

8.	In this question you must show all stages of your working.	
	Solutions based entirely on calculator technology are not acceptable.	
	(i) Solve, for $-\frac{\pi}{2} < x < \pi$, the equation	
	$5\sin(3x+0.1)+2=0$	
	giving your answers, in radians, to 2 decimal places.	(4)
	(ii) Solve, for $0 < \theta < 360^{\circ}$, the equation	
	$2\tan\theta\sin\theta = 5 + \cos\theta$	
	giving your answers, in degrees, to one decimal place.	(5)

Question 8 continued

Question 8 continued

Question 8 continued	
	(Total for Question 8 is 9 marks)

9. In this question you must show all stages of your working.

Solutions based entirely on calculator technology are not acceptable.

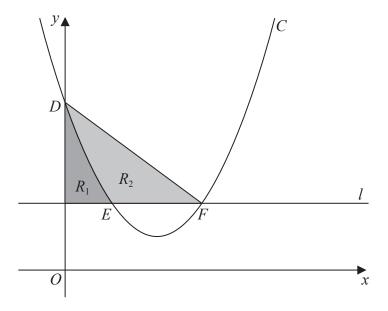


Figure 3

Figure 3 shows

• the curve C with equation $y = x^2 - 4x + 5$

• the line l with equation y = 2

The curve C intersects the y-axis at the point D.

(a) Write down the coordinates of D.

(1)

The curve C intersects the line l at the points E and F, as shown in Figure 3.

(b) Find the x coordinate of E and the x coordinate of F.

(2)

Shown shaded in Figure 3 is

- the region R_1 which is bounded by C, l and the y-axis
- the region R_2 which is bounded by C and the line segments EF and DF

Given that $\frac{\text{area of } R_1}{\text{area of } R_2} = k$, where k is a constant,

(c) use algebraic integration to find the exact value of k, giving your answer as a simplified fraction.

(5)

Question 9 continued

Question 9 continued
(Total for Question 9 is 8 marks)

if <i>n</i> is an integer then $2n^2 + n + 1$ is not divisible by 3	
The start of the student's proof is shown in the box below.	
Consider the case when $n = 3k$	
$2n^2 + n + 1 = 18k^2 + 3k + 1 = 3(6k^2 + k) + 1$	
which is not divisible by 3	
Complete this proof.	
	(4)

Question 10 continued

Question 10 continued	
	(Total for Question 10 is 4 marks)
	TOTAL FOR PAPER IS 75 MARKS

Please check the examination details below before entering your candidate information		
Candidate surname	Other names	
Centre Number Candidate Nu		
Pearson Edexcel Interi	national Advanced Level	
Thursday 18 May 20	23	
Morning (Time: 1 hour 30 minutes)	Paper reference WMA12/01	
Mathematics	△ •	
International Advanced Su Pure Mathematics P2	bsidiary/Advanced Level	
You must have: Mathematical Formulae and Statistical	Tables (Yellow), calculator	

Candidates may use any calculator permitted by Pearson regulations.

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- Answer the questions in the spaces provided
 there may be more space than you need.
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- Inexact answers should be given to three significant figures unless otherwise stated.

Information

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- There are 11 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
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Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have

Turn over ▶

1. The continuous curve C has equation y = f(x).

A table of values of x and y for y = f(x) is shown below.

x	4.0	4.2	4.4	4.6	4.8	5.0
y	9.2	8.4556	3.8512	5.0342	7.8297	8.6

Use the trapezium rule with all the values of y in the table to find an approximation for

$$\int_{4}^{5} f(x) dx$$

$\int_{4} f(x) dx$	
giving your answer to 3 decimal places.	(3)

Question 1 continued
(Total for Question 1 is 3 marks)
(2000 TOT QUEDUIN TID & MINTED)

2.	In this question you must show all stages of your working.	
	Solutions relying on calculator technology are not acceptable.	
	$f(x) = 4x^3 - 8x^2 + 5x + a$	
	where a is a constant.	
	Given that $(2x - 3)$ is a factor of $f(x)$,	
	(a) use the factor theorem to show that $a = -3$	(2)
	(b) Hence show that the equation $f(x) = 0$ has only one real root.	
		(4)

Question 2 continued
(Total for Question 2 is 6 marks)
(Total for Question 2 is 6 marks)

3.	A circle C has centre $(2, 5)$	
	Given that the point $P(8, -3)$ lies on C	
	(a) (i) find the radius of C	
	(ii) find an equation for C	
		(3)
	(b) Find the equation of the tangent to C at P giving your answer in the form $ax + by + c = 0$ where a , b and c are integers to be found.	
	ax + by + c = 0 where a, b and c are integers to be found.	(4)

Question 3 continued
(Total for Question 3 is 7 marks)
(Total for Question 5 is 7 marks)

4.	The binomial expansion, in ascending powers of x , of	
	$(3+px)^5$	
	where p is a constant, can be written in the form	
	$A + Bx + Cx^2 + Dx^3 \dots$	
	where A , B , C and D are constants.	
	(a) Find the value of A	(4)
	Given that	(1)
	• $B = 18D$	
	• $p < 0$	
	(b) find	
	(i) the value of p	
	(ii) the value of C	(6)
		(6)

Question 4 continued

Question 4 continued	

Question 4 continued
(Total for Question 4 is 7 marks)

5.	Use the laws of logarithms to solve	
	$\log_2(16x) + \log_2(x+1) = 3 + \log_2(x+6)$	(5)
		(5)

Question 5 continued
(Total for Question 5 is 5 marks)
(Total for Question 3 is 3 marks)

6.	In this question you must show all stages of your working.	
	Solutions relying entirely on calculator technology are not acceptable.	
	A software developer released an app to download.	
	The numbers of downloads of the app each month, in thousands, for the first three months after the app was released were	
	2k-15 k $k+4$	
	where k is a constant.	
	Given that the numbers of downloads each month are modelled as a geometric series,	
	(a) show that $k^2 - 7k - 60 = 0$	(2)
	(b) predict the number of downloads in the 4th month.	(2)
	(b) predict the number of downloads in the 4th month.	(4)
	The total number of all downloads of the app is predicted to exceed 3 million for the first time in the N th month.	
	(c) Calculate the value of N according to the model.	(2)
		(3)

Question 6 continued

Question 6 continued

Question 6 continued
(Total for Question 6 is 9 marks)

7.	The height of a river above a fixed point on the riverbed was monitored over a 7-day period.	
	The height of the river, H metres, t days after monitoring began, was given by	
	$H = \frac{\sqrt{t}}{20}(20 + 6t - t^2) + 17 \qquad 0 \leqslant t \leqslant 7$	
	Given that H has a stationary value at $t = \alpha$	
	(a) use calculus to show that α satisfies the equation	
	$5\alpha^2 - 18\alpha - 20 = 0$	(5)
	(b) Hence find the value of α , giving your answer to 3 decimal places.	(1)
	(c) Use further calculus to prove that H is a maximum at this value of α .	(2)

Question 7 continued
(Total for Question 7 is 8 marks)
(Total for Question 7 is 6 marks)

8.	(i)	A student writes the following statement:	
		"When a and b are consecutive prime numbers, $a^2 + b^2$ is never a multiple of 10"	
		Prove by counter example that this statement is not true.	
		Flove by counter example that this statement is not true.	(2)
	···		(-)
	(11)	Given that x and y are even integers greater than 0 and less than 6, prove by exhaustion, that	
		exhaustion, that	
		$1 < x^2 - \frac{xy}{4} < 15$	
		4	(3)
			(-)

Question 8 continued
(Total for Question 8 is 5 marks)

9. In this question you must show all stages of your working.	
Solutions relying entirely on calculator technology are not acceptable.	
(a) Show that	
$3\cos\theta(\tan\theta\sin\theta+3)=11-5\cos\theta$	
may be written as	
$3\cos^2\theta - 14\cos\theta + 8 = 0$	(3)
(b) Hence solve, for $0 < x < 360^{\circ}$	` ,
$3\cos 2x(\tan 2x\sin 2x + 3) = 11 - 5\cos 2x$	
giving your answers to one decimal place.	(4)

Question 9 continued

Question 9 continued

Question 9 continued
(Total for Question 9 is 7 marks)
(

10. The curve C has equation

$$y = \frac{(x-k)^2}{\sqrt{x}} \qquad x > 0$$

where k is a **positive** constant.

(a) Show that

$$\int_{1}^{16} \frac{(x-k)^2}{\sqrt{x}} \, \mathrm{d}x = ak^2 + bk + \frac{2046}{5}$$

where a and b are integers to be found.

(5)

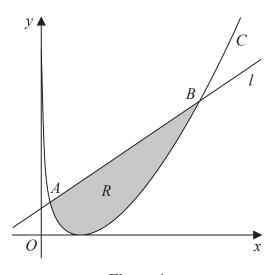


Figure 1

Figure 1 shows a sketch of the curve C and the line l.

Given that l intersects C at the point A(1, 9) and at the point B(16, q) where q is a constant,

(b) show that k = 4

(2)

The region R, shown shaded in Figure 1, is bounded by C and l

Using the answers to parts (a) and (b),

(c) find the area of region R

(3)

Question 10 continued

Question 10 continued

Question 10 continued
(Total for Question 10 is 10 marks)
(Total for Question to is to marks)

11. A sequence u_1, u_2, u_3, \dots is defined by	
$u_{n+1} = b - au_n$	
$u_1 = 3$	
where a and b are constants.	
(a) Find, in terms of a and b ,	
(i) u_2	
(ii) u_3	(2)
Given	
$\bullet \qquad \sum_{n=1}^{3} u_n = 153$	
• $b=a+9$	
(b) show that	
$a^2 - 5a - 66 = 0$	(3)
(c) Hence find the larger possible value of u_2	
	(2)
	(3)
	(3)
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Question 11 continued	
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Question 11 continued		
	(Total for Question 11 is 8 marks)	
	TOTAL FOR PAPER IS 75 MARKS	

Please check the examination details below before entering your candidate information		
Candidate surname	Other names	
Centre Number Candidate Number Pearson Edexcel Internation	nal Advanced Level	
Friday 13 October 2023		
Afternoon (Time: 1 hour 30 minutes) Paper reference	wMA12/01	
Mathematics		
International Advanced Subsidia Pure Mathematics P2	ry/Advanced Level	
You must have: Mathematical Formulae and Statistical Tables (Yo	ellow), calculator	

Candidates may use any calculator permitted by Pearson regulations.

Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
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- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each guestion.

Advice

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- Try to answer every question.
- Check your answers if you have

end end

Turn over ▶

- 1. Given that a, b and c are integers greater than 0 such that
 - c = 3a + 1
 - a + b + c = 15

prove, by exhaustion, that the product abc is always a multiple of 4

You may use the table below to illustrate your answer.

(3)

You may not need to use all rows of this table.

a	b	С	abc

Question 1 continued	
(Total for	Question 1 is 3 marks)

2.	A sequence u_1, u_2, u_3, \dots is defined by	
	$u_1 = 3$	
	$u_{n+1} = 2 - \frac{4}{u_n}$	
	(a) Find the value of u_2 , the value of u_3 and the value of u_4	
	(b) Find the value of	(3)
	$\sum_{i} u_{r}$	
	r=1	(2)

Question 2 continued
(Total for Question 2 is 5 marks)

3.	In this question you must show all stages of your working.	
	Solutions relying entirely on calculator technology are not acceptable.	
	(a) Solve, for $0 < \theta \leqslant 360^{\circ}$ the equation	
	$2\tan\theta + 3\sin\theta = 0$	
	giving your answers, as appropriate, to one decimal place.	(5)
	(b) Hence, or otherwise, find the smallest positive solution of	
	$2\tan(2x+40^\circ)+3\sin(2x+40^\circ)=0$	
	giving your answer to one decimal place.	(2)
		(2)

Question 3 continued	
	(Total for Question 3 is 7 marks)

4.	In this question you must show all stages of your working.	
	Solutions relying on calculator technology are not acceptable.	
	$f(x) = 4x^3 + ax^2 - 29x + b$	
	where a and b are constants.	
	Given that $(2x + 1)$ is a factor of $f(x)$,	
	(a) show that	
	a + 4b = -56	(2)
	Given also that when $f(x)$ is divided by $(x-2)$ the remainder is -25	
	(b) find a second simplified equation linking a and b .	(2)
	(c) Hence, using algebra and showing your working,	
	(i) find the value of a and the value of b ,	
	(ii) fully factorise $f(x)$.	(5)

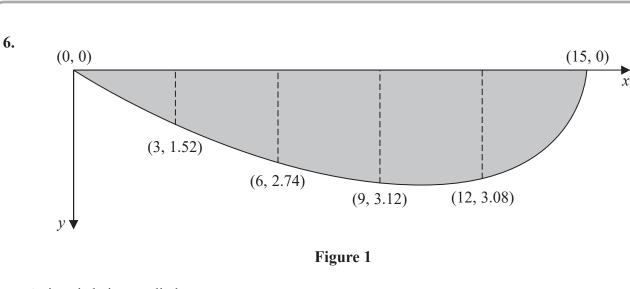
Question 4 continued

Question 4 continued

Question 4 continued
(Total for Question 4 is 9 marks)

5.	In this question you must show all stages of your working.	
	Solutions relying entirely on calculator technology are not acceptable.	
(i)	Solve	
(1)		
	$3^a = 70$	
	giving the answer to 3 decimal places.	(2)
(ii)	Find the exact value of b such that	(-)
(11)		
	$4 + 3\log_3 b = \log_3 5b$	(4)

Question 5 continued		
(Total for Question 5 is 6 marks)		



A river is being studied.

At one particular place, the river is 15 m wide.

The depth, y metres, of the river is measured at a point x metres from one side of the river.

Figure 1 shows a plot of the cross-section of the river and the coordinate values (x, y)

(a) Use the trapezium rule with all the y values given in Figure 1 to estimate the cross-sectional area of the river.

(3)

The water in the river is modelled as flowing at a constant speed of 1.5 m s⁻¹ across the whole of the cross-section.

(b) Use the model and the answer to part (a) to estimate the volume of water flowing through this section of the river each minute, giving your answer in m³ to 2 significant figures.

(2)

Assuming the model,

(c)	state, giving a reason for your answer, whether your answer for part (b) is an
	overestimate or an underestimate of the true volume of water flowing through this
	section of the river each minute.

(1)

Question 6 continued		
(Total for Question 6 is 6 marks)		

7.

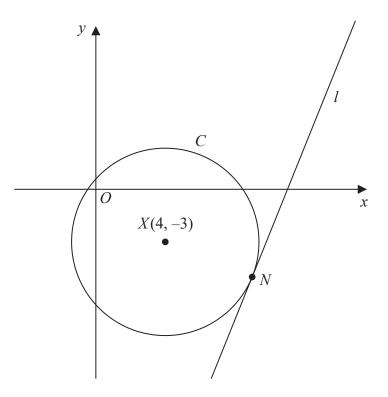


Figure 2

Figure 2 shows a sketch of

- the circle C with centre X(4, -3)
- the line *l* with equation $y = \frac{5}{2}x \frac{55}{2}$

Given that l is the tangent to C at the point N,

(a) show that an equation for the straight line passing through X and N is

$$2x + 5y + 7 = 0$$

(3)

- (b) Hence find
 - (i) the coordinates of N,
 - (ii) an equation for C.

(5)

Question 7 continued		

Question 7 continued		

Question 7 continued		
(Total for Question 7 is 8 marks)		

8.	In a large theatre there are n rows of seats, where n is a constant.	
	The number of seats in the first row is a , where a is a constant.	
	In each subsequent row there are 4 more seats than in the previous row so that	
	• in the 2nd row there are $(a + 4)$ seats	
	• in the 3rd row there are $(a + 8)$ seats	
	• the number of seats in each row form an arithmetic sequence	
	Given that the total number of seats in the first 10 rows is 360	
	(a) find the value of a.	
		(2)
	Given also that the total number of seats in the n rows is 2146	
	(b) show that	
	$n^2 + 8n - 1073 = 0$	(2)
	(c) Hence	(-)
	(i) state the number of rows of seats in the theatre,	
	(ii) find the maximum number of seats in any one row.	
	(ii) This the maximum number of seats in any one low.	(3)

Question 8 continued		

Question 8 continued		

Question 8 continued		
	Total for Question 8 is 7 marks)	

9.

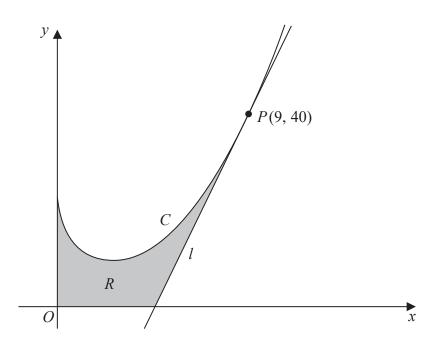


Figure 3

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

Figure 3 shows a sketch of part of the curve C with equation

$$y = \frac{2}{3}x^2 - 9\sqrt{x} + 13 \qquad x \geqslant 0$$

(a) Find, using calculus, the range of values of x for which y is increasing.

(4)

The point P lies on C and has coordinates (9, 40).

The line *l* is the tangent to *C* at the point *P*.

The finite region R, shown shaded in Figure 3, is bounded by the curve C, the line l, the x-axis and the y-axis.

(b) Find, using calculus, the exact area of R.

(8)

Question 9 continued		

Question 9 continued	

Question 9 continued	
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(Total for Question 9 is 12 marks)	_

10. (i) (a) Find, in ascending powers of x, the 2nd, 3rd and 5th terms of the binomial expansion of	
$(3+2x)^6$	(3)
For a particular value of x , these three terms form consecutive terms in a geometric series.	
(b) Find this value of x.	(3)
(ii) In a different geometric series,	
• the first term is $\sin^2 \theta$	
• the common ratio is $2\cos\theta$	
• the sum to infinity is $\frac{8}{5}$	
(a) Show that	
$5\cos^2\theta - 16\cos\theta + 3 = 0$	(3)
(b) Hence find the exact value of the 2nd term in the series.	(2)
	(3)

Question 10 continued

Question 10 continued

Question 10 continued

Question 10 continued	
(Total for O 10 to 12 1)	
(Total for Question 10 is 12 marks)	
TOTAL FOR PAPER IS 75 MARKS	

Please check the examination details below before ent	ering your candidate information
Candidate surname	Other names
Centre Number Candidate Number Pearson Edexcel Internation	nal Advanced Level
Tuesday 16 January 2024	
Afternoon (Time: 1 hour 30 minutes) Paper reference	wMA12/01
Mathematics	
International Advanced Subsidiar Pure Mathematics P2	ry/Advanced Level
You must have: Mathematical Formulae and Statistical Tables (Ye	ellow), calculator

Candidates may use any calculator permitted by Pearson regulations.

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Instructions

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Information

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Advice

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- Try to answer every question.
- Check your answers if you have



Turn over ▶

1.	$f(x) = ax^3 + 3x^2 - 8x + 2$ where a is a constant	
	Given that when $f(x)$ is divided by $(x-2)$ the remainder is 3, find the value of a .	
	Given that when $I(x)$ is divided by $(x-2)$ the remainder is 3, find the value of a .	(3)
		(-)

Question 1 continued	
(Total for	Question 1 is 3 marks)

2.	Find the coefficient of the term in x^7 of the binomial expansion of	
	$\left(\frac{3}{8}+4x\right)^{12}$	
	giving your answer in simplest form.	(3)

Question 2 continued
(Total for Question 2 is 3 marks)

3.	The circle C	
	• has centre $A(3, 5)$	
	• passes through the point $B(8, -7)$	
	(a) Find an equation for C.	(2)
		(3)
	The points M and N lie on C such that MN is a chord of C .	
	Given that MN	
	• lies above the <i>x</i> -axis	
	• is parallel to the <i>x</i> -axis	
	• has length $4\sqrt{22}$	
	(b) find an equation for the line passing through points M and N .	(3)
		(3)

Question 3 continued
(Total for Question 3 is 6 marks)

4. (a) Sketch the curve with equation

$$y = a^{-x} + 4$$

where a is a constant and a > 1

On your sketch show

- the coordinates of the point of intersection of the curve with the y-axis
- the equation of the asymptote to the curve.

(3)

х	-4	-1.5	1	3.5	6	8.5
у	13	6.280	4.577	4.146	4.037	4.009

The table above shows corresponding values of x and y for $y = 3^{-\frac{1}{2}x} + 4$

The values of y are given to four significant figures, as appropriate.

Using the trapezium rule with all the values of *y* in the table,

(b) find an approximate value for

$$\int_{-4}^{8.5} \left(3^{-\frac{1}{2}x} + 4 \right) \mathrm{d}x$$

giving your answer to two significant figures.

(3)

(c) Using the answer to part (b), find an approximate value for

(i)
$$\int_{-4}^{8.5} \left(3^{-\frac{1}{2}x}\right) dx$$

(ii)
$$\int_{-4}^{8.5} \left(3^{-\frac{1}{2}x} + 4 \right) dx + \int_{-8.5}^{4} \left(3^{\frac{1}{2}x} + 4 \right) dx$$

(3)

Question 4 continued	

Question 4 continued

Question 4 continued
(Total for Question 4 is 9 marks)
(Local for Question 1 is 7 marks)

5. (i) Find the value of	
$\sum_{r=1}^{\infty} 6 \times \left(0.25\right)^r$	
	(3)
(ii) A sequence $u_1, u_2, u_3,$ is defined by	
$u_1 = 3$ $u_{n+1} = \frac{u_n - 3}{u_n - 2} \qquad n \in \mathbb{N}$	
(a) Show that this sequence is periodic.	(2)
(b) State the order of this sequence.	(1)
(c) Hence find	
$\sum_{n=1}^{70} u_n$	
	(2)

Question 5 continued

Question 5 continued

Question 5 continued
(Total for Question 5 is 8 marks)

6. (a) Given that	
$2\log_4(x+3) + \log_4 x = \log_4(4x+2) + \frac{1}{2}$	
show that	
$x^3 + 6x^2 + x - 4 = 0$	(4)
(b) Given also that −1 is a root of the equation	
$x^3 + 6x^2 + x - 4 = 0$	
(i) use algebra to find the other two roots of the equation.	(3)
(ii) Hence solve	
$2\log_4(x+3) + \log_4 x = \log_4(4x+2) + \frac{1}{2}$	
	(1)

Question 6 continued

Question 6 continued

Question 6 continued
(Total for Question 6 is 8 marks)

7.	Wheat is grown on a farm.	
	• In year 1, the farm produced 300 tonnes of wheat.	
	• In year 12, the farm is predicted to produce 4000 tonnes of wheat.	
	Model A assumes that the amount of wheat produced on the farm will increase by the same amount each year.	
	(a) Using model A, find the amount of wheat produced on the farm in year 4. Give your answer to the nearest 10 tonnes.	(3)
	Model <i>B</i> assumes that the amount of wheat produced on the farm will increase by the same percentage each year.	
	(b) Using model <i>B</i> , find the amount of wheat produced on the farm in year 2. Give your answer to the nearest 10 tonnes.	(3)
	(c) Calculate, according to the two models, the difference between the total amounts of wheat predicted to be produced on the farm from year 1 to year 12 inclusive. Give your answer to the nearest 10 tonnes.	
		(3)

Question 7 continued

Question 7 continued

Question 7 continued
(Total for Question 7 is 9 marks)

8. (i) Use a counter example to show that the following statement is false	
" $n^2 + 3n + 1$ is prime for all $n \in \mathbb{N}$ "	
	(2)
(ii) Use algebra to prove by exhaustion that for all $n \in \mathbb{N}$	
" $n^2 - 2$ is not a multiple of 4"	
	(4)

Question 8 continued
(Total for Question 8 is 6 marks)
(Total for Question 6 is 6 marks)

9. In this question you must show detailed reasoning.

Solutions relying entirely on calculator technology are not acceptable.

(i) Solve, for $0 \le x < 360^{\circ}$, the equation

$$\sin x \tan x = 5$$

giving your answers to one decimal place.

(6)

(ii)

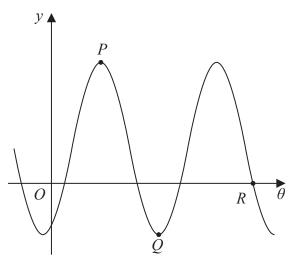


Figure 1

Figure 1 shows a sketch of part of the curve with equation

$$y = A\sin\left(2\theta - \frac{3\pi}{8}\right) + 2$$

where A is a constant and θ is measured in radians.

The points P, Q and R lie on the curve and are shown in Figure 1.

Given that the y coordinate of P is 7

(a) state the value of A,

(1)

(b) find the exact coordinates of Q,

(3)

(c) find the value of θ at R, giving your answer to 3 significant figures.

(4)

Question 9 continued

Question 9 continued

Question 9 continued	
	(Total for Question 9 is 14 marks)

10. In this question you must show detailed reasoning.

Solutions relying entirely on calculator technology are not acceptable.

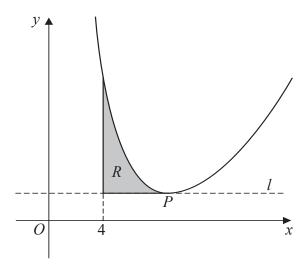


Figure 2

Figure 2 shows a sketch of the curve with equation

$$y = \frac{1}{2}x^2 + \frac{1458}{\sqrt{x^3}} - 74 \qquad x > 0$$

The point *P* is the only stationary point on the curve.

(a) Use calculus to show that the x coordinate of P is 9

(4)

The line l passes through the point P and is parallel to the x-axis.

The region R, shown shaded in Figure 2, is bounded by the curve, the line l and the line with equation x = 4

(b) Use algebraic integration to find the exact area of R.

(5)

Question 10 continued

Question 10 continued	
(Total for Question 10 is 9 n	narks)
TOTAL FOR PAPER IS 75 MA	ARKS

Please check the examination details below	v before entering your candidate information
Candidate surname	Other names
Centre Number Candidate Nur	
Pearson Edexcel Intern	ational Advanced Level
Tuesday 14 May 202	4
Morning (Time: 1 hour 30 minutes)	Paper reference WMA12/01
Mathematics	×10
International Advanced Su Pure Mathematics P2	bsidiary/Advanced Level
You must have: Mathematical Formulae and Statistical	Tables (Yellow), calculator

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- Answer the questions in the spaces provided
 - there may be more space than you need.
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Information

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- The marks for each question are shown in brackets
 use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

1. (a) Find the first four terms, in ascending powers of x , of the binomial expansion of	
$\left(1-\frac{1}{6}x\right)^9$	
giving each term in simplest form.	(3)
(b) Hence find the coefficient of x^3 in the expansion of	
$(10x+3)\left(1-\frac{1}{6}x\right)^9$	
giving the answer in simplest form.	(2)

Question 1 continued
(Total for Question 1 is 5 marks)

2.	In this question you must show all stages of your working. Solutions relying entirely on calculator technology are not acceptable.	
	In an arithmetic series,	
	• the sixth term is 2	
	• the sum of the first ten terms is -80	
	For this series,	
	(a) find the value of the first term and the value of the common difference.	
		(4)
	(b) Hence find the smallest value of <i>n</i> for which	
	$S_n > 8000$	(3)

Question 2 continued
(Total for Question 2 is 7 marks)

3.		In this question you must show all stages of your working. Solutions relying entirely on calculator technology are not acceptable.	
	(i)	Using the laws of logarithms, solve	
		$2\log_2(2-x) = 4 + \log_2(x+10)$	(5)
	(ii)	Find the value of	
		$\log_{\sqrt{a}}a^6$	
		where a is a positive constant greater than 1	
			(1)

Question 3 continued
(Total for Question 3 is 6 marks)

4.	$f(x) = (x-2)(2x^2 + 5x + k) + 21$	
	where k is a constant.	
	(a) State the remainder when $f(x)$ is divided by $(x-2)$	(1)
	Given that $(2x-1)$ is a factor of $f(x)$	
	(b) show that $k = 11$	(2)
	(c) Hence	
	(i) fully factorise $f(x)$,	
	(ii) find the number of real solutions of the equation	
	f(x) = 0	
	giving a reason for your answer.	(5)

Question 4 continued

Question 4 continued

Question 4 continued
(Total for Question 4 is 8 marks)

5.		In this question you must show detailed reasoning.	
J.	(a)		
	(a)	Given that x and y are positive numbers such that	
		$(x-y)^3 > x^3 - y^3$	
		prove that	
		y > x	
		(4)	
	(b)	Using a counter example, show that the result in part (a) is not true for all real numbers.	
		(2)	
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Question 5 continued
(Total for Question 5 is 6 marks)

6. (a) Sketch the curve with equation

$$y = a^x + 4$$

where a is a positive constant greater than 1

On your sketch, show

- the coordinates of the point of intersection of the curve with the y-axis
- the equation of the asymptote of the curve

(3)

х	2	2.3	2.6	2.9	3.2	3.5
У	0	0.3246	0.8629	1.6643	2.7896	4.3137

The table shows corresponding values of x and y for

$$y = 2^x - 2x$$

with the values of y given to 4 decimal places as appropriate.

Using the trapezium rule with all the values of y in the given table,

(b) obtain an estimate for $\int_{2}^{3.5} (2^{x} - 2x) dx$, giving your answer to 2 decimal places. (3)

(c) Using your answer to part (b) and making your method clear, estimate

$$(i) \quad \int_2^{3.5} \left(2^x + 2x\right) \mathrm{d}x$$

(ii)
$$\int_{2}^{3.5} \left(2^{x+1} - 4x\right) dx$$

(3)

Question 6 continued	,
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Question 6 continued

Question 6 continued
(Total for Question 6 is 9 marks)

7. The circle C_1 has equation	
$x^2 + y^2 + 8x - 10y = 29$	
(a) (i) Find the coordinates of the centre of C_1	
(ii) Find the exact value of the radius of C_1	(2)
In part (b) you must show detailed reasoning.	(3)
The circle C_2 has equation	
$(x-5)^2 + (y+8)^2 = 52$	
(b) Prove that the circles C_1 and C_2 neither touch nor intersect.	
	(3)

Question 7 continued

Question 7 continued		

Question 7 continued		
(Total for Question 7 is 6 marks)		

•	In this question you must show all stages of your working. Solutions relying entirely on calculator technology are not acceptable.	
(i)	Solve, for $0 < x \le \pi$, the equation	
	$5\sin x \tan x + 13 = \cos x$	
	giving your answer in radians to 3 significant figures.	(5)
(ii)	The temperature inside a greenhouse is monitored on one particular day.	
	The temperature, H° C, inside the greenhouse, t hours after midnight, is modelled by the equation	
	$H = 10 + 12\sin(kt + 18)^{\circ} \qquad 0 \le t < 24$	
	where k is a constant.	
	Use the equation of the model to answer parts (a) to (c).	
	Given that	
	• the temperature inside the greenhouse was 20 °C at 6 am	
	• 0 < k < 20	
	(a) find all possible values for k , giving each answer to 2 decimal places.	(4)
	Given further that $0 < k < 10$	
	(b) find the maximum temperature inside the greenhouse,	(1)
	(c) find the time of day at which this maximum temperature occurs.	
	Give your answer to the nearest minute.	(2)

Question 8 continued

Question 8 continued		
(Total for Question 8 is 12 marks)		

9.

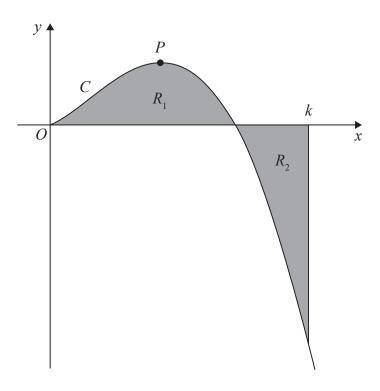


Figure 1

Figure 1 is a sketch of the curve C with equation

$$y = 2x^{\frac{3}{2}} (4 - x) \qquad x \geqslant 0$$

The point P is the stationary point of C.

(a) Find, using calculus, the x coordinate of P.

(4)

The region R_1 , shown shaded in Figure 1, is bounded by C and the x-axis.

The region R_2 , also shown shaded in Figure 1, is bounded by C, the x-axis and the line with equation x = k, where k is a constant.

Given that the area of R_1 is equal to the area of R_2

(b) find, using calculus, the exact value of k.

(4)

Question 9 continued			

Question 9 continued

Question 9 continued		
(Total for Question 9 is 8 marks)		

10.	In this question you must show all stages of your working.	
10.	Solutions relying entirely on calculator technology are not acceptable.	
,	The number of dormice and the number of voles on an island are being monitored.	
]	Initially there are 2000 dormice on the island.	
	A model predicts that the number of dormice will increase by 3% each year, so that the numbers of dormice on the island at the end of each year form a geometric sequence.	
((a) Find, according to the model, the number of dormice on the island 6 years after monitoring began. Give your answer to 3 significant figures.	(2)
,	The number of voles on the island is being monitored over the same period of time.	
•	Given that 4 years after monitoring began there were 3690 voles on the island 7 years after monitoring began there were 3470 voles on the island the number of voles on the island at the end of each year is modelled as a geometric sequence	
((b) find the equation of this model in the form	
	$N = ab^t$	
	where N is the number of voles, t years after monitoring began and a and b are constants. Give the value of a and the value of b to 2 significant figures.	(3)
	When $t = T$, the number of dormice on the island is equal to the number of voles on the island.	
((c) Find, according to the models, the value of <i>T</i> , giving your answer to	
	one decimal place.	(3)

Question 10 continued			
Question 10 continued			

Question 10 continued		
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(Total for Question 10 is 8 marks)	_	
TOTAL FOR PAPER IS 75 MARKS		

Please check the examination details below before entering your candidate information		
Candidate surname	Other names	
Centre Number Candidate Nu	mber	
Pearson Edexcel Inter	national Advanced Level	
Tuesday 15 October	2024	
Morning (Time: 1 hour 30 minutes)	Paper reference WMA12/01	
Mathematics	0	
International Advanced Su Pure Mathematics P2	ıbsidiary/Advanced Level	
You must have: Mathematical Formulae and Statistical	Tables (Yellow), calculator	

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use black ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 11 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer cross it out and put your new answer and any like it is the control of the control o

Turn over

1. A continuous curve has equation y = f(x).

A table of values of x and y for y = f(x) is shown below.

х	0.5	1.75	3	4.25	5.5
у	3.479	6.101	7.448	6.823	5.182

Using the trapezium rule with all the values of y in the given table,

(a) find an estimate for

$$\int_{0.5}^{5.5} f(x) dx$$

giving your answer to one decimal place.

(3)

(b) Using your answer to part (a) and making your method clear, estimate

$$\int_{0.5}^{5.5} \left(f\left(x\right) + 4x \right) dx$$

(2)

Question 1 continued
(Total for Ougstion 1 is 5 marks)
(Total for Question 1 is 5 marks)

2.	A sequence of numbers u_1, u_2, u_3, \dots is defined by	
	$u_1 = 7$	
	$u_{n+1} = (-1)^n u_n + k$	
	where k is a constant.	
	(a) Show that $u_5 = 7$ Given that $\sum_{r=1}^{4} u_r = 30$	(3)
	(b) find the value of k .	(2)
	(c) Hence find the value of $\sum_{r=1}^{150} u_r$	(2)

Question 2 continued
(Total for Question 2 is 7 marks)

3.	$f(x) = 2x^3 - x^2 + Ax + B$	
	where A and B are integers.	
	Given that when $f(x)$ is divided by $(x + 3)$ the remainder is 55	
	(a) show that	
	3A - B = -118	
		(2)
	Given also that $(2x - 5)$ is a factor of $f(x)$,	
	(b) find the value of A and the value of B.	
		(3)
	(c) Hence find the quotient when $f(x)$ is divided by $(x - 7)$	(2)
		(2)

Question 3 continued

Question 3 continued

Question 3 continued
(Total for Question 3 is 7 marks)

4.	In this question you must show all stages of your working.	
	Solutions relying entirely on calculator technology are not acceptable.	
	The curve C has equation	
	$y = 4x^{\frac{1}{2}} + 9x^{-\frac{1}{2}} + 3 \qquad x > 0$	
	(a) Find $\frac{dy}{dx}$ giving each term in simplest form.	(2)
	(b) Hence find the x coordinate of the stationary point of C.	(2)
	(c) (i) Find $\frac{d^2y}{dx^2}$ giving each term in simplest form.	
	(ii) Hence determine the nature of the stationary point of <i>C</i> , giving a reason for your answer.	
		(2)
	(d) State the range of values of x for which y is decreasing.	(1)

Question 4 continued
(Total for Question 4 is 7 marks)
(Total for Question 4 is / marks)

5.	(a) Find, in terms of <i>a</i> , the first 3 terms, in ascending powers of <i>x</i> , of the binomial expansion of	
	$(2+ax)^6$	
	where a is a non-zero constant. Give each term in simplest form.	(3)
	$f(x) = \left(3 + \frac{1}{x}\right)^2 \left(2 + ax\right)^6$	
	Given that the constant term in the expansion of $f(x)$ is 576	
	(b) find the value of a.	(4)

Question 5 continued		
(Total for Question 5 is 7 marks)		

6.	In this question you must show all stages of your working.	
	Solutions relying entirely on calculator technology are not acceptable.	
	Using the laws of logarithms, solve	
	$\log_4(12 - 2x) = 2 + 2\log_4(x + 1)$	(5)
		(5)

Question 6 continued		
(Total for Question 6 is 5 marks)		

7.	Jem pays money into a savings scheme, A, over a period of 300 months.	
	Jem pays £20 into scheme A in month 1, £20.50 in month 2, £21 in month 3 and so on, so that the amounts Jem pays each month form an arithmetic sequence.	
	(a) Show that Jem pays £69.50 into scheme A in month 100	(1)
		(1)
	(b) Find the total amount that Jem pays into scheme A over the period of 300 months.	(2)
	Kim pays money into a different savings scheme, <i>B</i> , over the same period of 300 months.	
	In a model, the amounts Kim pays into scheme <i>B</i> increase by the same percentage each month, so that the amounts Kim pays each month form a geometric sequence.	
	Given that Kim pays	
	• £20 into scheme <i>B</i> in month 1	
	• £250 into scheme <i>B</i> in month 300	
	(c) use the model to calculate, to the nearest £10, the difference between the total amount paid into scheme A and the total amount paid into scheme B over the period of 300 months.	
	of 500 mondis.	(3)

Question 7 continued		

Question 7 continued		

Question 7 continued		
(Total for Overtion 7 is 6 marks)		
(Total for Question 7 is 6 marks)		

8. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

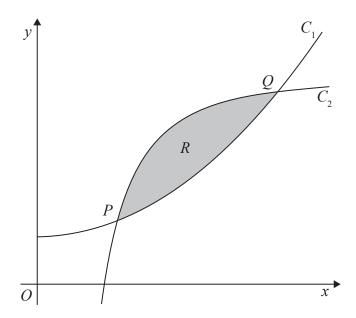


Figure 1

Figure 1 shows a sketch of part of the curve C_1 with equation

$$y = x^2 + 3 \qquad x > 0$$

and part of the curve C_2 with equation

$$y = 13 - \frac{9}{x^2}$$
 $x > 0$

The curves C_1 and C_2 intersect at the points P and Q as shown in Figure 1.

(a) Use algebra to find the x coordinate of P and the x coordinate of Q.

(4)

The finite region R, shown shaded in Figure 1, is bounded by C_1 and C_2

(b) Use algebraic integration to find the exact area of R.

(4)

Question 8 continued		

Question 8 continued		

Question 8 continued		
(Total for Question 8 is 8 marks)		

9.	In this question you must show detailed reasoning.	
	Solutions relying entirely on calculator technology are not acceptable.	
	(a) Show that the equation	
	$2\tan\theta = 3\cos\theta$	
	can be written as	
	$3\sin^2\theta + 2\sin\theta - 3 = 0$	(3)
	(b) Hence solve, for $-\pi < x < \pi$, the equation	` ,
	$2\tan\left(2x + \frac{\pi}{3}\right) = 3\cos\left(2x + \frac{\pi}{3}\right)$	
	giving your answers to 3 significant figures.	(4)

Question 9 continued
(Total for Question 9 is 7 marks)

10. The circle C has equation	
$x^2 + y^2 + 4x - 30y + 209 = 0$	
(a) Find	
(i) the coordinates of the centre of C,	
(ii) the exact value of the radius of C .	(3)
The line L has equation $y = mx + 1$, where m is a constant.	
Given that L is the tangent to C at the point P ,	
(b) show that	
$2m^2 - 7m - 22 = 0$	
	(3)
(c) Hence find the possible pairs of coordinates of P .	(4)

Question 10 continued

Question 10 continued

Question 10 continued
(Total for Question 10 is 10 marks)

11. (i) Prove by counter example that the statement	
"If <i>n</i> is a prime number then $3^n + 2$ is also a prime number."	
is false. (2)	
(ii) Use proof by exhaustion to prove that if <i>m</i> is an integer that is not divisible by 3, then	
m^2-1	
is divisible by 3 (4)	

Question 11 continued

Question 11 continued
(Total for Question 11 is 6 marks)
TOTAL FOR PAPER IS 75 MARKS