

Pearson Edexcel

A Level Mathematics 9MA0

Unit Test

1 Proof

Time allowed: 50 minutes

School:

Name:

Teacher:

| Question | Points | Score |
|----------|--------|-------|
| 1 | 4 | |
| 2 | 3 | |
| 3 | 5 | |
| 4 | 5 | |
| 5 | 4 | |
| 6 | 4 | |
| 7 | 4 | |
| 8 | 5 | |
| 9 | 10 | |
| 10 | 6 | |
| Total: | 50 | |



1. It is suggested that the sequence $a_k = 2^k + 1, k \geq 1$ produces only prime numbers.

(a) Show that a_1, a_2 and a_4 produce prime numbers. [2]

(b) Prove by counter example that the sequence does not always produce a prime number. [2]

Total: 4



2. Prove by exhaustion that

[3]

$$1 + 2 + 3 + \cdots + n \equiv \frac{n(n+1)}{2}$$

for positive integers from 1 to 6 inclusive.



3. Use proof by contradiction to prove the statement: ‘The product of two odd numbers is odd.’ [5]



4. Prove by contradiction that if n is odd, $n^3 + 1$ is even.

[5]



5. Use proof by contradiction to show that there exist no integers a and b for which $25a + 15b = 1$. [4]



6. Use proof by contradiction to show that there is no greatest positive rational number.

[4]



7. Use proof by contradiction to show that, given a rational number a and an irrational number b , $a - b$ is irrational. [4]



8. Use proof by contradiction to show that there are no positive integer solutions to the statement [5]
- $$x^2 - y^2 = 1.$$



9. (a) Use proof by contradiction to show that if n^2 is an even integer then n is also an even integer. [4]

(b) Prove that $\sqrt{2}$ is irrational. [6]

Total: 10



10. Prove by contradiction that there are infinitely many prime numbers.

[6]

