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| Question | Answer | Marks | Guidance |
|----------|---|-------|---|
| 1 | $6C2 \times (2x)^4 \times \frac{1}{(4x^2)^2}$ | B1 | SOI SC: Condone errors in $(4^{-1})^2$ evaluation or interpretation for B1 only |
| | $15 \times 2^4 \times \frac{1}{4^2}$ | B1 | Identified as required term. |
| | 15 | B1 | |
| | | 3 | |

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|----------|--|-------|-----------------------------|
| 2 | Attempt to solve $f'(x) = 0$ or $f'(x) > 0$ or $f'(x) \ge 0$ | M1 | SOI |
| | (x-2)(x-4) | A1 | 2 and 4 seen |
| | (Least possible value of n is) 4 | A1 | Accept $n = 4$ or $n \ge 4$ |
| | | 3 | |

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|----------|--|----------|--|
| 3 | $\frac{\mathrm{d}y}{\mathrm{d}x} = 6x^2 - 10x - 3$ | B1 | |
| | At $x = 2$, $\frac{dy}{dx} = 24 - 20 - 3 = 1 \rightarrow a = 1$ | M1 A1 | |
| | $6 = 2 + b \longrightarrow b = 4$ | B1FT | Substitute $x = 2$, $y = 6$ in $y = (their a)x + b$ |
| | $6 = 16 - 20 - 6 + c \rightarrow c = 16$ | B1 | Substitute $x = 2, y = 6$ into equation of curve |
| | | 5 | |

| Question | Answer | Marks | Guidance |
|----------|---|----------|--|
| 4(i) | Identifies common ratio as 1.1 | B1 | |
| | Use of $x(1.1)^{20} = 20$ | M1 | SOI |
| | $x\left(=\frac{20}{(1.1)^{20}}\right)=3.0$ | A1 | Accept 2.97 |
| | | 3 | |
| 4(ii) | $their 3.0 \times \frac{\left[\left(1.1 \right)^{21} - 1 \right]}{1.1 - 1} \to 192$ | M1 A1 | Correct formula used for M mark. Allow 2.97 used from (i) Accept 190 from $x = 2.97$ |
| | | 2 | |

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<u>9709_w19_ms_</u>11

| Question | Answer | Marks | Guidance |
|----------|--|------------|--|
| 5(i) | $4\tan x + 3\cos x + \frac{1}{\cos x} = 0 \rightarrow 4\sin x + 3\cos^2 x + 1 = 0$ | M1 | Multiply by $\cos x$ or common denominator of $\cos x$ |
| | $4\sin x + 3(1 - \sin^2 x) + 1 = 0 \implies 3\sin^2 x - 4\sin x - 4 = 0$ | M1 | Use $\cos^2 x = 1 - \sin^2 x$ and simplify to 3-term quadratic in $\sin x$ |
| | $\sin x = -\frac{2}{3}$ | A1 | AG |
| | | 3 | |
| 5(ii) | $2x - 20^\circ = 221.8^\circ, 318.2^\circ$ | M1A1 | Attempt to solve $sin(2x-20) = -2/3(M1)$. At least 1 correct (A1) |
| | $x = 120.9^{\circ}, 169.1^{\circ}$ | A1 A1FT | FT for 290° – other solution. SC A1 both answers in radians |
| | | 4 | |

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|----------|--|-------|----------|
| 6 | Equation of line is $y = mx - 2$ | B1 | OR |
| | $x^{2} - 2x + 7 = mx - 2 \rightarrow x^{2} - x(2 + m) + 9 = 0$ | M1 | |
| | Apply $b^2 - 4ac(=0) \rightarrow (2+m)^2 - 4 \times 9 (=0)$ | *M1 | |
| | m = 4 or -8 | A1 | |
| | $m = 4 \rightarrow x^2 - 6x + 9 = 0 \rightarrow x = 3$ $m = -8 \rightarrow x^2 + 6x + 9 = 0 \rightarrow x = -3$ | DM1 | |
| | (3, 10), (-3, 22) | A1A1 | |
| | Alternative method for question 6 | | |
| | $\frac{\mathrm{d}y}{\mathrm{d}x} = 2x - 2$ | B1 | |
| | 2x - 2 = m | M1 | |
| | $x^{2} - 2x + 7 = (2x - 2)x - 2 = 2x^{2} - 2x - 2$ | M1 | |
| | $x^2 - 9 = 0 \rightarrow x = \pm 3$ | A1 | |
| | (3, 10), (-3, 22) | A1A1 | |
| | When $x = 3$, $m = 4$; when $x = -3$, $m = -8$ | A1 | |
| | | 7 | |

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| Question | Answer | Marks | Guidance |
|----------|---|-------|---------------------------------------|
| 7(i) | Range of f is $0 < f(x) < 3$ | B1B1 | OE. Range cannot be defined using x |
| | Range of g is $g(x) > 2$ | B1 | OE |
| | | 3 | |
| 7(ii) | $(fg(x) =)\frac{3}{2(\frac{1}{x}+2)+1} = \frac{3x}{2+5x}$ | B1B1 | Second B mark implies first B mark |
| | | 2 | |
| 7(iii) | $y = \frac{3x}{2+5x} \rightarrow 2y + 5xy = 3x \rightarrow 3x - 5xy = 2y$ | M1 | Correct order of operations |
| | $x(3-5y)=2y \rightarrow x=\frac{2y}{3-5y}$ | M1 | Correct order of operations |
| | $((fg)^{-1}(x)) = \frac{2x}{3-5x}$ | A1 | |
| | | 3 | |

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|----------|--|-------|----------|
| 8(i) | $OA \times \frac{3}{8}\pi = 6$ | M1 | |
| | $OA = \frac{16}{\pi} = 5.093(0)$ | A1 | |
| 8(ii) | $AB = their 5.0930 \times \tan\frac{3}{16}\pi$ | M1 | |
| | Perimeter = $2 \times 3.4030 + 6 = 12.8$ | A1 | |
| 8(iii) | Area $OABC = (2 \times \frac{1}{2}) \times their 5.0930 \times their 3.4030$ | M1 | |
| | Area sector = $\frac{1}{2} \times (their 5.0930)^2 \times \frac{3}{8}\pi$ | M1 | |
| | Shaded area = $their 17.331 - their 15.279 = 2.05$ | M1A1 | |

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| | 9709 | w19 | ms | 11 |
|--|------|-----|----|----|
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| Question | Answer | Marks | Guidance |
|----------|--|----------|---|
| 9(i) | $y = [(5x-1)^{1/2} \div \frac{3}{2} \div 5] [-2x]$ | B1 B1 | |
| | $3 = \frac{27}{(3/2) \times 5} - 4 + c$ | M1 | Substitute $x = 2, y = 3$ |
| | $c = 7 - \frac{18}{5} = \frac{17}{5} \rightarrow \left(y = \frac{2(5x-1)^3}{15} - 2x + \frac{17}{5} \right)$ | A1 | |
| 9(ii) | $d^{2}y / dx^{2} = \left[\frac{1}{2}(5x - 1)^{-1/2}\right] [\times 5]$ | B1 B1 | |
| 9(iii) | $(5x-1)^{1/2} - 2 = 0 \implies 5x-1 = 4$ x = 1 | M1A1 | Set $\frac{dy}{dx} = 0$ and attempt solution (M1) |
| | $y = \frac{16}{25} - 2 + \frac{17}{5} = \frac{37}{15}$ | A1 | Or 2.47 or $\left(1, \frac{37}{15}\right)$ |
| | $\frac{\mathrm{d}^2 y}{\mathrm{d}x^x} = \frac{5}{2} \times \frac{1}{2} = \frac{5}{4} \ (>0) \text{ hence minimum}$ | A1 | OE |

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|----------|---|-------|--|
| 10(i) | $\mathbf{AB} = \begin{pmatrix} 2 \\ -3 \\ 5 \end{pmatrix} - \begin{pmatrix} -1 \\ 3 \\ -4 \end{pmatrix} = \begin{pmatrix} 3 \\ -6 \\ 9 \end{pmatrix}, \qquad \mathbf{BC} = \begin{pmatrix} 4 \\ -2 \\ 5 \end{pmatrix} - \begin{pmatrix} 2 \\ -3 \\ 5 \end{pmatrix} = \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix}$ | B1B1 | Condone reversal of labels |
| | AB.BC = $6 - 6 \rightarrow = 0$ (hence perpendicular) | B1 | AG |
| 10(ii) | $\mathbf{DC} = \begin{pmatrix} 4 \\ -2 \\ 5 \end{pmatrix} - \begin{pmatrix} 2 \\ 2 \\ -1 \end{pmatrix} = \begin{pmatrix} 2 \\ -4 \\ 6 \end{pmatrix}$ | B1 | Or: $\mathbf{C}\mathbf{D} = \begin{pmatrix} -2\\4\\-6 \end{pmatrix}$ |
| | $\mathbf{AB} = k\mathbf{DC}$ | M1 | OE Expect $k = \frac{3}{2}$ Or: DC.BC = 4 - 4 = 0 hence <i>BC</i> is also perpendicular to <i>DC</i> Or: AB.DC = 1 or AB.CD = -1, angle between lines is 0 or 180 |
| | <i>AB</i> is parallel to <i>DC</i> , hence <i>ABCD</i> is a trapezium | A1 | |
| 10(iii) | $ \mathbf{AB} = \sqrt{9 + 36 + 81} = \sqrt{126} = 11.22$ $ \mathbf{DC} = \sqrt{4 + 16 + 36} = \sqrt{56} = 7.483$ $ \mathbf{BC} = \sqrt{4 + 1 + 0} = \sqrt{5} = 2.236$ | M1 | Method for finding at least 2 magnitudes |
| | Area = $\frac{1}{2}$ (<i>theirAB</i> + <i>theirDC</i>)× <i>theirBC</i> = 20.92 | M1A1 | OE |

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|----------|--|-----------|--|
| 11(i) | $\left(y=\right)\left(x+2\right)^2-1$ | B1 DB1 | 2nd B1 dependent on 2 in bracket |
| | $x + 2 = (\pm)(y + 1)^{1/2}$ | M1 | |
| | $x = -2 + \left(y + 1\right)^{1/2}$ | A1 | |
| 11(ii) | $x^{2} = 4 + (y+1) - / + 4(y+1)^{\frac{1}{2}}$ | *M1A1 | SOI. Attempt to find x^2 . The last term can be – or + at this stage |
| | $(\pi) \int x^{2} (dy) = (\pi) \left[5y + \frac{y^{2}}{2} - \frac{4(y+1)^{\frac{3}{2}}}{\frac{3}{2}} \right]$ | A2,1,0 | |
| | $(\pi)\left[15+\frac{9}{2}-\frac{64}{3}-\left(-5+\frac{1}{2}\right)\right]$ | DM1 | Apply <i>y</i> limits |
| | $\frac{8\pi}{3}$ or 8.38 | A1 | |