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1	$V \sin \theta = \frac{2.4g}{2}$ or $48 = V \cos \theta \times 2.4$ $\tan \theta = \frac{12}{\frac{48}{2.4}}$ $\theta = 31(0)^\circ$	B1 M1 A1	[3]	$-V \sin \theta = V \sin \theta - 2.4g$
2 (i)	$\frac{0.2 \times 10^2}{2} = \frac{64e^2}{2 \times 0.8}$ $AP = 1.3$	M1 A1 A1	[3]	KE loss = EE gain $e = 0.5$
(ii)	$\frac{0.2 \times 10^2}{2} = \frac{64 \times 0.2^2}{2 \times 0.8} + \frac{0.2v^2}{2}$ $v = 9.17 \text{ ms}^{-1}$	M1 A1 A1	[3]	KE / EEbalance
3 (i)	$mv \frac{dv}{dx} = -mg - 0.02mv$ $\frac{v + 50g - 50g}{50g + v} \frac{dv}{dx} = -0.02$ $\left(\frac{500}{500 + v} - 1 \right) \frac{dv}{dx} = 0.02$ AG	M1 DM1 A1	[3]	Newton's 2 nd law, 2 resistive forces. $-mg - 0.02mv = -0.02(50g + v)$ used
(ii)	$\int \frac{500}{500 + v} - 1 dv = \int 0.02 dx$ $\left[500 \ln(500 + v) - v \right]_{14}^0 = 0.02H$ $H = 9.62 \text{ m}$	M1 DM1 A1	[3]	Attempts integration Appropriate use of $v = 14, 0$
4 (i)	$V \sin \theta = 50 \sin 30 - 4g$ $V^2 = (50 \cos 30)^2 + (-15)^2$ $V = 45.8 \text{ ms}^{-1}$ $15 = 50 \sin 30 - gt$ $t = 1$	B1 M1 A1 M1 A1	[5]	-15
(ii)	$OP^2 = (4 \times 50 \cos 30)^2 + \left(4 \times 50 \sin 30 - \frac{4^2 g}{2} \right)^2$ $OP = 174 \text{ m}$	M1 A1	[2]	

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5 (i)	$T = \frac{12(d - 0.6)}{0.6} = \frac{21(d - 0.7)}{0.7}$ $d = 0.9$ $T = \frac{12(0.2 - 0.6)}{0.6} = \frac{21(0.2 - 0.7)}{0.7}$ $W = 12$	M1 A1 M1 A1	[4]	Uses $T = \frac{\lambda \text{ ext}}{l}$ either string Must be total length, not extension Equation with both sides correct Finds either Tension (= 6)
(ii)	$\text{PE} = 0.2 \times 12 \quad (= 2.4)$ $\frac{12 \times 0.1^2}{2 \times 0.6} + 12 \times 0.2 = \frac{\frac{12}{g} v^2}{2} + \frac{12 \times 0.3^2}{2 \times 0.6} + \frac{21 \times 0.2^2}{2 \times 0.7}$ $v = 1.29 \text{ ms}^{-1}$	B1 M1 A1 A1	[4]	ft their value of d and their value of W PE / KE / EE balance
6 (i)	$\frac{0.2 \times 1.5^2}{0.5} = \text{Fr}$ $\mu \left(= \frac{\text{Fr}}{0.2g} \right) = 0.45$	M1 A1	[2]	Newton's 2 nd law, acc = $\frac{v^2}{r}$ Fr = 0.9 N
(ii)	$R = 0.2g - \frac{0.2g}{2} \sin 30$ $\text{Fr} = 0.45 \times 1.5$ $\frac{0.2g}{2} \cos 30 \pm 0.675 = 0.2\omega^2 0.5$ $\omega = 3.93 \text{ (greatest)}$ $\omega = 1.38 \text{ (least)}$	M1 A1 M1 A1 A1	[5]	1.5 0.675 Either
(iii)	$\frac{0.2g}{2} \cos 30 = 0.2\omega^2 0.5$ $\omega = 2.94$	M1 A1	[2]	

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7 (i)	$OG \text{ (sector)} = \frac{2 \times 0.35 \sin \frac{2\pi}{3}}{3 \times \frac{2\pi}{3}}$ $\text{Area (sector)} = \frac{0.35^2 \times \frac{4\pi}{3}}{2}$ $OG \text{ (triangle)} = \frac{2 \times 0.35 \cos \frac{\pi}{3}}{3} \quad \text{and}$ $\text{Area (triangle)} = \frac{0.35^2 \sin \frac{2\pi}{3}}{2}$ $0.096482... \times 0.256563... -$ $0.116666... \times 0.053044...$ $= d(0.256563... + 0.053044...)$ $d = 0.06(00) \text{m} \quad \text{AG}$	B1 B1 B1 M1 A1 A1	0.096482... 0.256563... 0.116666... 0.053044...
(ii) a	$F \times 0.35 \cos \frac{\pi}{3} = 0.06 \times 14$ $F = 4.8$	M1 A1	[2]
(ii) b	$F \sin \frac{\pi}{3} \times \left(0.35 + 0.35 \sin \frac{\pi}{3} \right)$ $+ F \cos \frac{\pi}{3} \times 0.35 \cos \frac{\pi}{3} = 14 \times 0.06$ $F = 1.29 \text{ N}$ <p>OR</p> $F \times 0.35 + Fr \times 0.35 = 14 \times 0.06$ $0.35F + 0.35F \sin \frac{\pi}{3} = 14 \times 0.06$ $F = 1.29 \text{ N}$	M1 A1 A1 (M1) (A1) (A1)	<p>Moments about point of contact</p> <p>Moments about O</p> <p>As $Fr = F \sin \frac{\pi}{3}$</p>