

Page 4	Mark Scheme	Syllabus	Paper
	GCE A LEVEL – October/November 2013	9709	73

1	$\text{Est}(\mu) = 1.8775 \text{ or } 1.88 \text{ (3 sf)}$ $\text{Est}(\sigma^2) = \frac{80}{79} \left(\frac{820.24}{80} - "1.8775"{}^2 \right)$ $= 6.81316 \text{ or } 6.81 \text{ (3 sf)}$ $z = 1.96$ $"1.8775" \pm z \times \sqrt{\frac{"6.81316"}{80}}$ $= 1.31 \text{ to } 2.45 \text{ (3 sf)}$	B1 M1 A1 B1 M1 A1	 	Accept 751/400 (not 150.2/80) Correct sub't'n in correct formula 1/79 (820.24 – 150.2 ² /80) Seen Must be an interval. NB use of biased var can still score A1.
	Total		[6]	
2	(i) Assume sd unchanged or sd = 10.4 H ₀ : Pop mean speed (or μ) = 62.3 H ₁ : Pop mean speed (or μ) < 62.3 $\frac{59.9 - 62.3}{\frac{10.4}{\sqrt{75}}}$ = – 1.999 or – 2.00 (allow + or –) Compare – 2.054 or – 2.055 No evidence that mean speed decreased (ii) Pop distribution unknown Yes	B1 B1 M1 A1 M1 A1 ft	 	Oe e.g. var unchanged Both. Not just “Mean . . ” Accept sd/var mixes, but must have $\sqrt{75}$ Correct z value (or correct critical value) Valid comparison of z's/areas/critical values No contradictions. Do not ft 2-tail test.
	Total		[8]	
3	(i) $\int_0^{10} \frac{1}{2500} (100t^3 - t^5) dt$ $(= \frac{1}{2500} \left[25t^4 - \frac{t^6}{6} \right]_0^{10} = \frac{100}{3})$ “ $\frac{100}{3}$ ” – $(\frac{16}{3})^2$ = $\frac{44}{9}$ or 4.89 (3 sf)	M1 M1 A1	 	Attempt integ $t^2 f(t)$ For $E(T^2) - (E(T))^2$
	(ii) $\int_n^{10} \frac{1}{2500} (100t - t^3) dt$ $\frac{1}{2500} \left[50t^2 - \frac{t^4}{4} \right] = 0.1$ $\frac{1}{2500} \left[2500 - \left(50n^2 - \frac{n^4}{4} \right) \right] = 0.1$ $(n^4 - 200n^2 + 9000 = 0)$ $(n^2 = 68.3772, n = 8.27)$ $n = 8$	M1 M1 M1 M1 A1	 	Attempt integ $f(t)$, ignore limits Attempt integ $f(t)$, limits n to 10 or 0 to n Equated to 0.1 or 0.9. Not need to be matched 0.1/0.9 matched to correct limits and used Correct method of solution of a QE in n^2 Must be single ans only
Total			[8]	

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4	(i)			
	(a)	$e^{-2.1} \times \frac{2.1^3}{3!}$ alone $= 0.189$	M1 A1	2 Allow any λ . Allow sum of 3 or 4 rel products, e.g. $P(3, 0)$
	(b)	$e^{-1.2} \times \frac{1.2^3}{3!} \times e^{-0.9}$ $+ e^{-1.2} \times \frac{1.2^2}{2!} \times e^{-0.9} \times 0.9$ $= 0.115$	M1 M1 A1	
	(ii)	$N(30, 30)$ $\frac{34.5-30}{\sqrt{30}} (= 0.8216)$ $1 - \Phi(“0.822”) = 0.206 (3sf)$	B1 M1 M1 A1	3 As final answer seen or implied standardising with their $N(\lambda, \lambda)$ 4 Allow with no or incorrect cc or no $\sqrt{}$ Area consistent with their working
	Total			
5	(i)	$E(X) = 3.5$ $(1^2 + 2^2 + 3^2 + 4^2 + 5^2 + 6^2) \div 6 - “3.5”^2$ $(= \frac{35}{12} \text{ AG})$	B1 B1	2 21/6 oe, must see correct expression and no incorrect working
	(ii)	Attempt $P(X < 3)$ or $1 - P(X \geq 3)$ $N(3.5, \frac{35}{12}/50)$ $\frac{3 - “3.5”}{\sqrt{\frac{35}{12}/50}} (= -2.070)$ $\Phi(“-2.070”) = 1 - \Phi(“2.070”) = 0.0192$ as final answer	M1 M1 M1 M1 A1	
	(iii)	Die is biased (towards lower numbers) Mean of 50 throws ≥ 3 (Allow > 3) or Equal nos of high and low scores or More high scores	B1 indep B1 indep	5 or $\frac{2.99 - “3.5”}{\sqrt{\frac{35}{12}/50}} (= -2.111)$ $\Phi(“-2.111”) = 1 - \Phi(“2.111”) = 0.0174$ or 0.0173 Consistent area As final answer or valid total method Allow with incorrect cc (e.g. 2.5) OR no $\sqrt{}$. Must have $\div 50$ Comment implying die is biased 2 Comment implying results of exp’t do not indicate bias (or indicate bias towards higher numbers) Both must be in context
	Total			[9]

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6	(i)	$N(5100, 5 \times 45^2)$ or $N(5100, 10125)$ $\frac{5200 - 5100}{\sqrt{10125}} (= 0.994)$ $\Phi(0.994)$ $= 0.840$ (3 sf)	B1 M1 M1 A1	4	seen or implied standardising with their new mean and new var area consistent with their working with normal
	(ii)	Use of $E - 3L$ or similar $E(E - 3L) = -260$ $\text{Var}(E - 3L) = 52^2 + 9 \times 45^2$ or 20929 $\frac{0 - (-260)}{\sqrt{20929}} (= 1.797)$ $1 - \Phi(1.797)$ $= 0.0361$ (3 sf) or 0.0362	M1 B1 B1 M1 M1 A1	6	2800 – 3 x 1020 with a pos var with 45^2 and 52^2 combined consistent area, must clearly be ϕ P ($3L - E < 0$): similar scheme SR: use of $3E - L$, M1, 7380 B1, 26361 B1 stand 0 with these values M1, M0A0 max 4/6
Total				[10]	