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	GCE A LEVEL – October/November 2013	9709	72

1 $\lambda = \frac{1}{30}$ $1 - e^{-\frac{1}{30}}$ $= 0.0328$ (3 s.f.)	B1 M1 M1 A1 [4]	o.e. $1 - P(X=0)$ by Poisson, any λ allow 1 end error $1 - P(X=0)$ by Poisson, correct λ no end errors S.R. Binomial with final answer 0.0328 B2 Correct answer, no working scores B2
2 $z = 2.576$ $2 \times z \times \frac{0.17}{\sqrt{n}} = 0.2$ oe $n = \left(\frac{2 \times 0.17 \times 2.576}{0.2}\right)^2$ oe (= 19.2) Smallest n is 20	B1 M1 M1 A1 [4]	Seen (accept 2.574 to 2.579) Allow without '2 ×' OR with incorrect z Attempt to arrange equ of correct form (with correct z and '2×' into the form $n=$ or $\sqrt{n}=$
3 (i) est (μ) = 2866 or 2870 (3 s.f.) est (σ^2) = $\frac{1}{49} (410900000 - \frac{143300^2}{50})$ (= 4126.53) = 4130 (3 sf)	B1 M1 A1 [3]	Accept 143300/50 o.e. Correct subst in correct formula
(ii) H_0 : Pop mean (or μ) = 2850 H_1 : Pop mean (or μ) \neq 2850 $\frac{\frac{143300}{50} - 2850}{\sqrt{4126.53}}$ $\sqrt{50}$ $= 1.761$ '1.761' < 1.96 No evidence mean distance changed	B1 M1 A1 M1 A1f [5]	Both. Not just 'mean' Allow '4126.53' without $\sqrt{\quad}$, but must have all $\sqrt{50}$ Or correct c.v. (2867.81) for alt method For valid comparison of z values, areas or c.v. Dep 1.96; ft their 1.761 If H_1 : $\mu > 2850$ and c.f. 1.645, max B0M1A1M1A0 (c.v. for 1 tail test 2864.94)
4 (i) $\lambda = 2.8$ $e^{-2.8} (1 + 2.8 + \frac{2.8^2}{2})$ $= 0.469$ (3 s.f.) or 0.47(0)	B1 M1 A1 [3]	seen any λ allow one end error As final answer
(ii) $e^{-0.7n} \geq 0.99$ or $e^{-\lambda} \geq 0.99$ $-0.7n \geq \ln 0.99$ or $-\lambda \geq \ln 0.99$ $n \leq 0.01436$ or $\lambda \leq 0.01005$ '0.01436' \times 150 or '0.01005' \times 150 \div 0.7 Max period is 2.15 mins (3 sf)	M1 M1 A1 M1 A1 [5]	Allow '=' throughout Attempt ln both sides Can be implied. Accept 3 s.f. Note $e^{-(0.7/150)n} \geq 0.99$ scores 1 st and 3 rd M1 T & I leading to ans 2.2 mins, SC: B2

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<p>5 (i) $\int_0^2 k(x-2)^2 dx = 1$ $\left(\left[\frac{k(x-2)^3}{3} \right]_0^2 = 1 \right)$ $k \left[0 - \left(-\frac{8}{3} \right) \right] = 1$ $k = \frac{3}{8}$ AG</p>	<p>M1 A1 [2]</p>	<p>Attempt to integrate $f(x)$ with correct limits and = 1 Must see this line or better, e.g. $k \times \frac{8}{3} = 1$</p>
<p>(ii) $\frac{3}{8} \int_d^2 (x-2)^2 dx = 0.2$ $\left(\frac{3}{8} \left[\frac{(x-2)^3}{3} \right]_d^2 = 0.2 \right)$ $\frac{3}{8} \left[0 - \frac{(d-2)^3}{3} \right] = 0.2$ oe $((d-2)^3 = -1.6)$ $d = 0.83(0)$ (3 s.f.)</p>	<p>M1 M1 A1 [3]</p>	<p>$\int f(x)dx$ with limits d and 2 or 0 and d, and = 0.2 or =0.8 Condone missing 'k' Reasonable attempt to integrate from a correct expression, with limits substituted to give expression in d^3. Condone missing 'k'</p>
<p>(iii) $\frac{3}{8} \int_0^2 x(x-2)^2 dx$ $\left(= \frac{3}{8} \int_0^2 x^3 - 4x^2 + 4xdx \right)$ $= \frac{3}{8} \left[\frac{x^4}{4} - \frac{4x^3}{3} + 2x^2 \right]_0^2$ $= \frac{1}{2}$</p>	<p>M1 A1 A1 [3]</p>	<p>Attempt integ $xf(x)$; ignore limits, condone missing k $\left(\frac{3}{8} \left[x \times \frac{(x-2)^3}{3} - \int \frac{(x-2)^3}{3} dx \right]_0^2 \right)$ $= \frac{3}{8} \left[x \times \frac{(x-2)^3}{3} - \frac{(x-2)^4}{12} \right]_0^2$ Correct integration & limits, condone missing k</p>
<p>6 (i) $P(\text{Type I}) = 1 - P(\geq 4 \text{ assuming } p = 0.7)$ $1 - ({}^6C_4 \times 0.7^4 \times 0.3^2 + {}^6C_5 \times 0.7^5 \times 0.3 + 0.7^6)$ $(= 1 - 0.744)$ $= 0.256$ (3 s.f.)</p>	<p>M1 M1 A1 [3]</p>	<p>or $P(\leq 3 \text{ assuming } p = 0.7)$ May be implied ${}^6C_3 \times 0.7^3 \times 0.3^3 + {}^6C_2 \times 0.7^2 \times 0.3^4 + {}^6C_1 \times 0.7 \times 0.3^5 + 0.3^6$ Allow one end error $= 0.256$ (3 s.f.) SR if zero scored allow B1 for use of $B(6, 0.7)$ in any two or more terms</p>
<p>(ii) $P(\text{Type II}) = P(\geq 4 \text{ assuming } p = 0.35)$ $= {}^6C_4 \times 0.35^4 \times 0.65^2 + {}^6C_5 \times 0.35^5 \times 0.65 + 0.35^6$ $= 0.117$</p>	<p>M1 M1 A1 [3]</p>	<p>May be implied Allow one end error SR if zero scored allow B1 for use of $B(6, 0.35)$ in any two or more terms</p>
<p>(iii) Type 1 They will reject Luigi's belief, although it might be true.</p>	<p>B1 B1 [2]</p>	<p>In context</p>

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7 (i) $N(10.61, 0.1017)$ $\frac{11 - 10.61}{\sqrt{0.1017}} (= 1.223)$ $\Phi(1.223)$ $= 0.889$ (3 s.f.)	B1 M1 M1 A1 [4]	o.e. Stated or implied (accept in un-simplified form) Allow without $\sqrt{}$ For attempt to find correct area consistent with their working
(ii) $P(K - 1.2A > 0)$ $\text{Var} = 0.0576 + 1.2^2 \times 0.0441$ $(= 0.121104)$ $N(-0.324, 0.121104)$ $\frac{0 - (-0.324)}{\sqrt{0.121104}} (= 0.931)$ $1 - \Phi(0.931)$ $= 0.176$ (3 s.f.)	M1 B1 B1 M1 M1 A1 [6]	Or similar stated or implied o.e. May be implied (accept in un-simplified form) Allow without $\sqrt{}$ For attempt to find correct area consistent with their working