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- 1 EITHER:** State or imply non-modular inequality  $(x+1)^2 > (x-4)^2$ , or corresponding equation or pair of linear equations M1
- Obtain critical value  $\frac{3}{2}$  A1
- State correct answer  $x > \frac{3}{2}$  A1
- OR:** State a correct linear equation for the critical value, e.g.  $x+1 = -x+4$ , or corresponding correct linear inequality, e.g.  $x+1 > -(x-4)$  M1
- Obtain critical value  $\frac{3}{2}$  A1
- State correct answer  $x > \frac{3}{2}$  A1 [3]
- 2** Use law for the logarithm of a product, a quotient or a power M1\*
- Obtain  $x \log 5 = (2x+1)\log 2$ , or equivalent A1
- Solve for  $x$ , via correct manipulative technique(s) M1(dep\*)
- Obtain answer  $x = 3.11$ . Allow  $x \in [3.10, 3.11]$  A1 [4]
- 3** Integrate and obtain  $\frac{1}{2}e^{2x}$  term B1
- Obtain  $2e^x$  term B1
- Obtain  $x$  B1
- Use limits correctly, allow use of limits  $x = 1$  and  $x = 0$  into an incorrect form M1
- Obtain given answer A1 [5]
- S. R. Feeding limits into original integrand, 0/5
- 4 (i)** State  $\frac{dx}{dt} = \frac{1}{t-2}$  or  $\frac{dy}{dt} = 1 - 9t^{-2}$  B1
- Use  $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$  M1
- Obtain given answer correctly A1 [3]
- (ii)** Equate derivative to zero and solve for  $t$  M1
- State or imply that  $t = 3$  is admissible c.w.o., and note  $t = -3, 2$  cases A1
- Obtain coordinates (1, 6) and no others A1 [3]
- 5** Use correct trig identity to obtain a quadratic in  $\cot \theta$  or  $\tan \theta$  M1
- Solve the quadratic correctly A1
- Obtain  $\tan \theta = \frac{1}{2}$  or  $-\frac{2}{3}$  A1✓
- Obtain answer  $26.6^\circ$  or  $146.3^\circ$  A1
- Carry out correct method for second answer from either root M1
- Obtain remaining 3 answers from  $26.6^\circ, 146.3^\circ, 206.6^\circ, 326.3^\circ$  and no others in the range A1 [6]
- [Ignore answers outside the given range]

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- 6 (i) Consider sign of  $\frac{6}{x^2} - x - 1$  at  $x = 1.4$  and  $x = 1.6$ , or equivalent M1  
Complete the argument correctly with appropriate calculations A1 [2]
- (ii) State  $\frac{6}{x^2} = x + 1$  B1  
Rearrange equation to given equation or *vice versa* B1 [2]
- (iii) Use the iterative formula correctly at least once M1  
Obtain final answer 1.54 A1  
Show sufficient iterations to justify its accuracy to 2 d.p. or show there is a sign change in the interval (1.535, 1.545) B1 [3]
- 7 (i) Substitute  $x = 1$ , equate to zero and obtain a correct equation in any form B1  
Substitute  $x = 2$  and equate to 10 M1  
Obtain a correct equation in any form A1  
Solve a relevant pair of equations for  $a$  or for  $b$  M1  
Obtain  $a = -17$  and  $b = 12$  A1 [5]
- (ii) At any stage, state that  $x = 1$  is a solution B1  
**EITHER:** Attempt division by  $x - 1$  and reach a partial quotient of  $3x^2 + 5x$  M1  
Obtain quotient  $3x^2 + 5x - 12$  A1  
Obtain solutions  $x = -3$  and  $x = \frac{4}{3}$  A1  
**OR:** Obtain solution  $x = -3$  by trial and error or inspection B1  
Obtain solution  $x = \frac{4}{3}$  B2
- [If an attempt at the quadratic factor is made by inspection, the M1 is earned if it reaches an unknown factor of  $3x^2 + 5x + \lambda$  and an equation in  $\lambda$ ] [4]
- 8 (i) Use product rule M1  
Obtain correct derivative in any form A1  
Substitute  $x = \frac{1}{2}\pi$ , and obtain gradient of  $-1$  for normal A1✓  
from  $y' = \sin x - x \cos x$  ONLY  
Show that line through  $\left(\frac{1}{2}\pi, \frac{1}{2}\pi\right)$  with gradient  $-1$  passes through  $(\pi, 0)$  M1  
A1 [5]
- (ii) Differentiate  $\sin x$  and use product rule to differentiate  $x \cos x$  M1  
Obtain  $x \sin x$ , or equivalent A1 [2]
- (iii) State that integral is  $\sin x - x \cos x (+ c)$  B1  
Substitute limits 0 and  $\frac{\pi}{2}$  correctly M1  
Obtain answer 1 A1 [3]  
S. R. Feeding limits into original integrand, 0/3