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- 1 (i) Either Square both sides to obtain linear equation M1
Obtain $x = \frac{165}{30}$ or $\frac{33}{6}$ or $\frac{11}{2}$ A1 [2]
Or Solve linear equation in which, initially, signs of x are different M1
Obtain $x + 2 = -x + 13$ or equivalent and hence $\frac{11}{2}$ or equivalent A1 [2]
- (ii) Apply logarithms and use power law M1
Obtain $y \log 3 = \log \frac{11}{2}$ and hence $y = 1.55$ A1 [2]
- 2 Use $\sin 2\theta = 2 \sin \theta \cos \theta$ B1
Simplify to obtain form $c_1 \sin^2 \theta = c_2$ or equivalent M1
Find at least one value of θ from equation of form $\sin \theta = k$ M1
Obtain 35.3° and 144.7° A1 [4]
- 3 (a) Integrate to obtain form $k \sin(\frac{1}{3}x + 2)$ where $k \neq 4$ M1
Obtain $12 \sin(\frac{1}{3}x + 2) (+ c)$ A1 [2]
- (b) State or imply correct y -values $2, \sqrt{20}, \sqrt{68}, \sqrt{148}$ B1
Use correct formula, or equivalent, with $h = 4$ and four y -values M1
Obtain 79.2 A1 [3]
- 4 Obtain $\frac{dx}{dt} = \frac{2}{t+1}$ B1
Obtain $\frac{dy}{dt} = 4e^t$ B1
Use $\frac{dy}{dx} = \frac{dy}{dt} / \frac{dx}{dt}$ with $t = 0$ to find gradient M1
Obtain 2 A1
Form equation of tangent through $(0, 4)$ with numerical gradient obtained from attempt to differentiate M1
Obtain $2x - y + 4 = 0$ or equivalent of required form A1 [6]
- 5 State or imply $\ln y = \ln K + px \ln 2$ B1
Obtain at least one of
 $1.87 = \ln K + 1.35p \ln 2, \quad 3.81 = \ln K + 3.35p \ln 2, \quad p \ln 2 = \frac{3.81 - 1.87}{3.35 - 1.35}$
or equivalents B1
Solve equation(s) to find one constant, dependent on previous B1 M1
Obtain $p = 1.40$ A1
Substitute to attempt value of K DM1
Obtain $\ln K = 0.5605$ and hence $K = 1.75$ A1 [6]

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- 6 (i) Substitute -2 and equate to zero, or divide and equate remainder to zero
Obtain $a = 12$ M1
A1 [2]
- (ii) Carry out division, or equivalent, at least as far as x^2 and x terms in quotient M1
Obtain $x^2 - 2x + 6$ A1
Calculate discriminant of a 3 term quadratic quotient (or equivalent) DM1
Obtain -20 (or equivalent) A1
Conclude by referring to, or implying, root -2 and no root from quadratic factor A1 [5]
- 7 (i) Integrate to obtain $ke^{3x} + mx^3$ M1
Apply both limits to obtain $\frac{1}{6}e^{3a} + \frac{1}{3}a^3 - \frac{1}{6} = 10$ or equivalent A1
Rearrange to form involving natural logarithm DM1
Obtain $a = \frac{1}{3}\ln(61 - 2a^3)$ with no errors seen (AG) A1 [4]
- (ii) Consider sign of $a - \frac{1}{3}\ln(61 - 2a^3)$ for 1.0 and 1.5 or equivalent M1
Obtain -0.36 and 0.17 or equivalent and justify conclusion A1 [2]
- (iii) Use iteration process correctly at least once M1
Obtain final answer 1.343 A1
Show sufficient iterations to 5 decimal places to justify answer or show a sign change in the interval (1.3425, 1.3435) A1 [3]
- 8 (i) Differentiate using product rule M1
Obtain $\sec^2 x \cos 2x - 2 \tan x \sin 2x$ A1
Use $\cos 2x = 2\cos^2 x - 1$ or $\sin 2x = 2\sin x \cos x$ or both B1
Express derivative in terms of $\sec x$ and $\cos x$ only M1
Obtain $4\cos^2 x - \sec^2 x - 2$ with no errors seen (AG) A1 [5]
- (ii) State $4\cos^4 x - 2\cos^2 x - 1 = 0$ B1
Apply quadratic formula to a 3 term quadratic equation in terms of $\cos^2 x$ to find the least positive value of $\cos^2 x$ M1
Obtain or imply $\cos^2 x = \frac{1 + \sqrt{5}}{4}$ or 0.809... A1
Obtain 0.45 A1 [4]