Р		age 4	ge 4 Mark Scheme				Paper 72	
			GCE AS/A LEVEL – M	lay/June	2013	9709	72	
L								
1	(i)	Binomial		B1				
		n = 400,  p = 0.012		B1 [2]	Both. Not <i>p</i> = Or B(400, 0.01	. Not <i>p</i> = 1.2% (400, 0.012): B1B1		
	(ii)	Poisson		B1				
		<i>n</i> large and	1 mean = 4.8, which is $< 5$	B1 [2]	n large, p small			
	(iii)	$1 - e^{-4.8}(1 - e^{-4.8})$	$+4.8+\frac{4.8^2}{2})$	M1	P( $X = 0, 1, 2$ ); allow any $\lambda$ ; allow one end error			
		=	= 0.857/0.858	A1 [2]	(Normal/Binomial in (ii) can score M1 only)			
			[[	Fotal: 6]				
2	(i)	$\frac{2}{3}\int_{1}^{2}x^{2}\mathrm{d}x$		M1	Attempt integ.	xf(x); ignore lim	its	
		$=\frac{2}{3}\left[\frac{x^3}{3}\right]_{1}^{2}$	2	A1	Correct integra	tion and limits		
		$=\frac{14}{9}$ or 1	.56 o.e.	A1 [3]	]			
	(ii)	$\frac{2}{3} \int_{1}^{\frac{14}{9}} x  dx$ $(=\frac{2}{2} \left[ \frac{x^3}{2} \right]$	2 )	M1	Attempt integ. $f(x)$ ; with limits			
		$=\frac{115}{243}$ or	0.473 (3 s.f.)	A1 [2]				
	(iii)	$\frac{115}{243} < \frac{1}{2}$	0.e.	M1	Comparison of	prob. or values		
		H	Hence mean < median	A1ft[2]	ft (i) or (ii)			
			[					

_		9709 s13 ms 72							
	Р	age 5	Mark Scheme			Syllabus	Paper		
Ī			GCE AS/A LEVEL – N	/lay/June	2013	9709	72		
L									
3	(i)	$\frac{73.1-75.2}{\frac{5.7}{\sqrt{2}}} = -1.563$		M1	For standardising (with $\sqrt{n}$ )				
		$n = \{-1.563 \times 5.7 \div (-2.1)\}^2$		A1	Any correct expression for <i>n</i> or $\sqrt{n}$ . May be implied by ans.				
		r I	a = 18 Assume s.d. for the region is 5.7	A1 B1 [4]					
	(ii)	$H_0$ : pop m $H_0$ : pop m 1.563 com Evidence t	ean (or $\mu$ ) = 75.2 ean (or $\mu$ ) < 75.2 p 1.555 hat plants shorter	B1 M1 A1 [3]	Both (could be stated in (i)) For comparison of z values / areas / x values CWO. No contradictions				
		[To							
4	(i)	$est(\mu) = 97$	750/150 = (65)	B1					
		$\operatorname{est}(\sigma^2) = \frac{1}{1}$	$\frac{1}{49}(\ 647500 - \frac{9750^2}{150})$	M1	Correct subst.	in correct formula	a		
		=	= 92.3 (3 s.f.)	A1 [3]					
	(ii)	<i>z</i> = 2.326	[ <u></u>	B1					
		$65' \pm z \times -$	$\frac{\sqrt{92.28188'}}{\sqrt{150}}$	M1	Any z				
		=	= 63.2 to 66.8 (3 s.f.)	A1 [3]	(Use of 'biased	l' can still score l	nere)		
	(iii)	$0.02^{2}$		M1	Allow M1 for	0.02 seen			
		=	= 0.0004 o.e.	A1 [2]					
			[						

	9709 s13 ms							
P	age 6	Mark Sche		Syllabus	Paper			
		GCE AS/A LEVEL – May/June			9709	72		
	<b>6 5</b> 10 · <b>5</b>	20 (2120)	DI					
5 (1)	$6 \times 510 + 10^{2}$	$4^2 = (3130)$	BI					
	N(3130, 88)	$4^{+} = (880)$ 30)	ы					
	$\frac{3050 - 3130}{\sqrt{880}}$	(=-2.697)						
	$\frac{3150-3130}{\sqrt{880}}$	(= 0.674)	M1	Both. With their mean and variance( $\geq 0$ ) All without $$				
	$ \begin{aligned} \Phi(`0.674') - (1 - \Phi(`2.697')) \\ (= 0.7499 - 0.0035) \\ = 0.746 \ (3 \ \text{sf}) \end{aligned} $ $ \begin{aligned} \mathbf{i})  510 - 8 \times 70 = (-50) \\ 12^2 + 8^2 \times 4^2 = (1168) \\ P - 8C \sim N(-50, 1168) \end{aligned} $		M1	Use of tables as with their work	nd attempt to fin	d area consistent		
			A1 [5]					
(ii)			B1 B1	o.e. $+50; 510/8$ o.e. $(12/8)^2 + 4$	8 -70; - (510/8 -	- 70)		
	$\frac{0-(-50)}{\sqrt{1168}}$	(= 1.463)	M1	For standardisi their mean and	ng with attempt variance(≥0).Al	"P-8C" oe with low without $$		
	$1 - \Phi(`1.40)$	53')	M1	Use of tables an with their work	nd attempt to fin	d area consistent		
	=	0.0717 (3 s.f.)	A1 [5]					
	[Total: 10]							

Γ	P	Page 7 Mark Scheme				<u> </u>	9 sl3 ms 72 Paner		
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L									
6	(i)	H <sub>0</sub> : Pop mean (or $\lambda$ or $\mu$ ) is 5.3 H <sub>1</sub> : Pop mean (or $\lambda$ or $\mu$ ) is less than 5.3		B1	Both				
		$P(X \le 2) = e^{-5.3}(1 + 5.3 + \frac{5.3^2}{2})/P(X=2)$		M1	Both attempted	mpted			
		$P(X \le 1) = 0.0314 \text{ or } 0.0315$ & $P(X \le 2) = 0.102/P(X=2)=0.7071$		A1	Both correct				
		CR is 0 or	1 cases	A1	Dep. M1 and P	$P(X \le 1) < 0.05 < P(X \le 2)$			
		No eviden	ce mean has decreased	B1f[5]	ft their CR				
	(ii)	Concludin	g mean has decreased when it	B1 In context					
		'0.0314 or	'0.0314 or 0.0315' B1ft[2] ft			ft their $P(X \le 1)$ , dep. < 0.05			
	(iii)	(Po(18.4)) N(18.4, 18	) .4)	B1 B1ft	Stated or implied B1 for N(18.4,); B1f for var. = 18.4		or var. = 18.4		
		$\frac{20.5 - 18.4}{\sqrt{18.4}} \qquad (= 0.490)$		M1	For standardisin without $$	ng with or with	out cc.Allow		
		1 – Φ('0.490')		M1	Use of tables ar with their work	nd attempt to fin ing	id area consistent		
		= 0.312 (3  s.f.) A1 [5]							
			[Te						