

Page 4	Mark Scheme	Syllabus	Paper
	GCE AS LEVEL – May/June 2013	9709	22

- 1 Integrate and obtain term of the form  $k \ln(7 - 2x)$  M1  
 State  $y = -2 \ln(7 - 2x) (+c)$  A1  
 Evaluate  $c$  DM1  
 Obtain answer  $y = -2 \ln(7 - 2x) + 2$  A1✓ [4]
- 2 Either State or imply non-modular inequality  $(x - 8)^2 > (2x - 4)^2$ , or M1  
 corresponding equation or pair of linear equations M1  
 Make reasonable solution attempt at a quadratic, or solve two linear equations A1  
 Obtain critical values 4 and  $-4$  A1  
 State correct answer  $-4 < x < 4$  [4]
- Or Obtain one critical value, e.g.  $x = 4$ , by solving a linear equation (or inequality) or B1  
 from a graphical method or by inspection B2  
 Obtain the other critical value similarly B1  
 State correct answer  $-4 < x < 4$  [4]
- 3 (i) Substitute  $x = -1$  and equate to zero M1  
 Obtain answer  $a = 7$  A1 [2]
- (ii) Substitute  $x = -3$  and evaluate expression M1  
 Obtain answer 18 A1 [2]
- 4 (i) State or imply  $(y + 1) \log 5 = 3x \log 2$  M1  
 State that this is of the form  $ay = bx + c$  and thus a straight line, or equivalent A1 [2]
- (ii) State gradient is  $\frac{3 \ln 2}{\ln 5}$ , or equivalent, e.g.  $3 \log_5 2$  B1  
 State  $(0, -1)$  B1 [2]
- 5 (i) State  $3 \frac{dy}{dx}$  as derivative of  $3y$ , or equivalent B1  
 State  $4xy + 2x^2 \frac{dy}{dx}$  as a derivative of  $2x^2y$ , or equivalent B1  
 Equate derivative of LHS to zero and solve for  $\frac{dy}{dx}$  M1  
 Obtain given answer correctly A1 [4]
- (ii) Substitute  $x = 2$  into given equation and solve for  $y$  M1  
 Obtain gradient  $= \frac{12}{5}$  correctly A1  
 Form equation of the normal at their point, using negative recip of their  $\frac{dy}{dx}$  M1  
 State correct equation of normal  $5x + 12y + 2 = 0$  or equivalent A1 [4]
- 6 (i) Make a recognisable sketch of a relevant graph, e.g.  $y = 3e^x$  or  $y = 8 - 2x$  B1  
 Sketch a second relevant graph and justify the given statement B1 [2]

Page 5	Mark Scheme	Syllabus	Paper
	GCE AS LEVEL – May/June 2013	9709	22

- (ii) Consider sign of  $3e^x - 8 + 2x$  at  $x = 0.7$  and  $x = 0.8$ , or equivalent M1  
 Complete the argument correctly with appropriate calculations A1 [2]  
 ( $f(0.7) = -0.559$ ,  $f(0.8) = 0.277$  or equivalent)

- (iii) Show that given equation is equivalent to  $x = \ln\left(\frac{8-2x}{3}\right)$ , or vice versa B1 [1]

- (iv) Use the iterative formula correctly at least once M1  
 Obtain final answer 0.768 A1  
 Show sufficient iterations to justify its accuracy to 3 d.p.

$x_0 = 0.7$	$x_0 = 0.75$	$x_0 = 0.8$
0.78846	0.77319	0.75769
0.76129	0.76603	0.77082
0.76971	0.76825	0.76676
0.76711	0.76756	0.76802
0.76791		0.76763
0.76766		

or show there is a sign change in the interval (0.7675, 0.7685) B1 [3]

- 7 (a) Obtain one term of form  $ke^{2x-1}$  with any non-zero  $k$  M1  
 Obtain correct integral  $x + \frac{1}{2}e^{2x-1}$  A1  
 Substitute limits, giving exact values M1  
 Correct answer  $\frac{1}{2}e^3 + 1$  A1 [4]

- (b) Use product or quotient rule M1\*  
 Obtain correct derivative in any form A1  
 Equate derivative to zero and solve for  $x$  M1\*  
 Obtain  $\tan 2x = 1$  dep  
 Obtain  $x = \frac{\pi}{8}$  A1 [5]

- 8 (i) Use correct  $\sin(A - B)$  and  $\cos(A - B)$  formula M1  
 Substitute exact values for  $\cos 30^\circ$  etc. M1  
 Obtain given answer correctly A1 [3]

- (ii) State  $2\operatorname{cosec} x = 3\cot^2 x - 2$  B1  
 Use  $\cot^2 x = \operatorname{cosec}^2 x - 1$  M1  
 Attempt solution of quadratic equation in  $\operatorname{cosec} x$  or  $\sin x$  M1  
 ( $3\operatorname{cosec}^2 x - 2\operatorname{cosec} x - 5 = 0$  or  $5\sin^2 x = 2\sin x - 3 = 0$ )  
 Obtain  $\sin x = \frac{3}{5}$  or  $-1$  A1✓  
 Obtain one correct answer for  $\sin^{-1}\left(\frac{3}{5}\right)$  A1  
 Obtain remaining 2 answers from  $36.9^\circ$ ,  $143.1^\circ$ ,  $270^\circ$  and no others in the range  
 [Ignore answers outside the given range] A1 [6]  
 SC If only answer given is  $270^\circ$  B1