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1	$0.6v dv/dx = 0.3x$	M1	Newton's Second Law with $a = v dv/dx$
	$0.6v^2/2 = 0.3x^2/2 (+ c)$	A1	From $\int 0.6v dv = \int 0.3x dx$
	$[x^2/2]_0^8 = [v^2]_2^v$	M1	Uses limits of finds constant
	$v = 6 \text{ ms}^{-1}$	A1 [4]	[4]
2 (i)	$12 \times 3 \times 0.2/8 - 8 \times 0.2/2 = (8 + 12)d$	M1	Table of values or moment equation
	$d (= 0.1/20) = 0.005 \text{ m}$ AG	A1	$0.9 - 0.8 = 20d$
		A1 [3]	Accept $d = -0.005$
(ii)	$F \times (2 \times 0.2) = (12 + 8) \times 0.005$	M1	Moments about point of contact
	$F = 0.25$	A1	
	OR	A1	
	$F \times (2 \times 0.2) + 8 \times 0.1 = 12 \times 0.075$	M1	Moments about point of contact
	$F = 0.25$	A1	
		A1 [3]	[6]
3 (i)	Length = $\sqrt{1.2^2 + 0.5^2} = 1.3$	B1	Pythagoras on $\frac{1}{2}$ string
	$2 \times [14.3 \times (1.3 - 1.1)/1.1] \times [0.5/1.3]$ $= mg$	M1* D* M1	Uses $T = \lambda x/L$ Component(s) T equated to weight
	$m = 0.2$	A1 [4]	
(ii)	$0.2v^2/2 = 0.2g \times 0.5 -$ $[14.3 \times 0.2^2/(2 \times 1.1) -$ $14.3 \times 0.1^2/(2 \times 1.1)] \times 2$	M1	KE/EE/PE balance (4 terms)
	$v = 2.47 \text{ ms}^{-1}$	A1 ✓ A1	✓ candidate's value of m from (i)
		A1 [3]	[7]

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4 (i) $0.25dv/dt = -3t$ $v = -12t^2/2 (+c)$ $0 = 12 \times 3^2/2 + c$ Initial speed = 54 ms^{-1}	M1	Newton's Second Law, – sign essential
	A1	Accept uncanceled form
	M1	Appropriate use of $v = 0, t = 3$
	A1 [4]	Goes beyond $c = 54$
(ii) $\int dx = \int (54 - 6t^2) dt$ $x = [54t - 6t^3/3]_0^3$ $x = 108 \text{ m}$	M1	Separates variables, integrates v
	A1 ^{ft}	^{ft} candidates value [v in (i)]
	A1 [3]	[7]
5 (i) $0 = (25\sin 70)t - gt^2/2$ $t = 4.7(0) \text{ s}$ $OP = (25\cos 70 \times 4.7) = 40.2 \text{ m}$ OR $OP = 25^2 \sin(2 \times 70)/g$ $OP = 40.2 \text{ m}$ $t[= 40.2/(25\cos 70)] = 4.7 \text{ s}$ OR $0 = 25\sin 70 - 10t$ $t = 2.349, 2t = 4.70$ $OP = (25\cos 70 \times 4.7) = 40.2 \text{ m}$ OR $0 = x \tan 70 - gx^2/(2 \times 25^2 \cos^2 70)$ $x = 40.2 \text{ m}$ $t = 4.70$	M1	Uses $0 = ut - gt^2/2$
	A1	
	A1	
	M1	Uses $R = v^2 \sin 2\alpha/g$
	A1	
	A1	
	M1	Find time to greatest height and double it
	A1	
	A1	
	M1	Use trajectory equation
	A1	
	A1 [3]	
(ii) $t[= 17.1/(25\cos 70)] = 2 \text{ s}$ $-v = v - g \times 2$ $V^2 = 10^2 + (25\cos 70)^2$ $V = 13.2 \text{ ms}^{-1}$	B1	Finds time of flight
	B1ft	Finds vertical component of speed
	M1	For squaring components
	A1 [4]	[7]

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6 (i) $\frac{2(1)\sin(\pi/2)}{3\pi/2} \times \pi(1^2)/2 = \frac{2r\sin(\pi/2)}{3\pi/2} \times \pi(r^2)/2 + OG(\pi/2 - \pi r^2/2)$ $OG = 4\pi(1 - r^3)/3(1 - r^2)$ $OG = 4(1 + r + r^2)/3\pi(1 + r)$ AG	M1	Uses table of values or moment equation	
	A1	Correct moment equation	
	A1		
	A1 [4]	Must use $1 - r$ as a factor of $1 - r^3$ and $1 - r^2$	
(ii) $r = 4(1 + r + r^2)/3\pi(1 + r)$ $(3\pi - 4)r^2 + (3\pi - 4)r - 4 = 0$ $r = 0.494$ AG OR $OG = 0.494$ if G on arc $OG = 4(1 + 0.494 + 0.494^2)/3\pi(1 + 0.494)$ $= 0.4937$ AG	M1*	Sets $r = \text{answer(i)}$	
	D* M1	Sets up and starts solving quadratic equation	
	A1 [3]		
	M1*		
	D* M1	Substitutes AG in OG expression	
(iii) $\tan \theta = 0.494/1$ $\theta = 26.3^\circ$	A1	Shows value rounding to 0.494	
7 (i) $T = 0.5 \text{ g}$ $T = 0.8 \times 6.25^2 \times r$ $r = 0.16 \text{ m}$ $v = 1 \text{ ms}^{-1}$	M1		
	B1	$T = 5$	
	M1		
	A1		
(ii) $T \cos 60 = 0.5 \text{ g}$ $r = 0.32 \text{ m}$ $T \sin 60 = 0.5 \times 6.25^2 \times R$ $R = 0.443(40) \text{ m}$ $L = 0.32 + 0.443(4)/\sin 60$ $L = 0.832 \text{ m}$	B1	$T = 10$	
	B1	$\frac{1}{2} (2 \times \text{candidate's value of } r)$	
	M1	Newton's Second Law with component of T	
	A1		
	M1		
	A1 [6]		[10]