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1	(i) [WD = $65 \times 76 \cos 5^\circ$] Work done is 4920 J	M1 A1	For using $WD = Td \cos \alpha$ [2]
	(ii) [P = $65 \cos 5^\circ \times 1.5$] Rate of working is 97.1 W	M1 A1ft	For using $P = Tv \cos \alpha$ ft for the value of ans(i) $\times 1.5 \div 76$ SR for candidates who assume without justification that the speed is constant (max 1/2) $t = 76 \div 1.5 = 50.6 \dots$ $\text{rate} = WD/t = 4960 \div 50.6 \dots = 97.1 \text{ W}$ B1
2	PE loss = $\frac{1}{2} 8(8^2 - 3^2) + 120 (= 340 \text{ J})$ [340 = 8gh] Height is 4.25 m	M1 A1 DM1 A1	For using 'loss of PE = gain in KE + WD against resistance' For using PE = mgh [4]
			SR for candidates who assume without justification that the resistance to motion is constant, usually implicitly by using constant acceleration formulae (max 3/4) For using Newton's second law with 3 terms, $v^2 - u^2 = 2as$ and $h = s \sin \alpha$ M1 For attempting to eliminate α , a and s from the equations $(80s \sin \alpha - 120/s = 8a$ $64 - 9 = 2as, h = s \sin \alpha)$ M1 $80s \sin \alpha - 120 = 4(64 - 9)$ $\rightarrow 80h - 120 = 220$ $\rightarrow h = 4.25$ A1
3	(i) [$\frac{1}{2} 5 \times 50 + \frac{1}{2} 7(8 + 50) + 90 \times 8$] Distance is 1048 m	M1 A1	For using the area property for distance or $s = \frac{1}{2} (u + v)t$ [2] AG
	(ii) $a = (8 - 50)/(12 - 5)$ or $d = (50 - 8)/(12 - 5)$ $850 - F = 85a$ (or $-85d$) Upward force is 1360 N	M1 A1 A1	For use of the gradient property for acceleration (deceleration) For using Newton's second law (3 terms) [5]

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4	(i)	M1	For resolving forces in the i and j directions	
		A1		
		A1		
		M1	For using $F^2 = X^2 + Y^2$ or $\tan \theta = Y/X$	
		A1		
		B1	[6]	
				SR for candidates who <u>consistently</u> have cos for sin and vice versa (max 4/6) M1 as above (resolving) A1 for $F \sin \theta = 12 \sin 30^\circ$ <u>and</u> $F \cos \theta = 10 - 12 \cos 30^\circ$ M1 as above $F^2 = \dots$ & $\tan \theta = \dots$ A1 for $F = 6.01$ <u>and</u> $\theta = 93.7$
	(ii) Magnitude is 12N	B1		
	Direction is 30° clockwise from +ve 'x' axis	B1	[2]	
	alternative for 4(i)			
	For triangle of forces with sides 12, F and 10 and at least one of the angles $(90^\circ - \theta)$ or 60° or $(\theta + 30^\circ)$	B1		
		M1	For use of cosine rule (with θ absent) or use of sine rule (with F absent) and use of $\sin(A \pm B) = \sin A \cos B \pm \sin B \cos A$	
	$F^2 = 12^2 + 10^2 - 2 \times 12 \times 10 \cos 60^\circ$ or $(12 \cos 30^\circ) \sin \theta = (10 - 12 \sin 30^\circ) \cos \theta$	A1		
	$F = 11.1$ or $\theta = 21.1$ (accept 21.0)	A1		
		M1	For correct method for θ or F	
	$\theta = 21.1$ (accept 21.0) or $F = 11.1$	A1	[6]	
	second alternative for 4(i)			
	For using Lami's theorem with 12 N and 10 N	M1		
	$12/\sin(90 + \theta) = 10/\sin(150 - \theta)$	A1		
	$12/\cos \theta = 20 \div (\cos \theta + 3^{1/2} \sin \theta)$ $\rightarrow 12 \times 3^{1/2} \sin \theta = 8 \cos \theta$ $\rightarrow \tan \theta = 2 \div (3 \times 3^{1/2})$ $\rightarrow \theta = 21.1$	A1		
	For using Lami's theorem with F N and (12 N or 10 N)	M1		
	$F/\sin 120^\circ = 12/\sin 111.1^\circ$ (or $10/\sin 128.9^\circ$)	A1		
	$F = 11.1$	A1	[6]	

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Alternative for 4(ii)			
For $X = 11.1\cos 21.1^\circ$ and $Y = 11.1\sin 21.1^\circ - 10$, $R^2 = X^2 + Y^2$ and $\tan \Phi = Y/X$	M1		
Magnitude 12 N and direction 30° clockwise from +ve x-axis	A1	[2]	
5 (i)	M1		For using $0 = u - gt$ to find times at maximum heights.
Times to max. height are 1.2s and 0.7s	A1		
Range of values is $0.7 < t < 1.2$	A1	[3]	
(ii)	M1		For using $h = ut - \frac{1}{2}gt^2$ and attempting to solve $3h_A = 8h_B$ for t
$36t - 1.5gt^2 = 56t - 4gt^2$	A1		
$t = 8/g$	A1		
	M1		For using $v = u - gt$
Velocities are 4m^{-1} and -1ms^{-1}	A1	[5]	
Alternative for part 5(ii)			
For using $3h_P = 8h_Q \rightarrow 3(v_P^2 - 144) \div (-20) = 8(v_Q^2 - 49) \div (-20) \rightarrow 3v_P^2 - 8v_Q^2 = 40$	B1		
For using $v_P = 12 - 10t$ and $v_Q = 7 - 10t$ $\rightarrow v_P - v_Q = 5$	B1		
For eliminating v_Q (or v_P) and solving for v_P (or v_Q).	M1		
$v_P^2 - 16v_P + 48 = 0 \rightarrow v_P = 4$ (or 4, 12)	A1		
Upward velocities are 4ms^{-1} and -1ms^{-1}	A1	[5]	
6 (i)	M1		For resolving forces on R vertically
$2T \cos \alpha = 0.6g$	A1		Where $\alpha = \frac{1}{2}$ angle ARB
Tension is 5N	A1	[3]	
(ii) $[F = T \sin \alpha]$	M1		For resolving forces on B horizontally
Frictional component is 4N	A1		
$[N = 0.4g + T \cos \alpha]$	M1		For resolving forces on B vertically
Normal component is 7 N	A1	[4]	
(iii)	M1		For using $\mu = F/N$
Coefficient is $4/7$ or 0.571	A1ft	[2]	ft conditional on both M1 marks scored in (ii); ft F and/or N

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Alternative for Q6(i)/(ii)			
7	(i) For finding the relevant angles and using Lami's theorem	M1	
	$6/\sin 106.26^\circ = T/\sin 126.87^\circ$	A1	
	Tension is 5N	A1	[3]
	(ii) $F/\sin 126.87^\circ = 5/\sin 90^\circ$	B1	
	Frictional component is 4N	B1	
	$(R - 4)/\sin 143.13^\circ = 5/\sin 90^\circ$	B1	
	Normal component is 7 N	B1	[4]
	(i) $[1.3 = 0.9 + 0.004T,$ $1.3^2 = 0.9^2 + 2 \times 0.004S]$	M1	For using $v = u + at$ or $v^2 = u^2 + 2as$
	Time is 100 s (or distance is 110 m)	A1	
	Distance is 110 m (or time is 100 s)	B1	[3]
	(ii) $\int kt^3 dt = \frac{1}{4} kt^4$	B1	
	$[k(\frac{1}{4} 100^4 - 0) = 110]$	M1	For using limits 0 to T and equating definite integral to S
	$k = 4.4 \times 10^{-6}$	A1	
	$[v_w = 0.9 + 0.004 \times 64.05,$ $v_c = 4.4 \times 10^{-6} \times 64.05^3]$	M1	For attempting to find the speed of the walker and of the cyclist.
	Both are equal to 1.16 ms^{-1} correct to 3 sf.	A1	[5]
	(iii) Acceleration = $3kt^2$	B1	
	Acceleration at B is 0.132 ms^{-2}	B1	[2]