

Page 4	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2010	9709	52

<b>1</b> c of m of arc = $20\sin(\pi/2)/(\pi/2)$  $(2 + 0.9)\bar{x} = 2 \times 20\sin(\pi/2)/(\pi/2)$ Distance is 8.78cm	B1 M1  A1 A1 [4]	For attempting to take moments about the diameter
<b>2 (i)</b>  $\tan 35^\circ = r/7.5$ $r = 5.25$	M1  A1ft A1 [3]	For using the idea that the c.m. is vertically above the lowest point of contact ft using their c of m from the base
<b>(ii)</b> [ $\mu mg \cos 35^\circ > mg \sin 35^\circ$ ]  $\mu > \tan 35^\circ \rightarrow$ Coefficient is greater than 0.7	M1  A1 [2]	For using 'no sliding $\rightarrow \mu R > \text{weight component}$ ' Do not allow $\mu \geq 0.7$ AG
<b>3 (i)</b> $mg = T \cos \theta$ $ma = T \sin \theta$ $\tan \theta = a/g = 0.75$ $T = 0.24 \times 10 / \cos \theta = 3$	B1 B1 B1 B1 [4]	SR B1 not B2 for $\tan \theta = v^2/gr$ or $a/g$ used  AG For using $T \cos \theta = mg$ to find T
<b>(ii)</b> [ $v^2 = 7.5 \times 2 \sin \theta$ ] Speed is $3 \text{ ms}^{-1}$	M1 A1 [2]	For using $v^2 = ar$ to find v
<b>4</b> Weight split is 9N:6N  For lamina $9 \times 0.75 + 6 \times 0.5$ $= T \times 1.5 \sin 30^\circ$ Tension is 13N  <b>Alternatively</b> $[(1.5^2 + \frac{1}{2} 1.5 \times 2) \bar{x} = 1.5^2 \times 0.75 + \frac{1}{2} 1.5 \times 2 \times 0.5]$ $\bar{x} = 0.65$  $15 \times 0.65 = T \times 1.5 \sin 30^\circ$ Tension is 13N	B1 M1 A1ft A1 A1 [5]  M1 A1 M1 A1ft A1 [5]	For taking moments about A      For using $A\bar{x} = A_1x_1 + A_2x_2$  For taking moments about A

Page 5	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2010	9709	52

<p><b>5 (i)</b> <math>7 = 16\tan\theta - 10 \times 16^2 / (2 \times 20^2) \cos^2\theta</math>  <math>[7 = 16T - 3.2(1 + T^2)]</math></p> <p><math>3.2T^2 - 16T + 10.2 = 0</math>  <math>T = \frac{3}{4}, 17/4</math></p>	<p>B1 M1 A1 A1 [4]</p>	<p>For using <math>\cos\theta = 1/\sec\theta</math> and the given identity to obtain a quadratic in <math>T(\tan\theta)</math> AEF AG</p>
<p><b>(ii)</b> <math>[x = \tan\theta \cos^2\theta / 0.0125 \text{ or } x = 20^2 \sin 2\theta / g]</math></p> <p>For <math>\tan\theta = 0.75</math>, distance is 38.4 m  For <math>\tan\theta = 4.25</math>, distance is 17.8 m</p>	<p>M1 A1 A1 [3]</p>	<p>For solving <math>y = 0</math> for <math>x</math> or for using <math>R = V^2 \sin 2\theta / g</math></p>
<p><b>(iii)</b> For sketching two parabolic arcs which intersect once, both starting at the origin, each with <math>y \geq 0</math> throughout, and each returning to the x-axis, the arc for which the angle of projection is smaller having the greater range.  The ranges appear significantly greater than <math>x</math> at the intersection, and slightly greater, respectively.</p>	<p>B1  B1 [2]</p>	
<p><b>6 (i)</b> <math>[0.35g = 2T\{0.7 / (2.4^2 + 0.7^2)^{1/2}\}]</math>  Tension is 6.25N  <math>[6.25 = \lambda \times \frac{1}{4}]</math>  Modulus is 25N</p>	<p>M1 A1 M1 A1 [4]</p>	<p>For resolving forces on P vertically  For using <math>T = \lambda x / L</math> AG</p>
<p><b>(ii)</b></p> <p>EE on release <math>= 25 \times 2^2 / (2 \times 4)</math>  EE when P is at M <math>= 25 \times 0.8^2 / (2 \times 4)</math></p> <p><math>25 \times 2^2 / (2 \times 4) = 0.35g \times 1.8 + 25 \times 0.8^2 / (2 \times 4) + \frac{1}{2} 0.35v^2</math>  Speed is <math>4.90 \text{ ms}^{-1}</math></p>	<p>M1 A1 A1 M1  A1 A1 [6]</p>	<p>For using <math>EE = \lambda x^2 / 2L</math>  For using <math>EE \text{ on release} = mgh + EE</math> when P is at M <math>+ \frac{1}{2} mv^2</math></p>
<p><b>7 (i)</b> <math>[0.25v(dv/dx) = -(5 - x)]</math></p> <p><math>[\int v dv = 4 \int (x - 5) dx]</math></p> <p><math>v^2/2 = 4(x - 5)^2/2 (+ A)</math></p> <p><math>v^2 = 4(x - 5)^2</math>  Selects correct square root to obtain <math>v = 10 - 2x</math></p>	<p>B1  M1  A1 M1 A1 A1 [6]</p>	<p>For using Newton's second law and <math>a = v(dv/dx)</math>  For separating variables and attempting to integrate  For using <math>v(0) = 10</math> Any correct expression in <math>x</math> AG</p>
<p><b>(ii)</b> <math>[\int \frac{dx}{10 - 2x} = \int dt]</math></p> <p><math>-\frac{1}{2} \ln(10 - 2x) = t(-\frac{1}{2} \ln B)</math>  <math>B = 10</math> (or equivalent)  <math>x = 5(1 - e^{-2t})</math>  <math>0 &lt; e^{-2t} &lt; 1</math> for all <math>t \rightarrow x &lt; 5</math> for all <math>t</math></p>	<p>M1  A1 A1 B1ft B1 [5]</p>	<p>For using <math>v = dx/dt</math> and separating variables    ft <math>x = (B/2)(1 - e^{-2t})</math> AG</p>