9709/62

I ÜBEISHED			9709_m21_ms_c
Question	Answer	Marks	Guidance
1(a)	$Est(\mu) = \frac{4820}{60} \text{ or } \frac{241}{3} \text{ or } 80.3 \text{ (3 sf)}$	B1	
	$\operatorname{Est}(\sigma^2) = \frac{60}{59} \left(\frac{392050}{60} - \left(\frac{4820}{60}\right)^2\right)$	M1	Use of biased (80.72) score M0 A0.
	82.0904 $\left(\frac{14530}{177}\right)$ to 82.635 or SD = 9.0604 to 9.0904 (3sf)	A1	
	z = 2.326	B1	
	$\frac{4820}{60} \pm z \times \sqrt{\frac{82.0904'}{60}}$	M1	Expression of the correct form $-$ must be z value.
	77.6 to 83.1 (3 sf)	A1	CWO Use of biased 77.6 to 83.0(3) can score B1M1A1 (max 4/6).
		6	
1(b)	Population distribution of times unknown	B1	Accept 'not normal'.
		1	

Question	Answer	Marks	Guidance
2(a)	$\frac{1}{2} \times \frac{1}{2} k \times k = 1$	M1	Or use of $\int_{0}^{k} \left(-\frac{1}{2}x + \frac{1}{2}k \right) dx = 1$ and attempt at integral.
	<i>k</i> = 2	A1	Unsupported answers M0 A0. Do not accept ±2.
		2	
2(b)	$\mathbf{f}(x) = -\frac{1}{2}x + 1$	B1 FT	FT their k from $y = -\frac{1}{2}x + \frac{1}{2}k$.
	$\int_{0}^{2} (-\frac{1}{2}x^{2} + x)dx = \left[-\frac{x^{3}}{6} + \frac{x^{2}}{2}\right]_{0}^{2}$	M1	Attempt integration of $xf(x)$ limits 0 to k . FT <i>their</i> $f(x)$. Could be in terms of k .
	$\frac{2}{3}$ or 0.667 (3 sf)	A1	
		3	

Question	Answer	Marks	Guidance
2(c)	$\int_{p}^{1} (-\frac{1}{2}x+1) dx \ [= 0.25]$	M1	FT their equation of line ; correct integral and limits (could be reversed) stated or $\frac{1}{2}(1-p)(1-\frac{1}{2}p+\frac{1}{2})$ [= 0.25].
	$\begin{bmatrix} -\frac{x^2}{4} + x \end{bmatrix}_p^1 = 0.25$ $-\frac{1}{4} + 1 + \frac{p^2}{4} - p = 0.25$	M1	Attempt substitution of correct limits (not reversed) into their integral or attempt expand must equal 0.25. OE
	$p^2 - 4p + 2 = 0$	M1	Obtain 3-term quadratic set equal to 0, obtain at least 1 solution.
	$p = 2 - \sqrt{2}$ or 0.586	A1	CAO
		4	

Question	Answer	Marks	Guidance
3(a)	One-tail because investigating whether "higher"	B1	OE. Must have both parts.
		1	
3(b)	H ₀ : Population mean (or μ) in city same as for others H ₁ : Population mean (or μ) in city greater than for others	B1 FT	If (a) two-tail: H ₀ : Pop mean (or μ) in city same as for others. H ₁ : Pop mean (or μ) in region different from others.
	2.41 > 2.326 or 0.008 < 0.01 or 0.992 > 0.99	M1	If (a) two-tail: 2.41 < 2.576 or 0.992 < 0.995.
	There is evidence that buildings are higher [on average].	A1 FT	In context, not definite. No contradictions. If (a) two-tail: There is no evidence that the [average] height of buildings is different.
		3	

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Question	Answer	Marks	Guidance
4(a)	B(1000, $\frac{1}{400}$)	B1	Accept Bin and $n = 1000, \ p = \frac{1}{400}$.
		1	
4(b)	Po(2.5)	B2	B1 for Po. B1 for $\lambda = 2.5$.
		2	
4(c)(i)	$e^{-2.5} \times \frac{2.5^4}{4!}$	M1	FT <i>their</i> (b) for Normal must have a continuity correction. Allow any λ
	0.134 (3 sf)	A1	CWO
		2	
4(c)(ii)	$e^{-2.5}\left(\frac{2.5^2}{2!} + \frac{2.5^3}{3!} + \frac{2.5^4}{4!}\right)$	M1	FT <i>their</i> (b) for Normal must have a continuity correction. Allow with one term extra or omitted or wrong. Allow any λ .
	0.604 (3 sf)	A1	CWO
		2	
4(d)	$\lambda = 2.5 \times 0.7 \text{ or } \lambda = 700 \times \frac{1}{400} \ [= 1.75]$	M1	Must see λ or use of Poisson.
	$1 - e^{-1.75}$	M1	Allow any λ . Allow $1 - P(0,1)$.
	0.826	A1	SC B1 Use of B(700,0.0025) leading to 0.826.
		3	

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Question	Answer	Marks	Guidance
5(a)	$E(L_1+L_2+L_3+S_1+S_2+S_3+S_4) = 3 \times 5.10 + 4 \times 2.51 [= 25.34]$	B1	OE $(E(3L + 4S - 25.5) = -0.16)$
	$Var(L_1+L_2+L_3+S_1+S_2+S_3+S_4) = 3 \times 0.0102 + 4 \times 0.0036 \ [= 0.045]$	B1	or $SD = \frac{3\sqrt{2}}{20} = 0.2121$.
	$\frac{25.5 - 25.34'}{\sqrt{0.045'}} \ [= 0.754]$	M1	No SD/variance mix. Standardising with <i>their</i> values (must be from a combination attempt).
	Φ('0.754')	M1	For the correct area consistent with <i>their</i> working.
	0.775 (3 sf)	A1	
		5	
5(b)	$E(L-2S) = 5.10 - 2 \times 2.51 [= 0.08]$	B1	OE
	$Var(L - 2S) = 0.0102 + 2^2 \times 0.0036 [= 0.0246]$	B1	Or $SD = 0.1568$.
	$\frac{0-0.08'}{\sqrt{0.0246'}} \ [=-0.510]$	M1	No SD/variance mix. Standardising with <i>their</i> values (must be from a combination attempt).
	$P(Z > '-0.510') = \phi(`0.510')$	M1	For the correct area consistent with <i>their</i> working.
	0.695 (3 sf)	A1	
		5	

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Question	Answer	Marks	Guidance
6(a)	H ₀ : population proportion = 0.08 OE H ₁ : population proportion > 0.08 OE	B1	Allow ' $p = 0.08$ ' etc.
	$P(X \ge 4) = 1 - P(X \le 3) = 1 - (0.92^{25} + 25 \times 0.92^{24} \times 0.08 + {}^{25}C_2 \times 0.92^{23} \times 0.08^2 + {}^{25}C_3 \times 0.92^{22} \times 0.08^3)$	M1	Allow 1 – (one term omitted or extra or wrong).
	0.135 (3 sf)	A1	
	0.135 > 0.05	M1	Valid comparison. Note: '0.865'<0.95 can score M1 A1 and can recover previous M1 A1 for 0.865.
	There is no evidence that proportion owning Chantor has increased	A1 FT	In context. Not definite, e.g. not 'Proportion not increased'. No contradictions.
		5	
6(b)	H ₀ was not rejected.	*B1 FT	H ₀ was rejected (consistent with (a)).
	Hence Type II might have been made.	DB1 FT	Type I error.
		2	
6(c)	$P(X \ge 5) = 1 - P(X \le 4)$ = 1 - ((1 - 0.1351) + ²⁵ C ₄ × 0.92 ²¹ × 0.08 ⁴) [= 0.0451]	*M1	Attempted. Note: If critical region method used in (a) marks can be awarded here.
	0.0451 < 0.05	A1	Comparison of 0.045[1] with 0.05. Note: If critical region method used in (a) marks can be awarded here.
	P(Type I error) = 0.0451 or 0.0452	A1	Dependent on M1* only. SC Unsupported answers score: B1 for 0.0451<0.05 and B1 for final answer 0.0451 only.
		3	