

Question	Answer	Marks	Guidance
1	${}^{38}C_r$ or ${}^nC_{34}$	M1	Either expression seen OE, no other terms, condone x1
	${}^{38}C_{34}$	A1	Correct unsimplified OE
	73815	A1	If M0, SCB1 ${}^{38}C_{34} \times k$, k an integer
		3	

Question	Answer	Marks	Guidance
2(a)	$\left(\frac{1}{3}\right)\left(\frac{2}{3}\right)^2 + \left(\frac{1}{3}\right)\left(\frac{2}{3}\right)^3 + \left(\frac{1}{3}\right)\left(\frac{2}{3}\right)^4$	M1	One correct term with $0 < p < 1$
	$= \frac{4}{27} + \frac{8}{81} + \frac{16}{243} \left(= \frac{2432}{7776} \right)$	A1	Correct expression, accept unsimplified
	$= \frac{76}{243}$ or 0.313	A1	
		3	

Question	Answer	Marks	Guidance										
2(b)	<table><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td></tr><tr><td>$P(x)$</td><td>$\frac{8}{27}$</td><td>$\frac{12}{27}$</td><td>$\frac{6}{27}$</td><td>$\frac{1}{27}$</td></tr></table>	x	0	1	2	3	$P(x)$	$\frac{8}{27}$	$\frac{12}{27}$	$\frac{6}{27}$	$\frac{1}{27}$	B1	Probability distribution table with correct values of x , no additional values unless with probability of 0 stated, at least one non-zero probability included
	x	0	1	2	3								
	$P(x)$	$\frac{8}{27}$	$\frac{12}{27}$	$\frac{6}{27}$	$\frac{1}{27}$								
	$P(0) = \left(\frac{2}{3}\right)^3$ $P(1) = \left(\frac{1}{3}\right)\left(\frac{2}{3}\right)^2 \times 3$ $P(2) = \left(\frac{2}{3}\right)\left(\frac{1}{3}\right)^2 \times 3$ $P(3) = \left(\frac{1}{3}\right)^3$	B1	1 correct probability seen (may not be in table) or 3 or 4 non-zero probabilities summing to 1										
		B1	All probabilities correct										
	3												
2(c)	$E(X) = \left[0 \times \frac{8}{27}\right] + 1 \times \frac{12}{27} + 2 \times \frac{6}{27} + 3 \times \frac{1}{27}$ $= \left[\frac{0}{27}\right] + \frac{12}{27} + \frac{12}{27} + \frac{3}{27}$	M1	Correct method from <i>their</i> probability distribution table with at least 3 terms, $0 \leq \text{their } P(x) \leq 1$, accept unsimplified										
	= 1	A1											
		2											

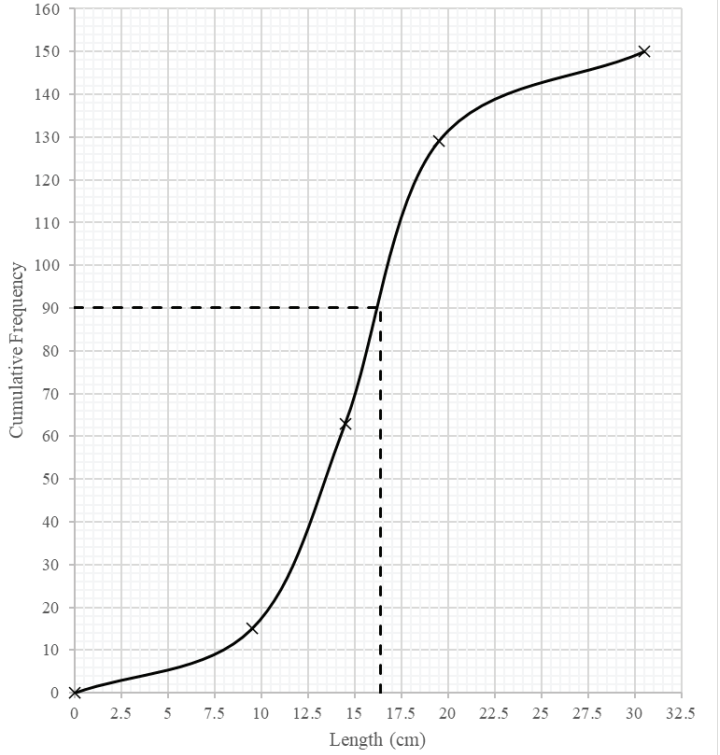
Question	Answer	Marks	Guidance
3(a)	$P(X > 87) = P\left(Z > \frac{87-82}{\sigma}\right) = 0.22$	M1	Using \pm standardisation formula, not σ^2 , not $\sqrt{\sigma}$, no continuity correction
	$P\left(Z < \frac{5}{\sigma}\right) = 0.78$ $\left(\frac{5}{\sigma} = \right) 0.772$	B1	AWRT ± 0.772 seen B0 for ± 0.228
	$\sigma = 6.48$	A1	
		3	
3(b)	$P\left(-\frac{4}{\sigma} < Z < \frac{4}{\sigma}\right) = P(-0.6176 < Z < 0.6176)$	M1	Using ± 4 used within a standardisation formula (SOI), allow σ^2 , $\sqrt{\sigma}$ and continuity correction
		M1	Standardisation formula applied to both <i>their</i> ± 4
	$\Phi = 0.7317$ Prob = $2\Phi - 1 = 2(0.7317) - 1$	M1	Correct area $2\Phi - 1$ oe linked to final solution
	$= 0.463$	A1	
		4	

Question	Answer	Marks	Guidance
4(a)	$R \wedge \wedge \wedge \wedge \wedge \wedge \wedge \wedge R$ $\frac{9!}{3!6!}$	M1	9! Alone on numerator, 3! × k or 6! × k on denominator
	= 84	A1	
		2	
4(b)	$\wedge (B B B) \wedge \wedge \wedge \wedge \wedge$	M1	$\frac{7!}{6!} \times k$ or $7k$ seen, k an integer > 0
	$\frac{7!}{6!} \times \frac{8 \times 7}{2}$	M1	$m \times n(n-1)$ or $m \times {}^nC_2$ or $m \times {}^nP_2$, $n=7, 8$ or 9 , m an integer > 0
		M1	$n = 8$ used in above expression
	= 196	A1	
	Alternative for question 4(b)		
	[Arrangements, blues together – Arrangements with blues together and reds together =] $\frac{9!}{2!6!} - \frac{8!}{6!}$	M1	9! Seen alone or as numerator with subtraction
	= [252 – 56]	M1	8! Seen alone or as numerator in a second term and no other terms
		M1	All terms divided by 6! × k, k an integer
	= 196	A1	
		4	

Question	Answer	Marks	Guidance
5(a)	$1 - P(6, 7, 8)$ $= 1 - ({}^8C_6 0.7^6 0.3^2 + {}^8C_7 0.7^7 0.3^1 + 0.7^8)$	M1	One term ${}^8C_x p^x (1-p)^{8-x}$, $0 < p < 1$, $x \neq 0$
	$= 1 - 0.55177$	A1	Correct unsimplified expression, or better
	$= 0.448$	A1	
	Alternative method for question 5(a)		
	$P(0, 1, 2, 3, 4, 5)$ $= 0.3^8 + {}^8C_1 0.7^1 0.3^7 + {}^8C_2 0.7^2 0.3^6 + {}^8C_3 0.7^3 0.3^5 + {}^8C_4 0.7^4 0.3^4 + {}^8C_5 0.7^5 0.3^3$	M1	One term ${}^8C_x p^x (1-p)^{8-x}$, $0 < p < 1$, $x \neq 0$
		A1	Correct unsimplified expression, or better
	$= 0.448$	A1	
		3	
5(b)	Mean = $120 \times 0.7 = 84$ Var = $120 \times 0.7 \times 0.3 = 25.2$	B1	Correct mean and variance, allow unsimplified
	$P(\text{more than } 75) = P\left(z > \frac{75.5 - 84}{\sqrt{25.2}}\right)$	M1	Substituting <i>their</i> μ and σ into the \pm standardising formula (any number), not σ^2 , not $\sqrt{\sigma}$
		M1	Using continuity correction 75.5 or 74.5
	$P(z > -1.693)$	M1	Appropriate area Φ , from final process, must be a probability
	$= 0.955$	A1	Allow $0.9545 < p \leq 0.955$
		5	

Question	Answer	Marks	Guidance
6(a)	<div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;">Box A</div> <div style="text-align: center;">Box B</div> </div>	B1	Both correct probs, box A
		B1	2 probs correct for box B
		B1	All correct probs for box B
		3	
6(b)	$\frac{7}{8} \times \frac{5}{15} + \frac{1}{8} \times \frac{9}{15}$	M1	Two 2 factor terms added, correct or FT <i>their 6(a)</i> .
	$= \frac{44}{120} \left[\frac{11}{30} \text{ or } 0.367 \right]$	A1	OE
		2	

Question	Answer	Marks	Guidance
6(c)	$P(A \text{ blue} B \text{ blue}) = \frac{P(A \text{ blue} \cap B \text{ blue})}{P(B \text{ blue})}$ $= \frac{\frac{1}{8} \times \frac{6}{15}}{\frac{7}{8} \times \frac{5}{15} + \frac{1}{8} \times \frac{6}{15}} = \frac{\frac{1}{20}}{\frac{41}{120}}$	M1	their $\frac{1}{8} \times \frac{6}{15}$ seen as numerator or denom of fraction
		M1	their $\frac{7}{8} \times \frac{5}{15} + \frac{1}{8} \times \frac{6}{15}$ seen
		M1	their $\frac{7}{8} \times \frac{5}{15} + \frac{1}{8} \times \frac{6}{15}$ seen as denominator
	$= \frac{6}{41}$ or 0.146	A1	
		4	

Question	Answer	Marks	Guidance
7(a)	15, 63, 129, 150 	B1	Correct cumulative frequencies seen (may be on graph)
		B1	$0 \leq \text{Horizontal axis} \leq 30$, $0 \leq \text{vertical axis} \leq 150$ Labels correct: length cm, cf
		M1	At least 3 points plotted at upper end points (e.g. allow 9, 9.5, 10) with a linear horizontal scale.
		A1	Linear vertical scale, all points at correct upper end points (9.5 etc.), curve drawn accurately, joined to (0,0) (condone $(-0.5, 0)$)
		4	
7(b)	60% of 150 = 90	M1	90 seen or implied by use on graph
	Approx. 16.5 [cm]	A1FT	FT <i>their</i> increasing cumulative frequency graph, Use of graph must be seen. If no clear evidence of use of graph SCB1FT correct value from <i>their</i> graph
		2	

Question	Answer	Marks	Guidance
7(c)	Midpoints: 4.75, 12, 17, 25	M1	At least 3 correct midpoints used (39449.4375 implies M1)
	$\text{Var} = \frac{4.75^2 \times 15 + 12^2 \times 48 + 17^2 \times 66 + 25^2 \times 21}{150} - 15.295^2$	M1	Using midpoints ± 0.5 in correct var formula, including subtraction of <i>their</i> μ^2 .
	= 29.1	A1	
		3	