

Question	Answer	Marks	Guidance
1	$0 = 15\sin 60 - gt$ ($t = 3\sqrt{3}/4 = 1.30$)	M1	Uses $v = u + at$ vertically
	$x = 15\cos 60 \times 1.3 (= 9.7428\dots)$	A1	
	$y = (15\sin 60)^2/(2g) (= 8.4375\dots)$	B1	Uses $v^2 = u^2 + 2as$ vertically
	$D = \sqrt{(9.74^2 + 8.44^2)}$	M1	Applies Pythagoras's theorem
	$D = 12.9 \text{ m}$	A1	
	Total:	5	

Question	Answer	Marks	Guidance
2(i)	$M = 2\pi \times 0.2 \times 0.9 + \pi \times 0.2^2$	B1	M = total mass of the container
	$(2\pi \times 0.2 \times 0.9 + \pi \times 0.2^2) \bar{x}$ $= 2\pi \times 0.2 \times 0.9 \times 0.9/2$	M1	Takes moments about the base
	$\bar{x} = 0.405 \text{ m}$ AG	A1	
	Total:	3	
2(ii)	$\tan \theta = 0.2/0.405$	M1	θ is the angle of slope of the plane
	$\mu = \tan \theta$	B1	
	$\mu = 0.494$	A1	
	Total:	3	

Question	Answer	Marks	Guidance
3(i)	$30 = (20\sin 60)t + \frac{1}{2}gt^2$	M1	Uses $s = ut + \frac{1}{2}at^2$ vertically
	$5t^2 + 10\sqrt{3}t - 30 = 0$	M1	Sets up a quadratic equation and attempts to solve it
	$t = 1.27$	A1	
	Total:	3	

Question	Answer	Marks	Guidance
3(ii)	$v^2 = (20\sin 60)^2 + 2g \times 30$ (hence $v = 30$)	B1	Uses $v^2 = u^2 + 2as$ vertically
	$V = \sqrt{30^2 + (20\cos 60)^2}$ or $\tan \theta = 30/(20\cos 60)$	M1	
	$V = 31.6 \text{ ms}^{-1}$	A1	
	$\theta = 71.6^\circ$ with the horizontal	A1	Or 18.4° with the downward vertical
	Total:	4	

Question	Answer	Marks	Guidance
4(i)	$A = 0.6 \times 0.75 + 0.3 \times 0.75/2$ (= 0.5625)	B1	A = total area of the lamina
	$0.5625 \bar{x} = 0.75 \times 0.6 \times 0.3 + \frac{1}{2} 0.3 \times 0.75 \times (0.6 + 0.3/3)$	M1	Takes moments about AB
	$\bar{x} = 0.38 \text{ m}$ (from AB) AG	A1	
	$0.5625 \bar{y} = 0.75 \times 0.6 \times 0.375 + \frac{1}{2} 0.3 \times 0.75 \times 0.25$	M1	Takes moments about BC
	$\bar{y} = 0.35 \text{ m}$ (from BC)	A1	
	Total:	5	
4(ii)	$\tan \theta = 0.35/0.38$	M1	$\tan \theta = \bar{y}/\bar{x}$ where θ is the required angle
	$\theta = 42.6^\circ$	A1	
	Total:	2	

Question	Answer	Marks	Guidance
5(i)	$T\cos 60 = 1.5 + 0.4g$	M1	Resolve vertically for P
	$T = 11 \text{ N}$	A1	
	$T\sin 60 = 0.4 \omega^2 \times 0.5 \sin 60$	M1	Uses Newton's Second Law horizontally for P
	$\omega = \sqrt{55} = 7.42$	A1	
	Total:	4	

Question	Answer	Marks	Guidance
5(ii)	$m = 0.15$ (from $mg = 1.5$)	B1	Resolves vertically for Q
	$T^* = 0.15 \times 7.42^2 \times 0.5 \sin 60$	M1	Uses Newton's Second Law horizontally for Q
	$T^* = 3.57 \text{ N}$	A1	
	Total:	3	

Question	Answer	Marks	Guidance
6(i)	Friction = $0.4 \times 0.4g$	B1	Uses $F = \mu R$
	$0.4v dv/dx = -0.4 \times 0.4g - 0.8/x$	M1	Uses Newton's Second Law and $a = v dv/dx$
	$v dv/dx = -4 - 2/x$	A1	
	Total:	3	
6(ii)	$\int v dv = \int \left(-4 - \frac{2}{x} \right) dx$	M1	Separates the variables and attempts to integrate
	$v^2/2 = -4x - 2 \ln x (+ c)$	A1	
	$v = U$ when $x = 1$ hence $c = U^2/2 + 4$	M1	Attempts to find c
	$0 = -4 \times 2 - 2 \ln 2 + U^2/2 + 4$ [$U^2 = 10.7(725)$] $0 = -4 \times 2.1 - 2 \ln 2.1 + U^2/2 + 4$ [$U^2 = 11.7(677)$]	M1	Put $v = 0$ and $x = 2$ Put $v = 0$ and $x = 2.1$
	$3.28 < U < 3.43$	A1	
	Total:	5	

Question	Answer	Marks	Guidance
7(i)	$0.4g = 24e/0.6$	M1	Uses $T = \lambda x/L$
	$e = 0.1 \text{ m}$	A1	
	Total:	2	
7(ii)	Initial EE = $24 \times 0.1^2/(2 \times 0.6)$ ($= 0.2 \text{ J}$)	B1	Uses $EE = \lambda x^2/2L$
	$0.4 \times 5^2/2 + 0.4gd = 24(0.1 + d)^2/(2 \times 0.6) - 24 \times 0.1^2/(2 \times 0.6)$	M1 A1	Set up a 4 term energy equation involving EE, PE and KE
	$d = 0.5 \text{ m}$	A1	
	Total:	4	

Question	Answer	Marks	Guidance
7(iii)	$e = 0.2$	B1	
	$0.8v^2/2 = 24 \times 0.6^2/(2 \times 0.6) - 24 \times 0.2^2/(2 \times 0.6) - 0.8g \times 0.4$	M1 A1	Set up a 4 term energy equation in EE, PE and KE
	$v = 2\sqrt{2} = 2.83 \text{ ms}^{-1}$	A1	
	Total:	4	