Solomon Practice Paper

Pure Mathematics 1J

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	7	
2	7	
3	8	
4	8	
5	9	
6	9	
7	11	
8	16	
Total:	75	

How I can achieve better:

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•

•





[3]

[4]

[3]

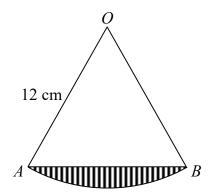
Total: 7

Total: 8

[3]

[5]

1. Figure shows a sector OAB of a circle, centre O and radius 12 cm.



Given that the perimeter of the sector OAB is 32 cm, find

- (a) the size of $\angle AOB$ in radians as an exact fraction,
- (b) the area of the shaded segment in cm², giving your answer correct to 3 significant figures.
- Total: 7 2. (a) Find $\int (3x-1)^2 dx$. [4]

Given that $\frac{dy}{dx} = (3x - 1)^2$ and that when x = -1, y = 2,

- (b) find y in terms of x.
- (a) Prove from first principles that the sum of the first n natural numbers, [4]

$$1+2+3+4+\ldots+n$$
,

is given by

$$\frac{1}{2}n(n+1).$$

- (b) Hence evaluate the sum of the integers between -30 and 72 inclusive.
- [4]
- 4. A is the point (8,0) and B is the point (12,6).
 - (a) Find an equation of the line passing through the points A and B.

M and N are the midpoints of OA and OB respectively, where O is the origin.

- (b) Calculate the area of the trapezium ABNM.
- Total: 8
- (a) Given that $y = 2^x$, show that [5]

i.
$$4^x = y^2$$



ii.
$$2^{x+2} = 4y$$

(b) By using your answers to part (a), or otherwise, solve the equation

[4]

$$4^x - 2^{x+2} - 32 = 0.$$

Total: 9

6. (a) Show that the solutions of the equation

[4]

$$5\tan(\theta) - 6\cos(\theta) = 0,$$

will be given by the values of θ for which

$$6\sin^2(\theta) + 5\sin(\theta) - 6 = 0,$$

(b) Hence solve the equation

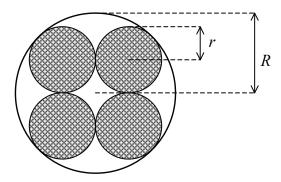
[5]

$$5\tan(\theta) - 6\cos(\theta) = 0$$

for θ in the interval $0 \le \theta \le 2\pi$, giving your answers correct to 2 decimal places.

Total: 9

7. Figure shows a design consisting of four identical circles of radius r,



which are shaded, arranged such that their centres are at the four corners of a square of side 2r. A larger circle of radius R circumscribes the four smaller circles.

(a) Show that
$$R = (1 + \sqrt{2})r$$
.

[5]

[6]

(b) Hence show that the ratio of the total area of the four shaded circles to the area of the larger circle is equal to $(12 - 8\sqrt{2})$: 1.

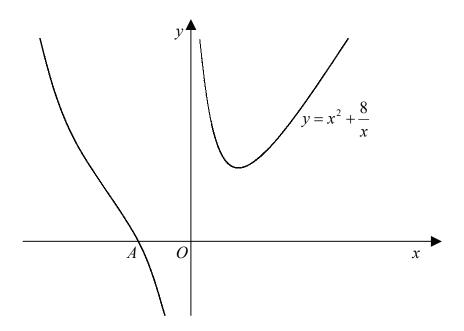
Total: 11

8. Figure shows part of the curve

$$y = x^2 + \frac{8}{x}$$

Last updated: May 5, 2023





which crosses the x-axis at the point A.

(a) Find the coordinates of the point A.

[3]

The line l is the normal to the curve at the point A.

(b) Find an equation of the line l.

[6]

(c) Show that the line l will intersect the curve where

[3]

$$6x^3 - x^2 - 2x + 48 = 0.$$

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(d) Hence prove that l does not cross the curve other than at A.

[4]

Total: 16