Pearson Edexcel

A Level Mathematics 9MA0

Unit Test

8 Differentiation

Time allowed: 50 minutes

School:

Name:

Teacher:

Question	Points	Score
1	6	
2	8	
3	6	
4	5	
5	5	
6	8	
7	6	
8	2	
9	4	
Total:	50	



1. (a) Given that $f(x) = \sin(x)$, show that

$$f'(x) = \lim_{h \to 0} \left(\left(\frac{\cos(h) - 1}{h} \right) \sin(x) + \frac{\sin(h)}{h} \cos(x) \right)$$

- (b) Hence prove that $f'(x) = \cos(x)$.
- A toy soldier is connected to a parachute. The soldier is thrown into the air from ground level. The height, in metres, of the soldier above the ground can be modelled by the equation

$$H = \frac{4t^{\frac{2}{3}}}{t^2 + 1} \qquad 0 \le t \le 6s$$

where H is height of the soldier above the ground and t is the time since the soldier was thrown.

(a) Show that

$$\frac{\mathrm{d}H}{\mathrm{d}t} = \frac{8(1-2t^2)}{3\sqrt[3]{t}(t^2+1)^2}$$

- (b) Using the differentiated function, explain whether the soldier was increasing or decreasing [2] in height after 2 seconds.
- (c) Find the exact time when the soldier reaches a maximum height. [2]

Total: 8

[6]

[2]

[3]

3. A curve has the equation

$$=\ln(3x) - e^{-2x}$$

Show that the equation of the tangent at the point with an x-coordinate of 1 is

y

$$y = \left(\frac{e^2 + 2}{e^2}\right)x - \left(\frac{e^2 + 3}{e^2}\right) + \ln(3)$$

4. Given that $x = \sec(4y)$, find

(a)
$$\frac{\mathrm{d}y}{\mathrm{d}x}$$
 in terms of y .

(b) Show that

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{k}{x\sqrt{x^2 - 1}}$$

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[4]

[2]

[4]

Total: 6

where k is a constant which should be found.

5. A curve C has equation $4^x = 2xy$ for x > 0.

Find the exact value of $\frac{dy}{dx}$ at the point C with coordinates (2, 4).

6. A curve has parametric equations

$$x = \cos(2t)$$
, and $y = \sin(t)$, $-\pi \le t \le \pi$.

- (a) Find an expression for $\frac{dy}{dx}$ in terms of t. [3] Leave your answer as a single trigonometric ratio.
- (b) Find an equation of the normal to the curve at the point A where $t = -\frac{5\pi}{6}$. [5]
- 7. The curve C has equation $y = x^3 + 6x^2 12x + 6$.
 - (a) Show that C is concave on the interval [-5, -3]. [3]
 - (b) Find the coordinates of the point of inflection.

Total: 6

[3]

[2]

Total: 8

- 8. In a rainforest, the area covered by trees, F, has been measured every year since 1990.It was found that the rate of loss of trees is proportional to the remaining area covered by trees.Write down a differential equation relating F to t, where t is the numbers of years since 1990.
- 9. The volume of a sphere $V \text{ cm}^3$ is related to its radius r cm by the formula $V = \frac{4}{3}\pi r^3$. [4] The surface area of the sphere is also related to the radius by the formula $S = 4\pi r^2$. Given that the rate of decrease in surface area, in cm²s⁻¹, is $\frac{dS}{dt} = -12$, find the rate of decrease of volume $\frac{dV}{dt}$.



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Total: 5

[5]