

GRAPHS OF POLYNOMIALS

[ESTIMATED TIME: 50 minutes]

GCSE

(+ IGCSE) EXAM QUESTION PRACTICE

1.

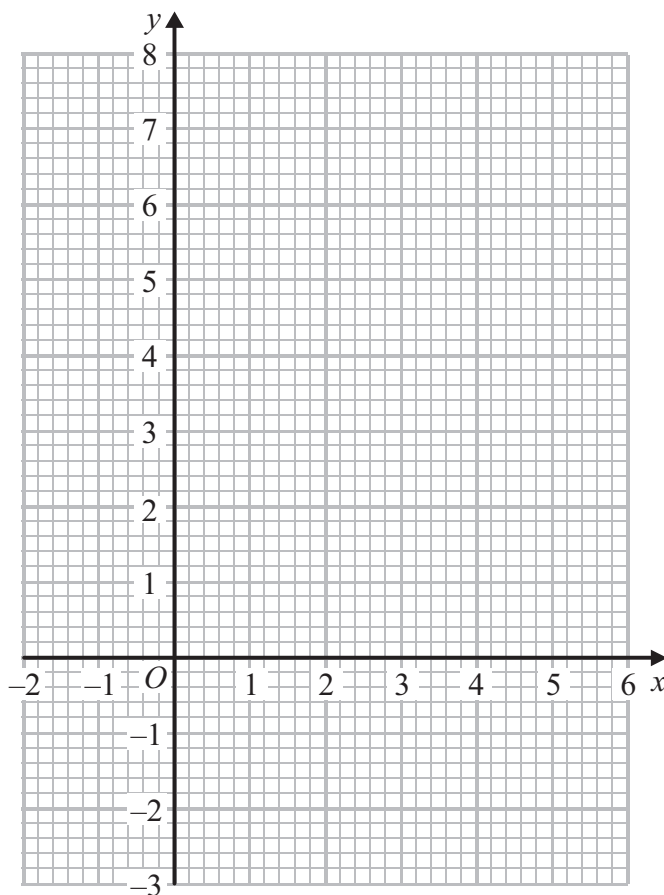
[4 marks]

(a) Complete the table of values for $y = x^2 - 4x + 2$

| | | | | | | | |
|-----|----|---|---|----|----|---|---|
| x | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| y | | 2 | | -2 | -1 | | |

(2)

(b) On the grid, draw the graph of $y = x^2 - 4x + 2$ for all values of x from -1 to 5



(2)

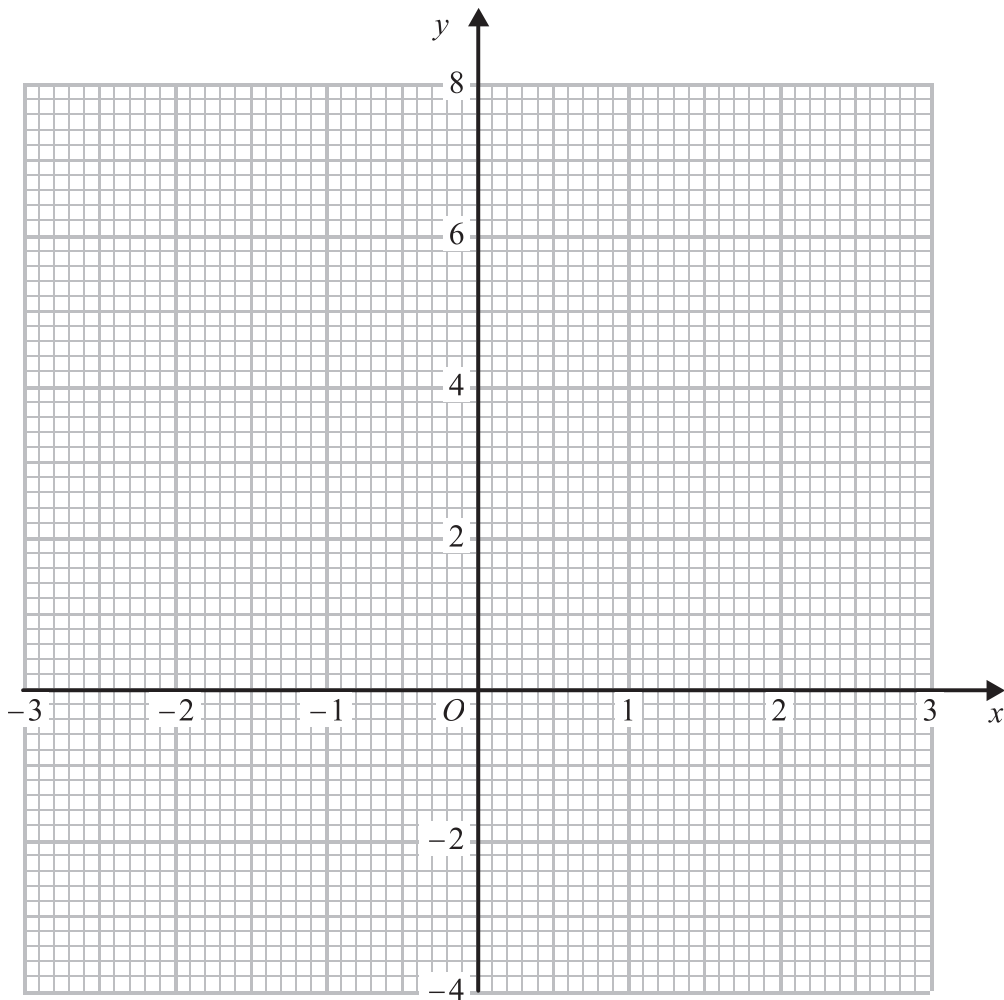


(a) Complete the table of values for $y = x^2 - 2$

| | | | | | | | |
|-----|----|----|----|---|---|---|---|
| x | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| y | | | -1 | | | | |

(2)

(b) On the grid, draw the graph of $y = x^2 - 2$



(2)



For $y = x^3 - 6x^2 + 20$

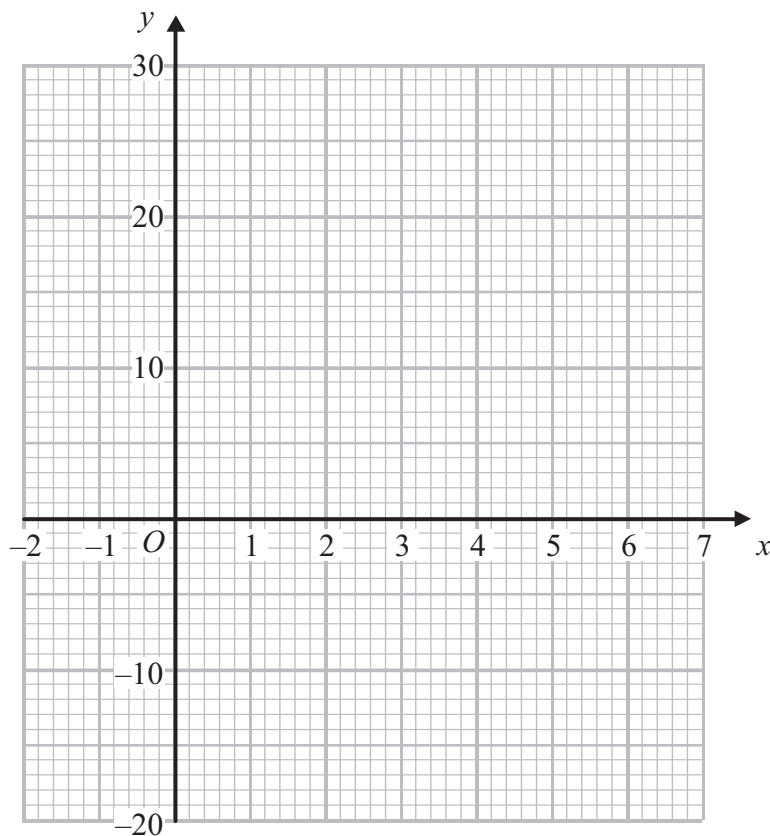
(a) (i) show that $y = 4$ when $x = 2$

(ii) complete the table of values

| | | | | | | | | |
|-----|----|----|----|---|----|-----|---|----|
| x | -1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| y | | 20 | 15 | | -7 | -12 | | 20 |

(2)

(b) On the grid, draw the graph of $y = x^3 - 6x^2 + 20$ for values of x from -1 to 6



(2)

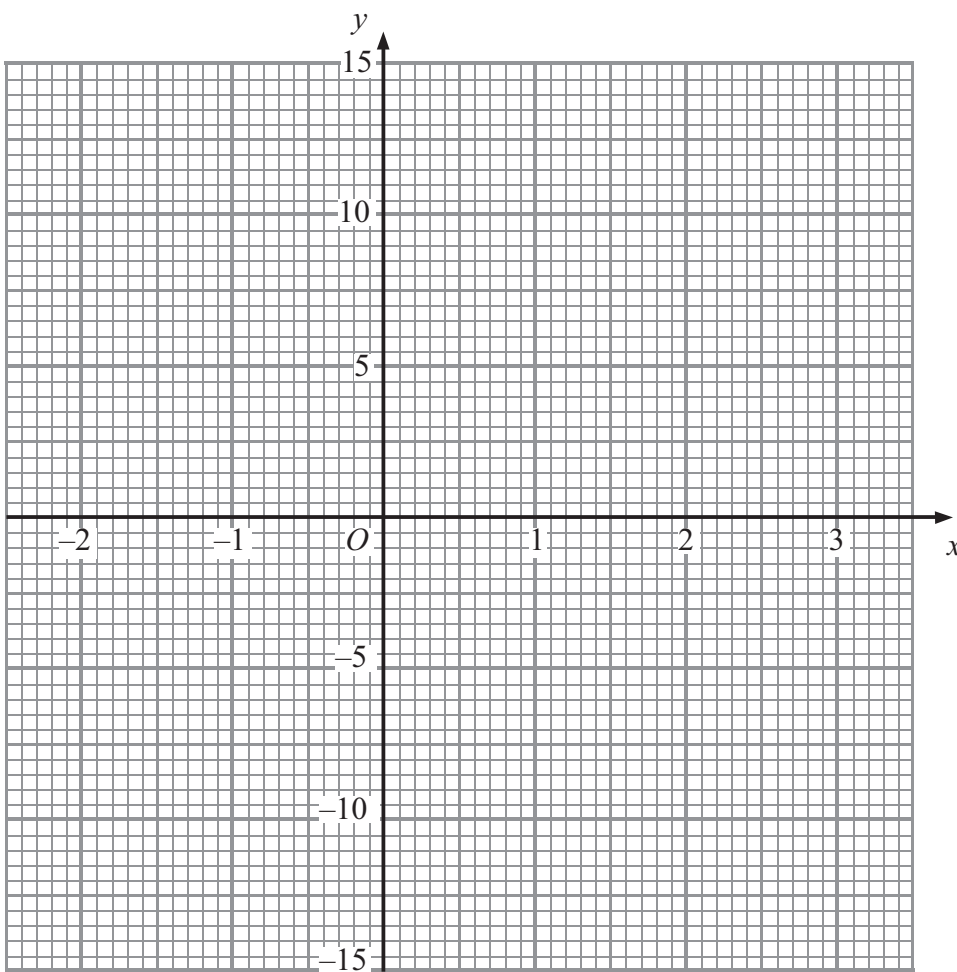


(a) Complete the table of values for $y = x^3 - 3x^2 + 12$

| | | | | | | |
|-----|----|----|---|---|---|---|
| x | -2 | -1 | 0 | 1 | 2 | 3 |
| y | | 8 | | | | |

(2)

(b) On the grid, draw the graph of $y = x^3 - 3x^2 + 12$



(2)

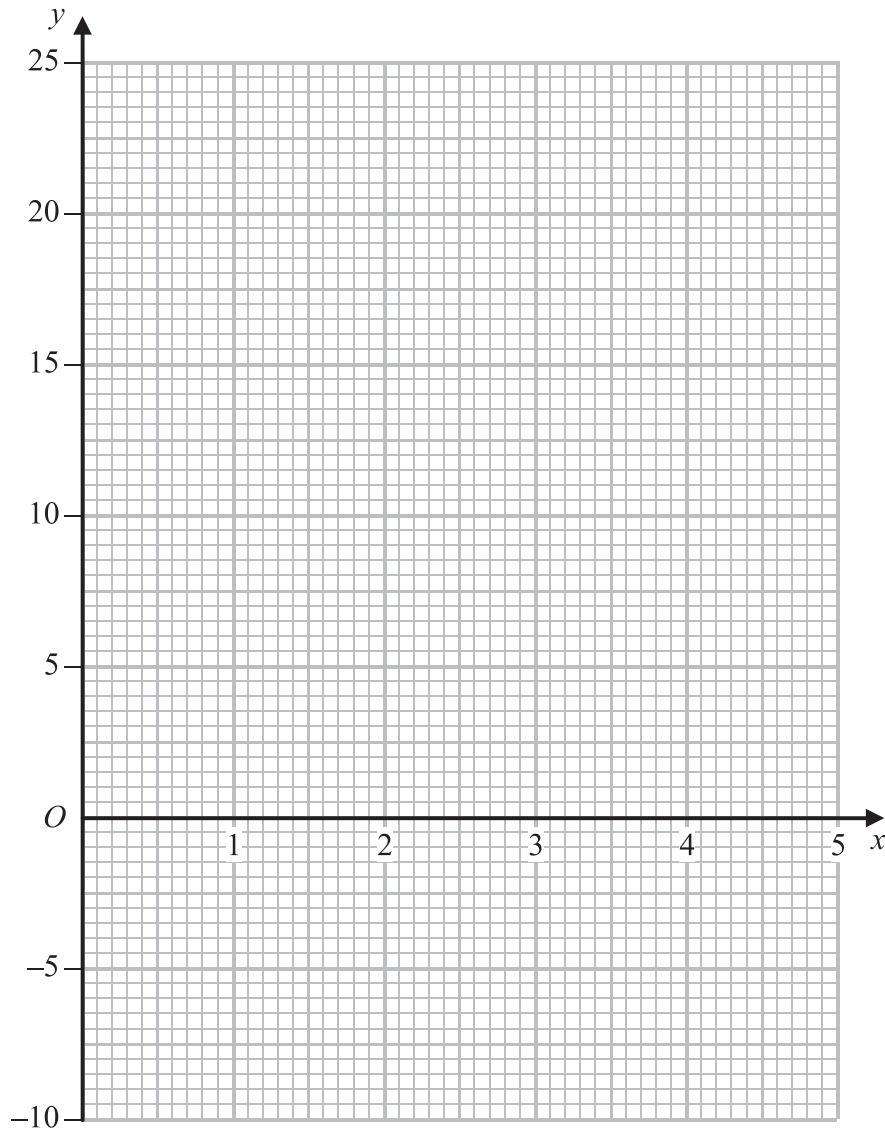


(a) Complete the table of values for $y = x^2 - \frac{3}{x}$

| | | | | | | | |
|-----|-------|----|-----|---|---|---|------|
| x | 0.5 | 1 | 1.5 | 2 | 3 | 4 | 5 |
| y | -5.75 | -2 | | | | | 24.4 |

(2)

(b) On the grid, draw the graph of $y = x^2 - \frac{3}{x}$ for $0.5 \leq x \leq 5$



(2)

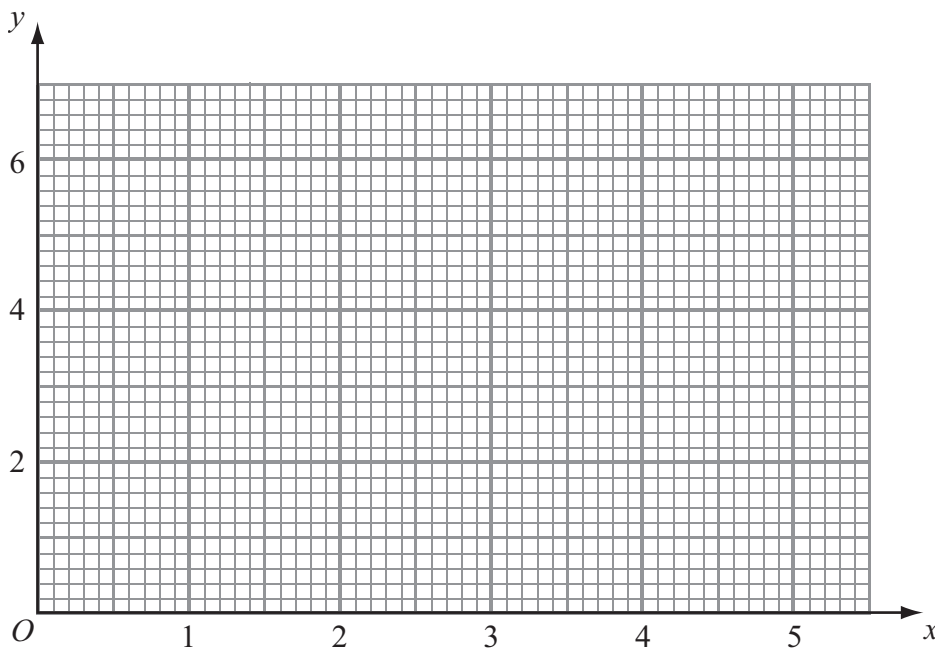


(a) Complete the table of values for $y = x + \frac{1}{x^2}$

| | | | | | | | |
|-----|-----|---|-----|-----|---|---|-----|
| x | 0.5 | 1 | 1.5 | 2 | 3 | 4 | 5 |
| y | | 2 | | 2.3 | | | 5.0 |

(2)

(b) On the grid, draw the graph of $y = x + \frac{1}{x^2}$ for $0.5 \leq x \leq 5$



(2)

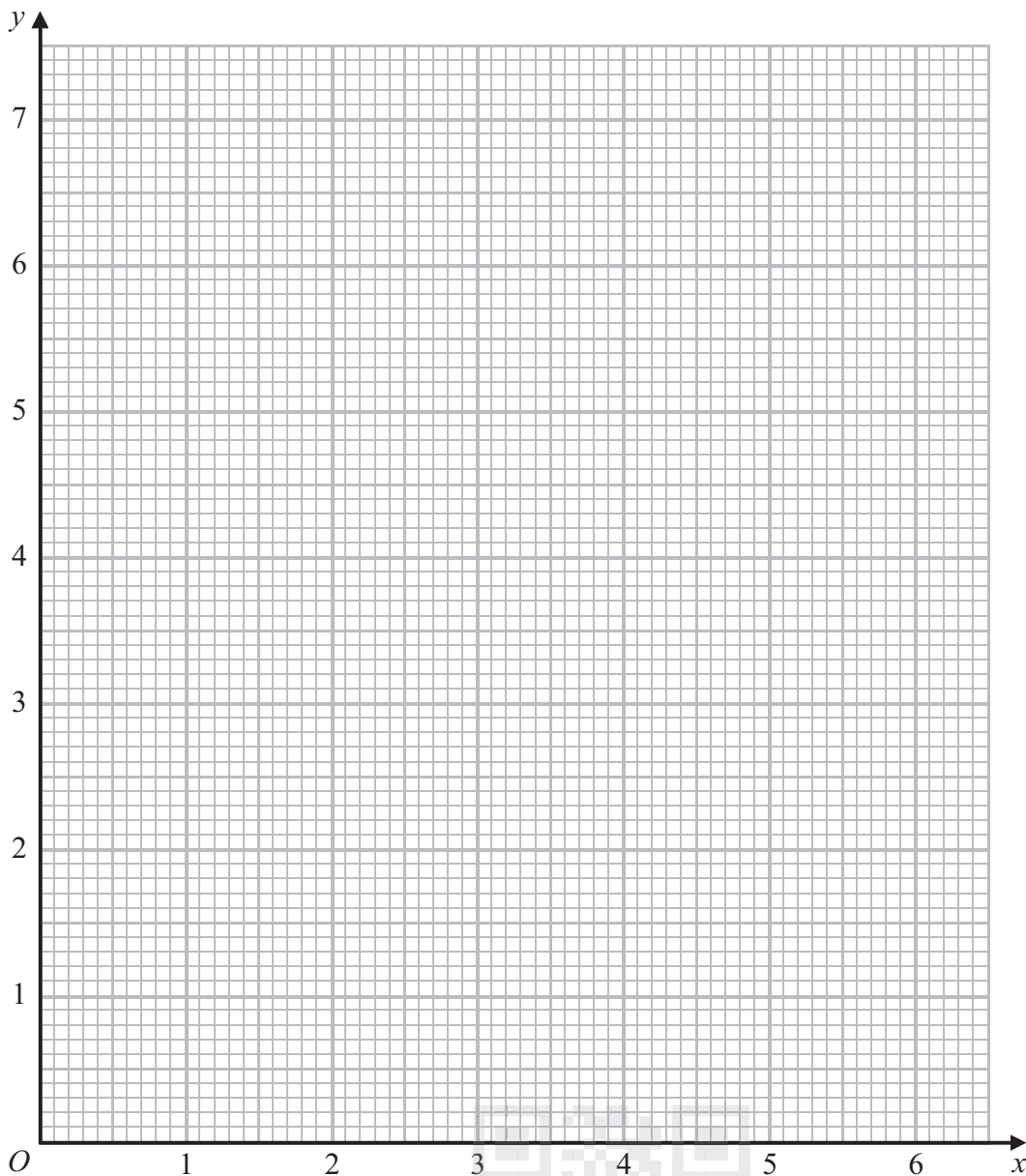


(a) Complete the table of values for $y = \frac{1}{2}\left(x + \frac{9}{x}\right)$

| | | | | | | | |
|-----|---|-----|------|---|-------|-----|---|
| x | 1 | 1.5 | 2 | 3 | 4 | 5 | 6 |
| y | 5 | | 3.25 | | 3.125 | 3.4 | |

(2)

(b) Draw the graph of $y = \frac{1}{2}\left(x + \frac{9}{x}\right)$ for values of x from 1 to 6



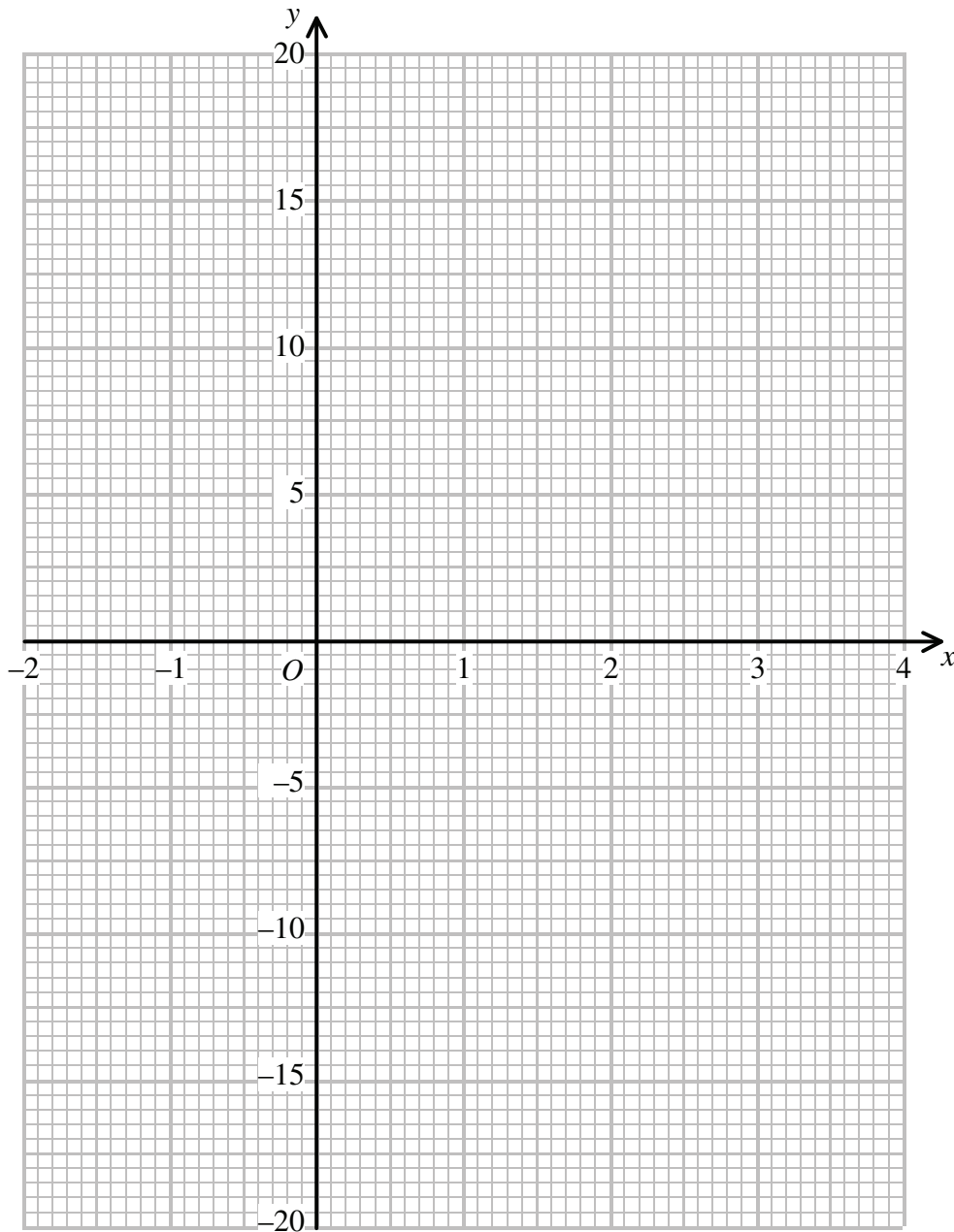
(2)

(a) Complete the table of values for $y = x^3 - 3x^2 + 2$

| | | | | | | | |
|-----|----|----|---|---|---|---|---|
| x | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| y | | -2 | | | | | |

(2)

(b) On the grid, draw the graph of $y = x^3 - 3x^2 + 2$



(2)

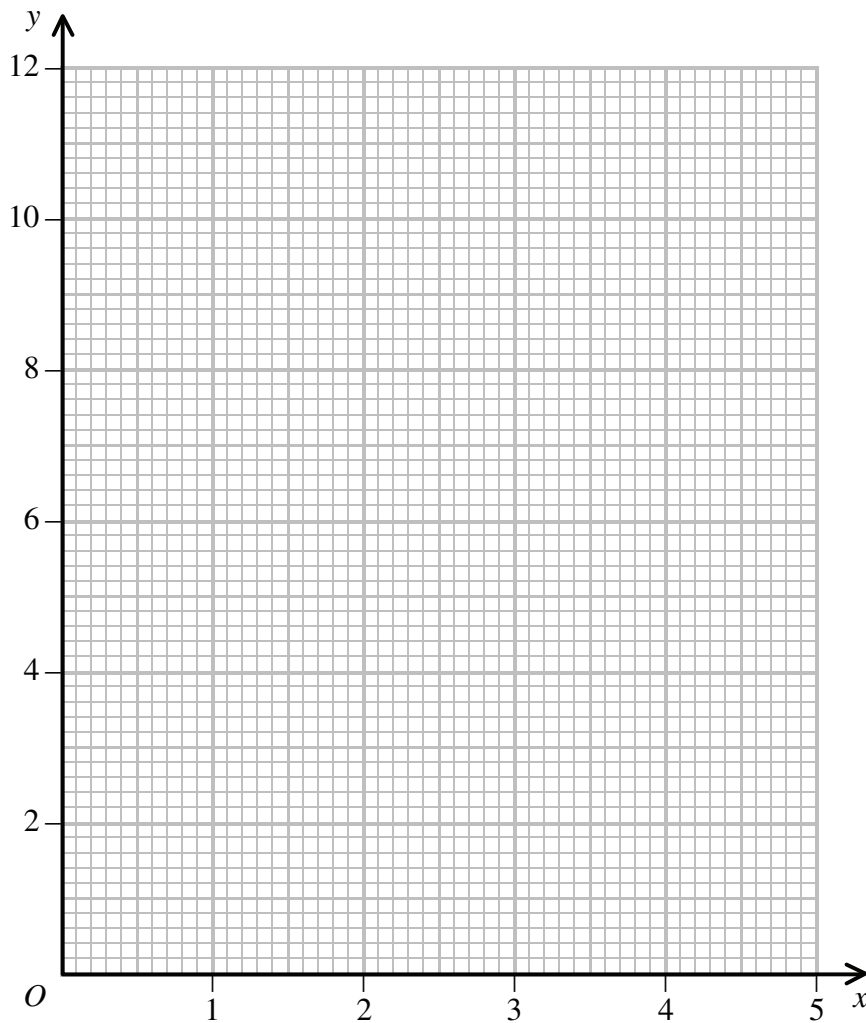


(a) Complete the table of values for $y = x + \frac{2}{x}$

| | | | | | | | | | | |
|-----|------|-----|-----|-----|---|-----|---|-----|---|-----|
| x | 0.2 | 0.4 | 0.6 | 0.8 | 1 | 1.5 | 2 | 3 | 4 | 5 |
| y | 10.2 | | 3.9 | | 3 | 2.8 | | 3.7 | | 5.2 |

(2)

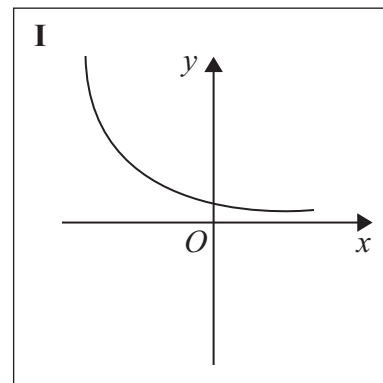
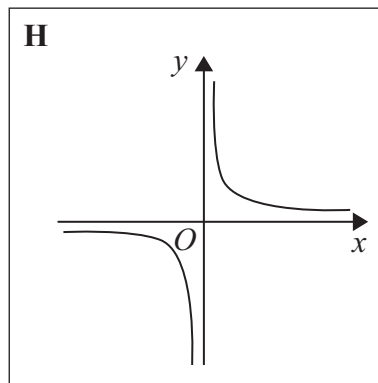
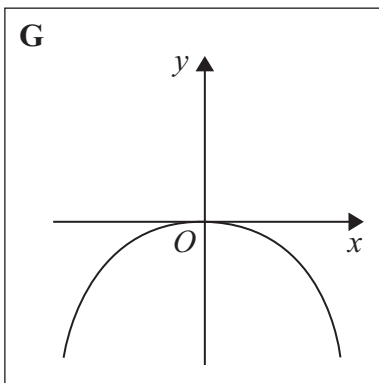
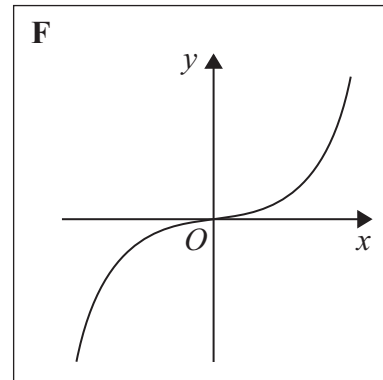
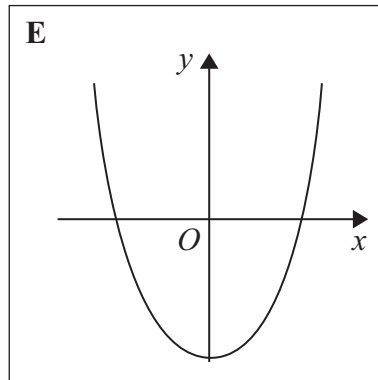
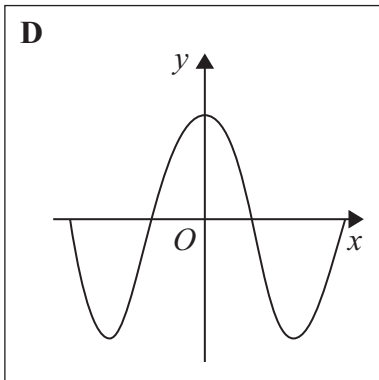
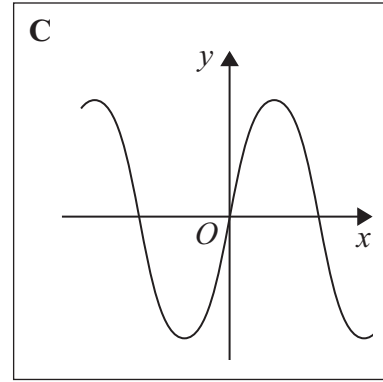
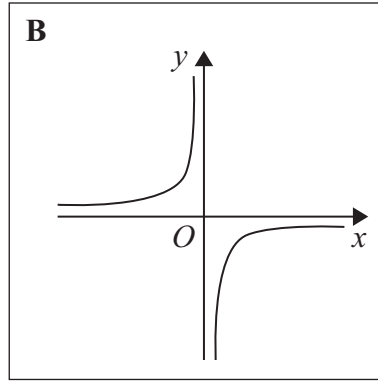
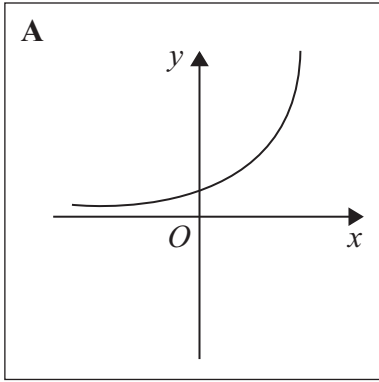
(b) On the grid, draw the graph of $y = x + \frac{2}{x}$ for $0.2 \leq x \leq 5$



(2)



Here are some graphs.



In the table below, match each equation with the letter of its graph.

| Equation | Graph |
|-------------------|-------|
| $y = \sin x$ | |
| $y = x^3 + 4x$ | |
| $y = 2^x$ | |
| $y = \frac{4}{x}$ | |

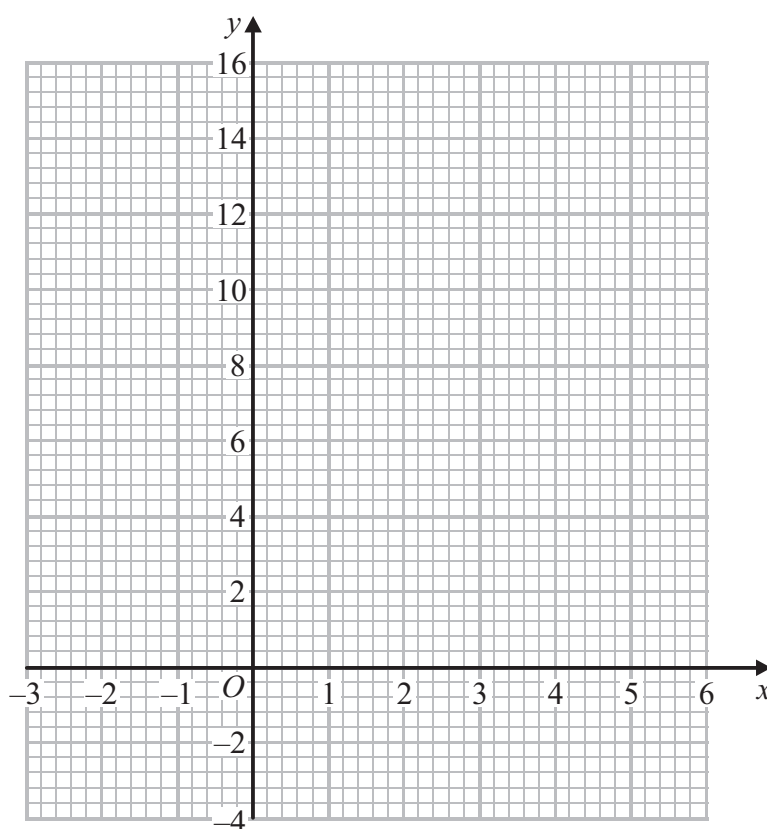


(a) Complete the table of values for $y = x^2 - 4x + 2$

| | | | | | | | | |
|-----|----|----|---|---|---|----|---|---|
| x | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| y | 14 | | 2 | | | -1 | 2 | |

(2)

(b) On the grid, draw the graph of $y = x^2 - 4x + 2$ for values of x from -2 to 5



(2)

The point $P(k, 4)$ where $k > 0$ lies on the graph of $y = x^2 - 4x + 2$

(c) Use your graph to find an estimate for the value of k .

(1)

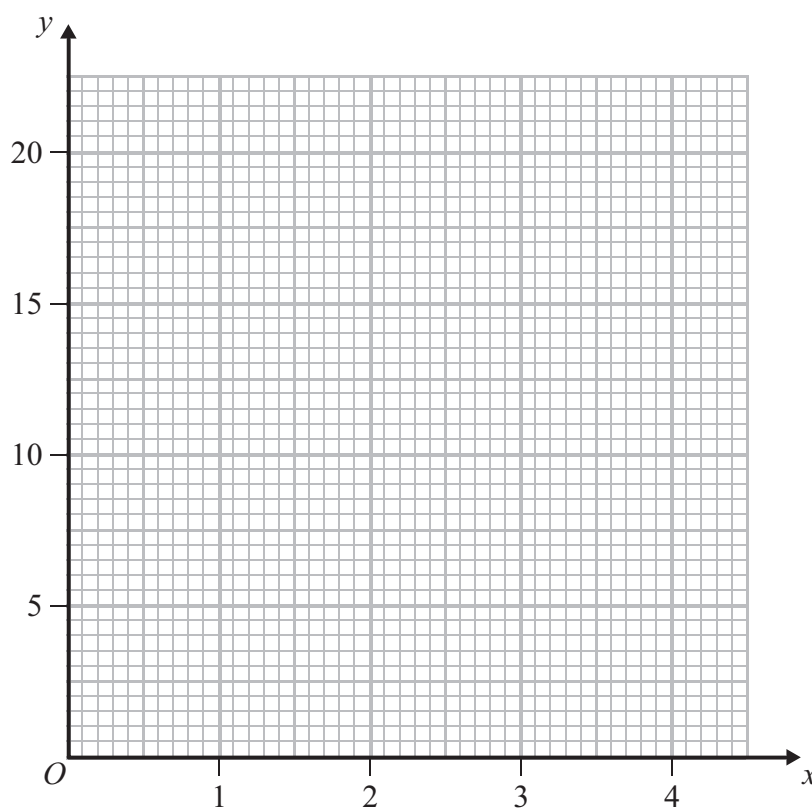


(a) Complete the table of values for $y = x^2 + \frac{2}{x}$

| | | | | | | | | |
|-----|-------|-------|-----|---|------|---|------|---|
| x | 0.1 | 0.2 | 0.5 | 1 | 1.5 | 2 | 3 | 4 |
| y | 20.01 | 10.04 | | 3 | 3.58 | 5 | 9.67 | |

(1)

(b) On the grid, draw the graph of $y = x^2 + \frac{2}{x}$ for $0.1 \leq x \leq 4$



(2)

(c) Use your graph to find estimates for the solutions of $x^2 + \frac{2}{x} = 14$ in the interval $0.1 \leq x \leq 4$

Give your estimates correct to 1 decimal place.



.....
(2)